

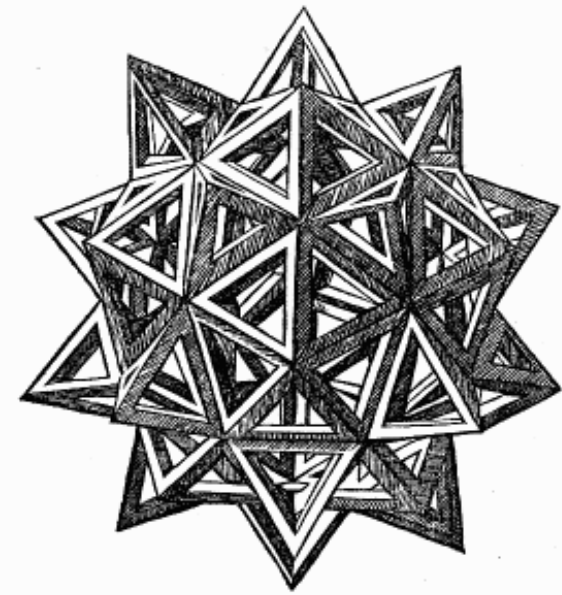
# Symmetries in Nuclear and Particle Physics

- 1. Symmetries in Physics
- 2. Interacting Boson Model
- 3. Nuclear Supersymmetry
- 4. Quark Model
- 5. Unquenched Quark Model



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# Temario



- Introducción
- Modelo de quarks
- Grados de libertad exóticos
- Modelo de quarks "unquenched"
- Resultados
- Resumen y conclusiones

# Structure of the Nucleon

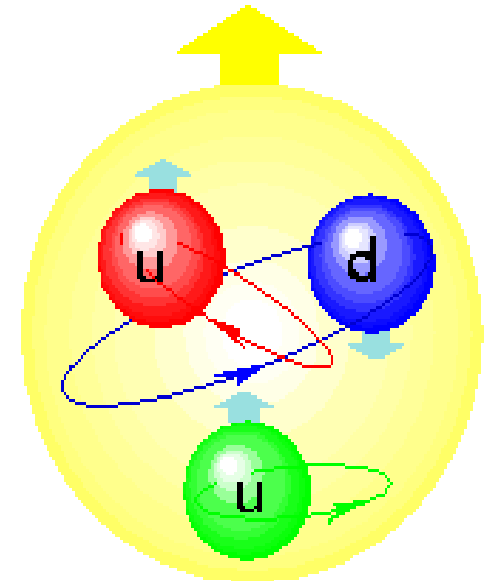
- Anomalous magnetic moment (Stern, 1930's)

$$\mu_p = 2.793 \mu_N, \quad \mu_n = -1.913 \mu_N$$

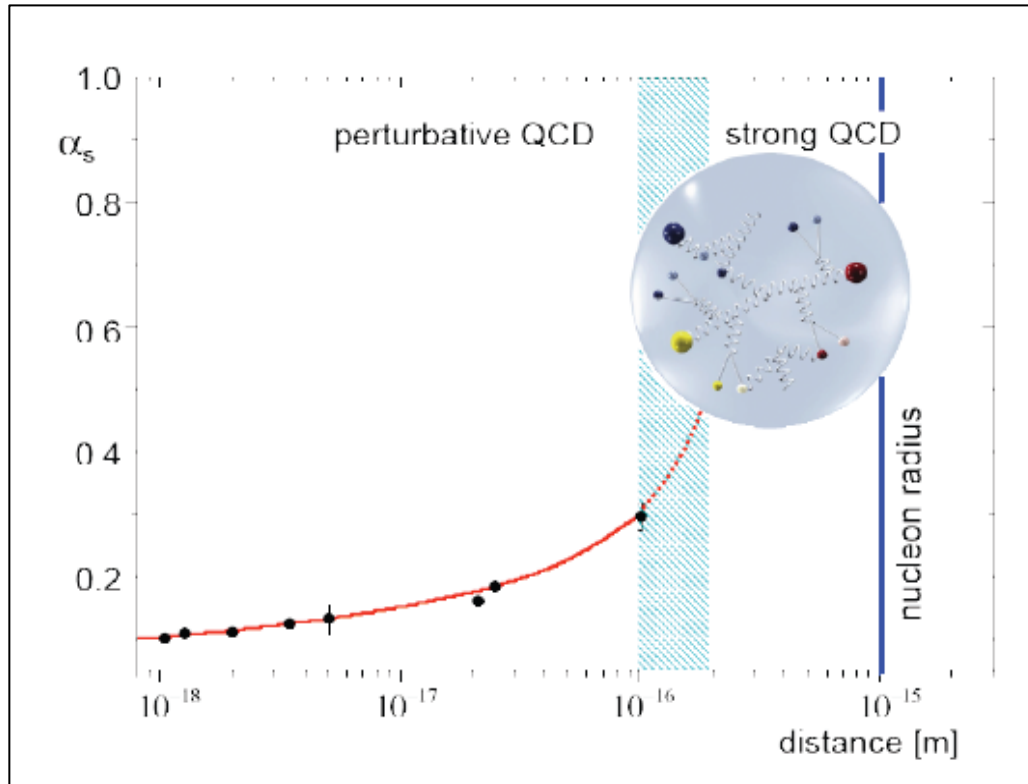
- Radius (Hofstadter, 1950's)

$$r_p = 0.862 \text{ fm}$$

- Quark structure of the proton (Friedman, Kendall, Taylor, 1968)
- Spin crisis (EMC, 1988)
- Flavor asymmetry (NMC, 1991)
- Form factor ratio  $G_E/G_M$  (2000's)
- Strangeness (2000's)



# Baryons: Strong QCD



- Lattice QCD
- Chiral PT as EFT of QCD
- Effective degrees of freedom
- Quark models

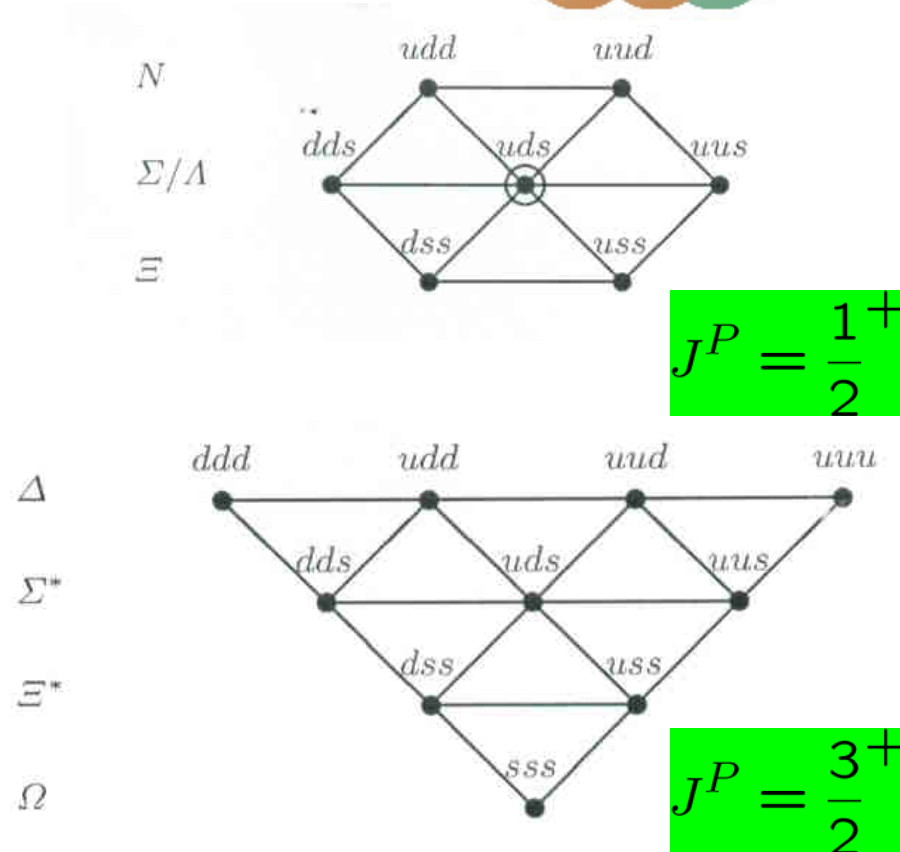
# Constituent Quark Model

- Octet baryons ( $qqq$ )
- Decuplet baryons ( $qqq$ )
- Magnetic moments

$$\frac{\mu_p}{\mu_n} = -\frac{3}{2} \quad -1.46 \text{ exp}$$

- Photocouplings, helicity amplitudes, form factors, strong decays, ...

Gell-Mann, Ne'eman, Zweig 1961-1964



# Magnetic Moments

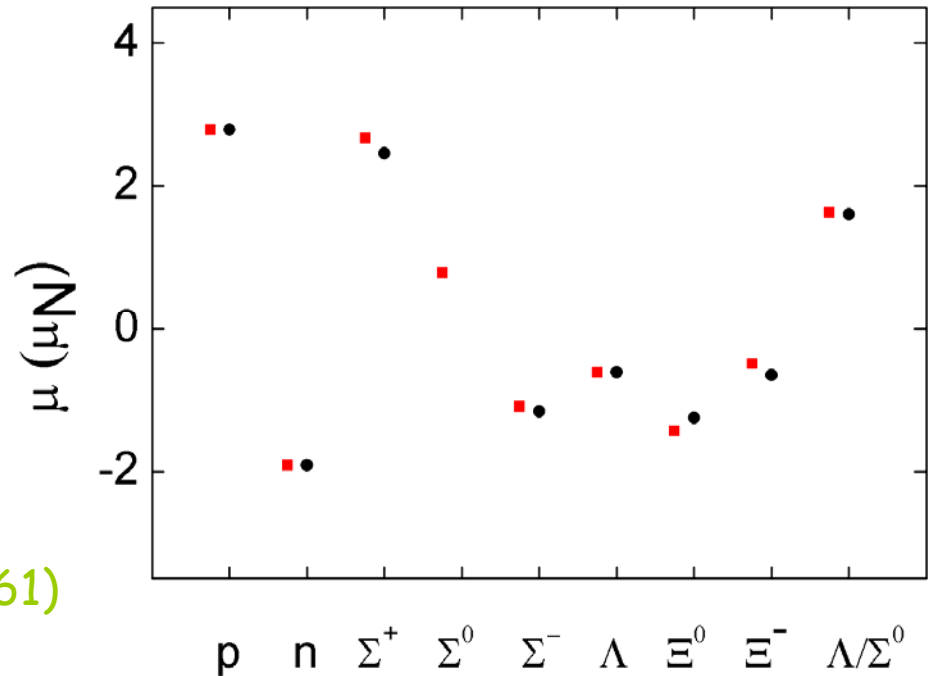
$$\begin{aligned} \mu_p &= (4\mu_u - \mu_d)/3 \\ \mu_n &= (4\mu_d - \mu_u)/3 \\ \mu_\Lambda &= \mu_s \\ \mu_{\Sigma^+} &= (4\mu_u - \mu_s)/3 \\ \mu_{\Sigma^0} &= (2\mu_u + 2\mu_d - \mu_s)/3 \\ \mu_{\Sigma^-} &= (4\mu_d - \mu_s)/3 \\ \mu_{\Xi^0} &= (4\mu_s - \mu_u)/3 \\ \mu_{\Xi^-} &= (4\mu_s - \mu_d)/3 \\ \mu_{\Sigma^0\Lambda} &= (\mu_u - \mu_d)/\sqrt{3} \end{aligned}$$

$$\mu_u = 1.852 \mu_N$$

$$\mu_d = -0.972 \mu_N$$

$$\mu_s = -0.613 \mu_N$$

CQM  
Experiment



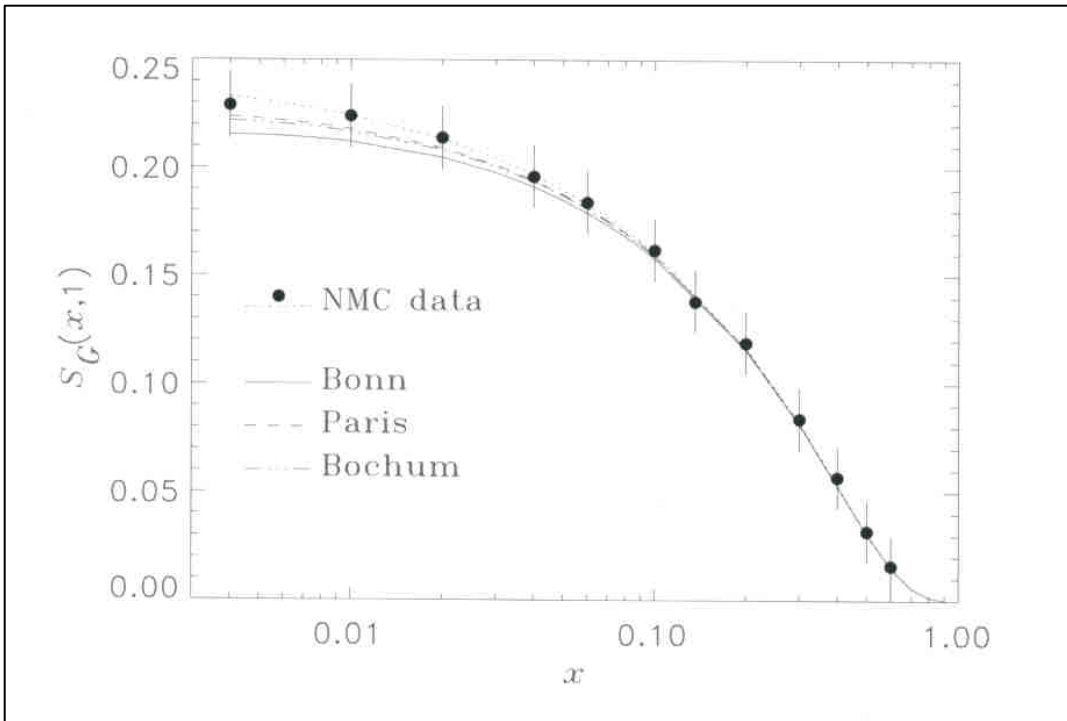
Coleman & Glashow, PRL 6, 423 (1961)

Beg, Lee & Pais, PRL 13, 514 (1964)

# Problem 1: Flavor asymmetry

- Gottfried sum rule

$$S_G = \int_0^1 dx \frac{F_{2p}(x) - F_{2n}(x)}{x} = \frac{1}{3} - \frac{2}{3} \int_0^1 dx [\bar{d}(x) - \bar{u}(x)]$$



$$S_G(x, 1) = \int_x^1 dx' \frac{F_{2p}(x') - F_{2n}(x')}{x'}$$

$$S_G = 0.2281 \pm 0.0065$$

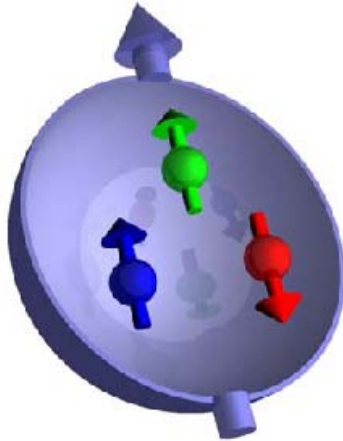
$$\begin{aligned} A(p) &= \int_0^1 dx [\bar{d}(x) - \bar{u}(x)] \\ &= 0.16 \pm 0.01 \end{aligned}$$

Excess:  $\bar{d} > \bar{u}$



# Problem 2: Proton Spin

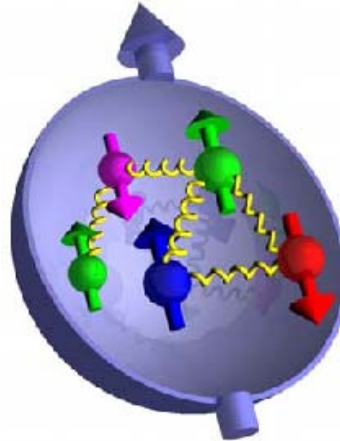
1980's



Naive quark model  
3 valence quarks

$$\frac{1}{2} = \frac{1}{2}(\Delta u + \Delta d)$$

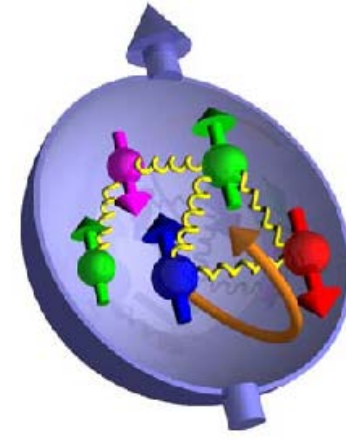
1990's



QCD: contributions from  
sea quarks and gluons

$$\frac{1}{2} = \frac{1}{2}(\Delta u + \Delta d + \Delta s) + \Delta G + \Delta L$$

2000's



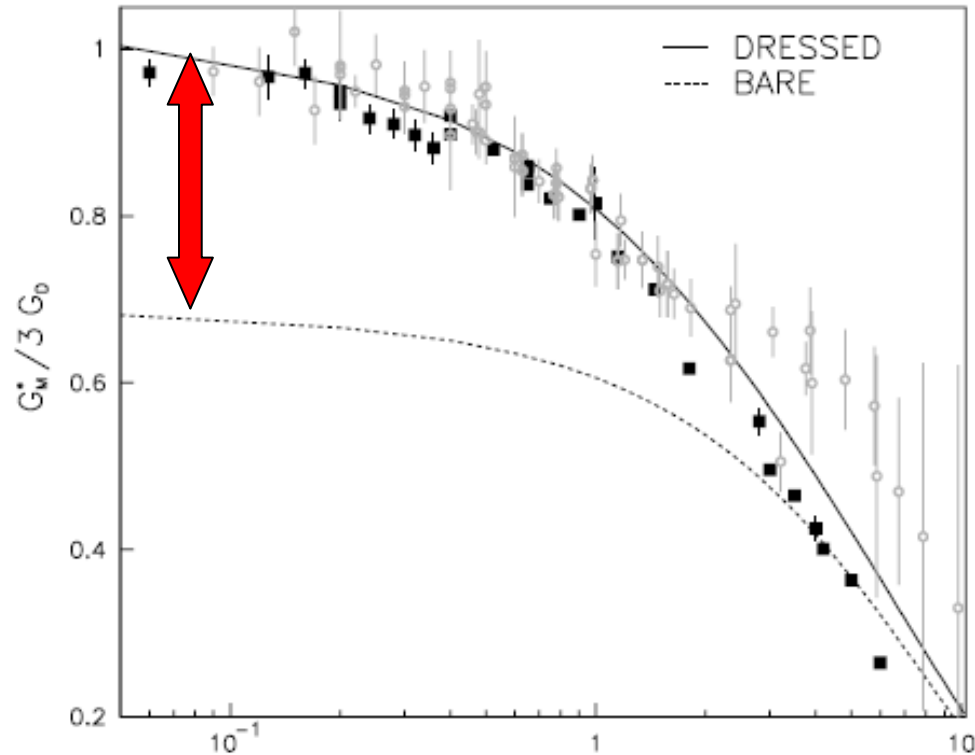
.. and orbital angular  
momentum

$$\left. \begin{aligned} \Delta u &= 0.842 \\ \Delta d &= -0.427 \\ \Delta s &= -0.085 \end{aligned} \right\}$$

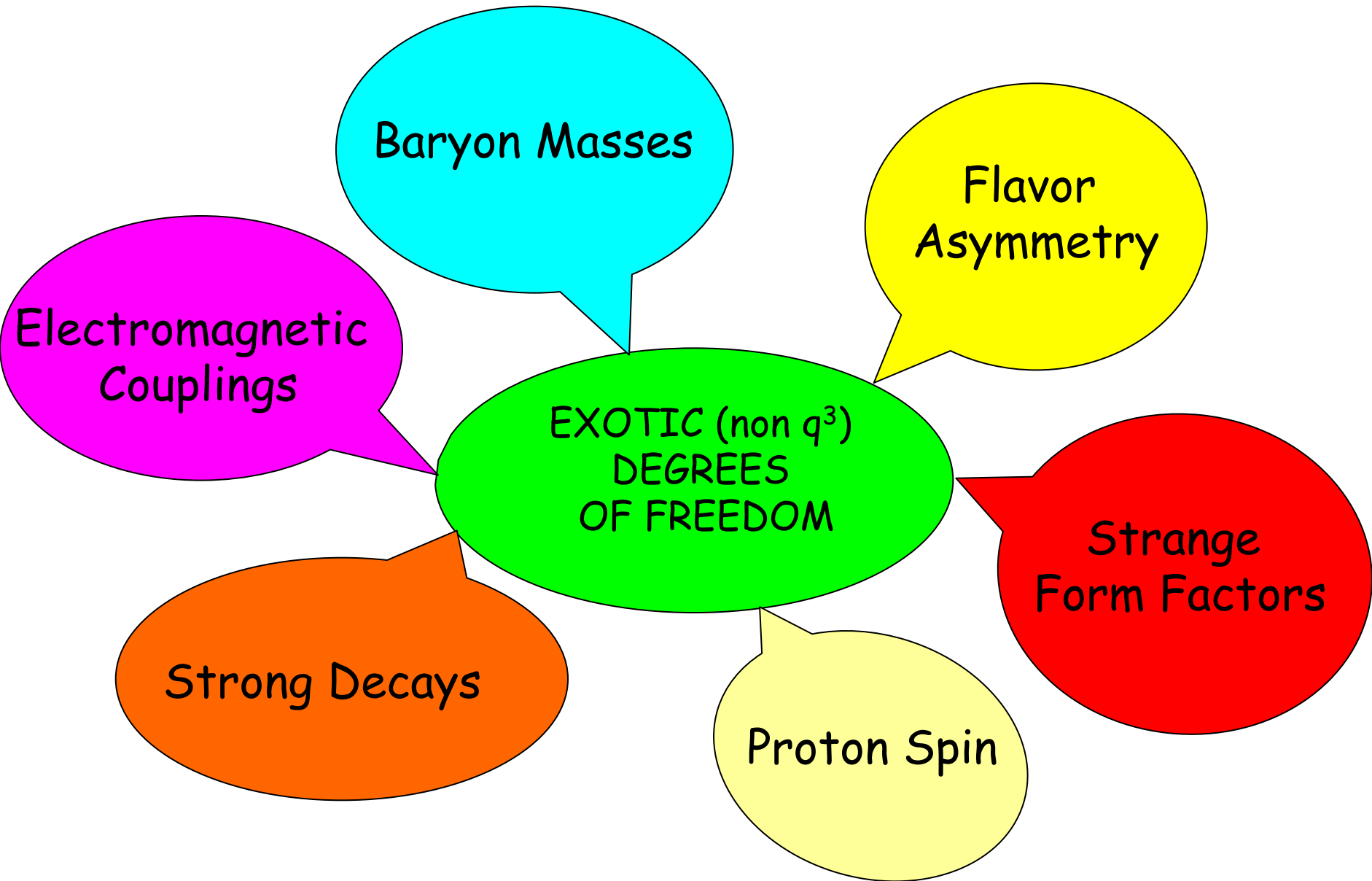
$$\Delta \Sigma = 0.330 \pm 0.039$$

HERMES, PRD 75, 012007 (2007)  
COMPASS, PLB 647, 8 (2007)

# Problem 3: Delta(1232)

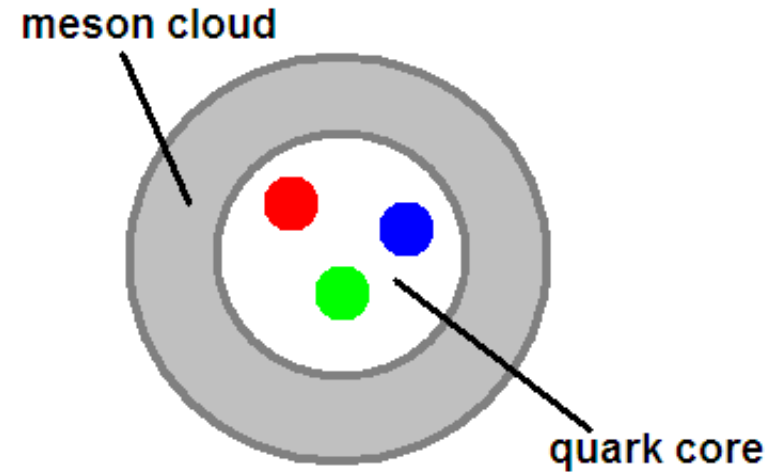


Julia-Diaz et al, PRC 75, 015205 (2007)

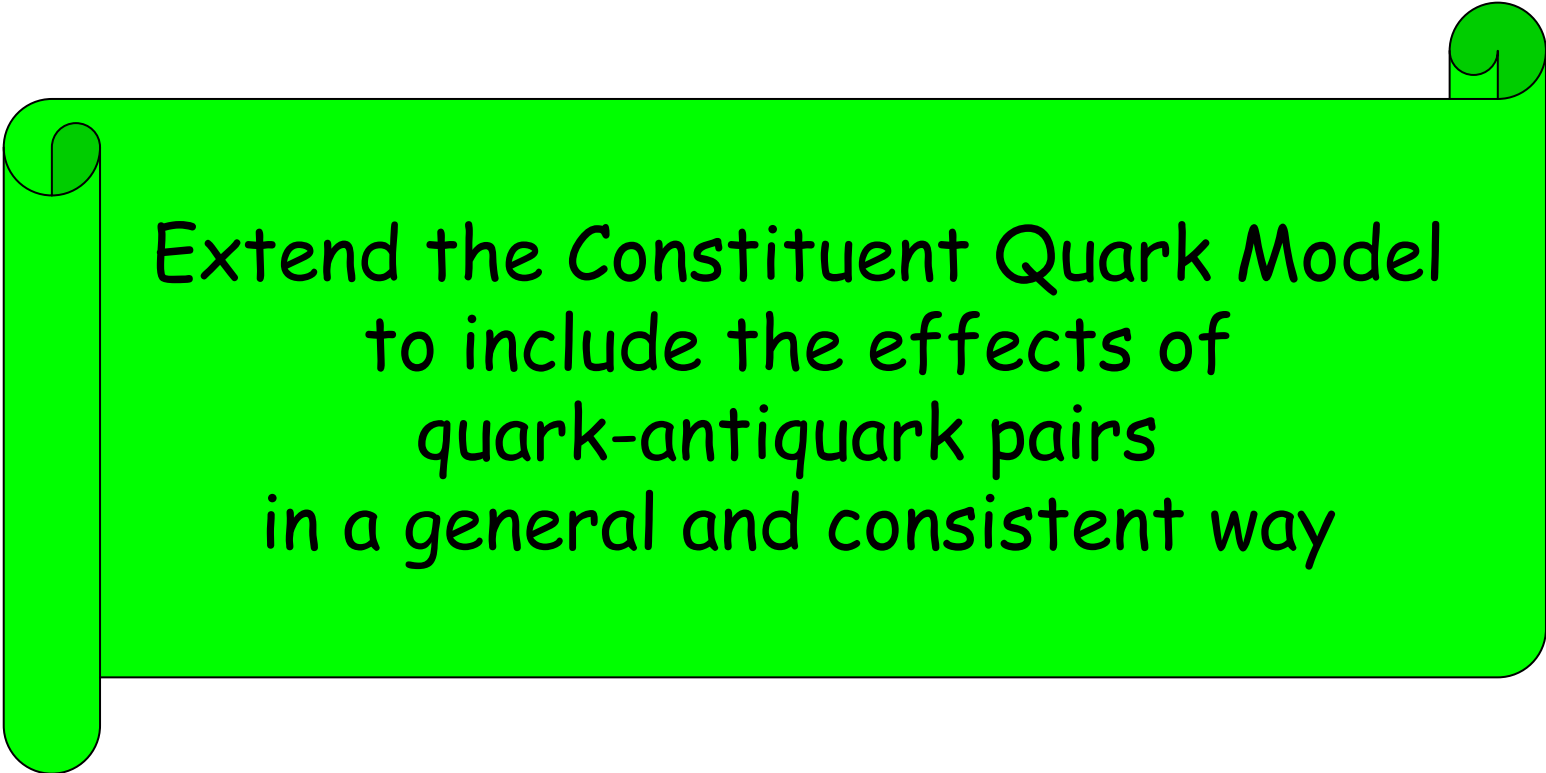


# Exotic Degrees of Freedom

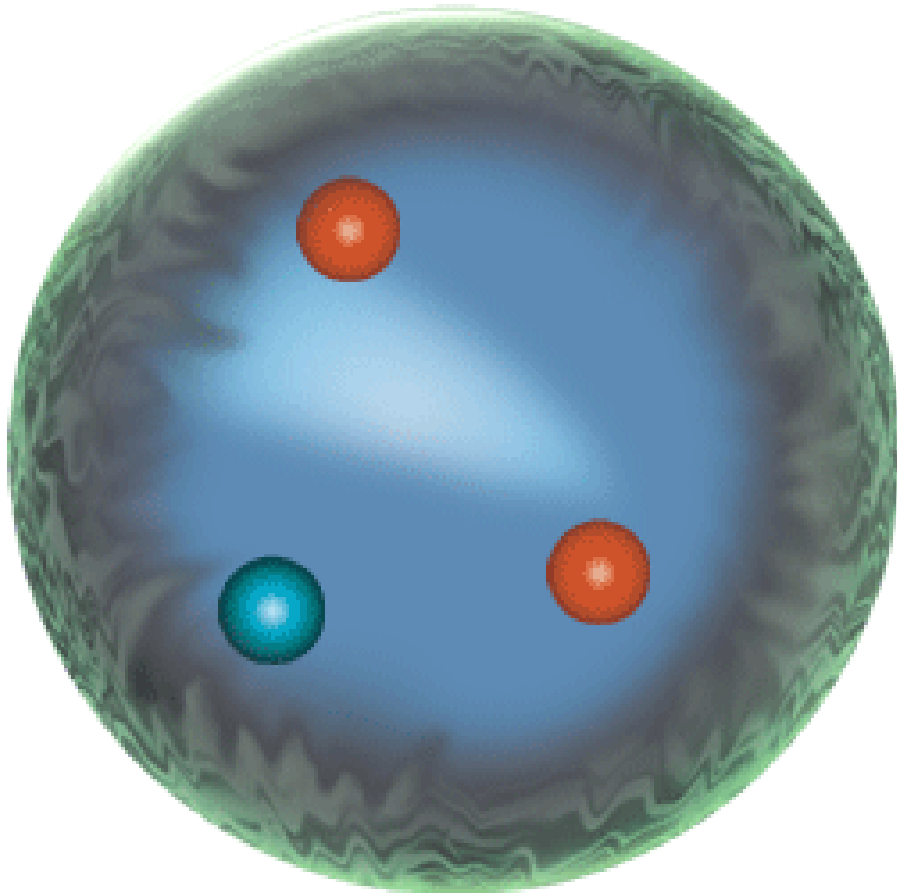
- Quark-antiquark pairs: pentaquarks, meson-cloud models (Thomas, Speth, Kaiser, Weise, Oset, Brodsky, Ma, Isgur, ...)
- Higher-Fock components (Riska, Zou, ...)



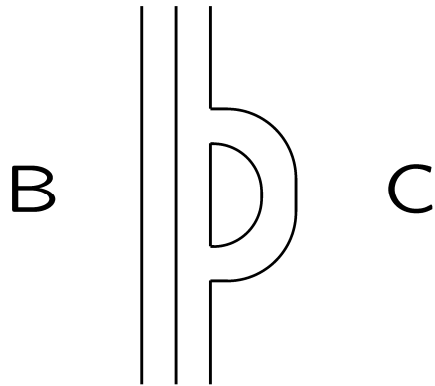
$$\psi = \mathcal{N} \left[ \psi(q^3) + \alpha \psi(q^3 - q\bar{q}) \right]$$



Extend the Constituent Quark Model  
to include the effects of  
quark-antiquark pairs  
in a general and consistent way



# Unquenched Quark Model



Strange quark-antiquark pairs in the proton with h.o. wave functions

Tornqvist & Zenczykowski (1984)  
Geiger & Isgur, PRD 55, 299 (1997)  
Isgur, NPA 623, 37 (1997)

- Pair-creation operator with  $^3P_0$  quantum numbers of vacuum
- **Important: sum over a large tower of intermediate states to preserve the phenomenological successes of CQM**

## Geiger & Isgur, PRD 55, 299 (1997)

It would be desirable to devise tests of the mechanisms underlying the delicate cancellations which conspire to hide the effects of the sea in the picture presented here. It also seems very worthwhile to extend this calculation to  $uu$  and  $dd$  loops. Such an extension could reveal the origin of the observed violations [38] of the Gottfried sum rule [39] and also complete our understanding of the origin of the spin crisis. From our previous calculations [4], the effects of “un-

## Extensions

Bijker & Santopinto,  
PRC 80, 065210 (2009)

- Any initial baryon or baryon resonance
- Any flavor of the quark-antiquark pair
- Any model of baryons and mesons



# Formalism

$$|\psi_A\rangle = \mathcal{N} \left\{ |A\rangle + \sum_{BCIJ} \int d\vec{K} k^2 dk |BC, l, J; \vec{K}, k\rangle \frac{\langle BC, l, J; \vec{K}, k | T^\dagger | A\rangle}{M_A - E_B - E_C} \right\}$$

Three-quark configuration  
SU(3) flavor symmetry

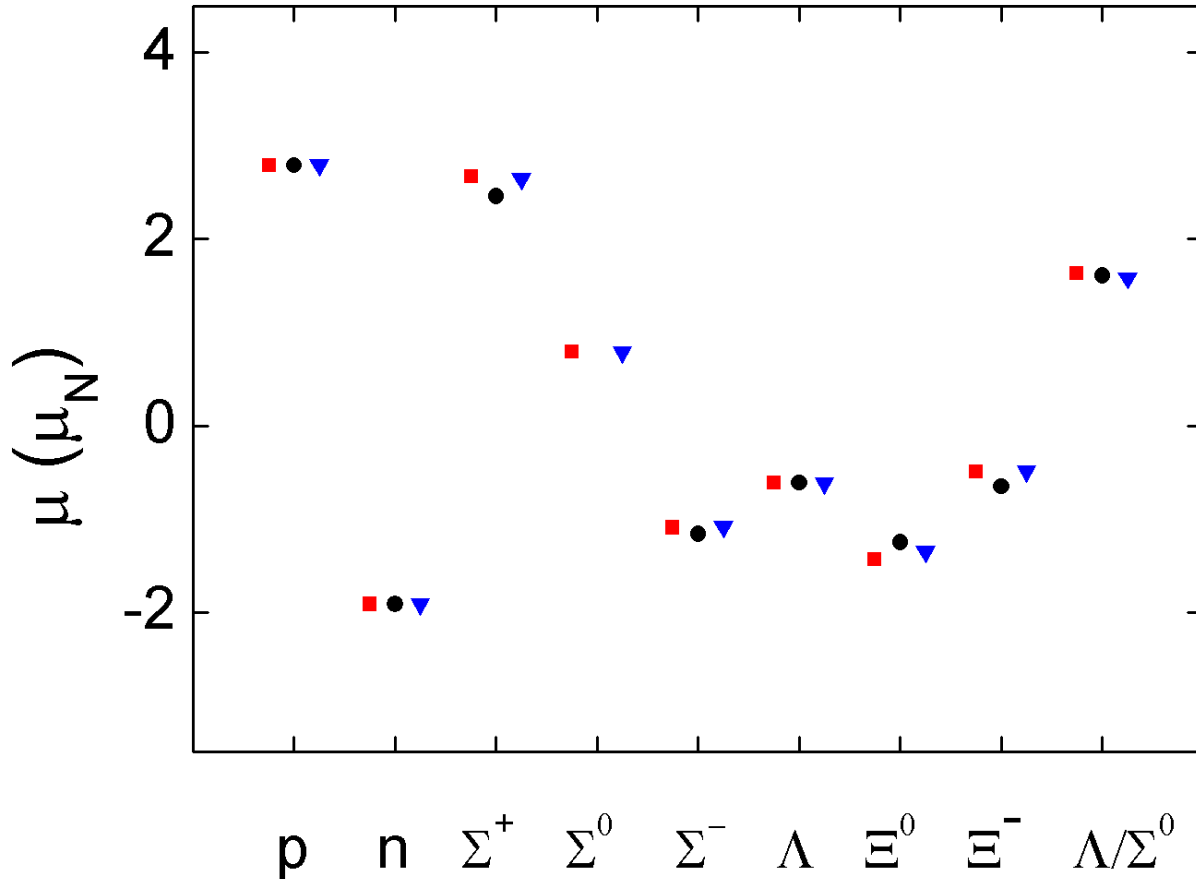
Five-quark component  
Isospin symmetry

Pair-creation operator:  $T^\dagger = T^\dagger(^3P_0)$   
L=S=1, J=0, color singlet, flavor singlet

# Unquenched Quark Model

- Harmonic oscillator quark model
- Sum over intermediate meson-baryon states includes for each oscillator shell all possible spin-flavor states
- Number of oscillator shells  $N_B, N_C \leq 5$
- Oscillator size parameters taken for baryons and mesons taken from literature (Capstick, Isgur, Karl)
- Smearing of the pair-creation vertex (Geiger, Isgur)
- Strength of  $^3P_0$  coupling taken from literature on strong decays of baryons (Capstick, Roberts)
- No attempt to optimize the parameters

# 1. Magnetic Moments



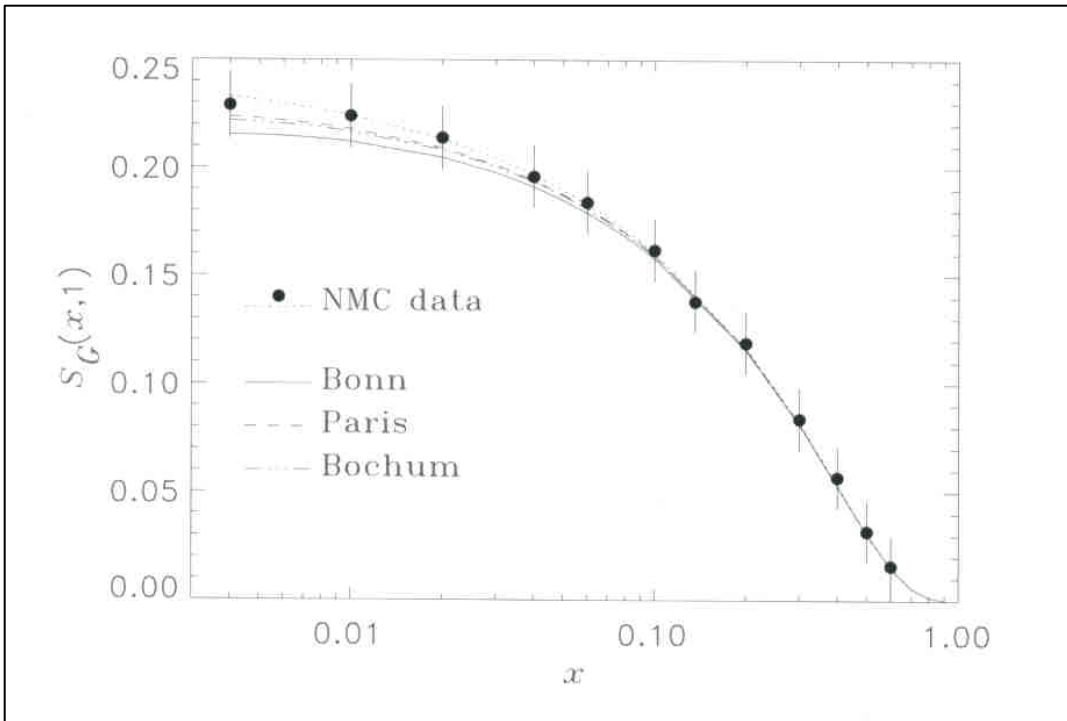
CQM  
 Experiment  
 Unquenched QM

	CQM	UQM
$\mu_u$	1.852	2.044
$\mu_d$	-0.972	-0.959
$\mu_s$	-0.613	-0.567

## 2. Flavor asymmetry

- Gottfried sum rule

$$S_G = \int_0^1 dx \frac{F_{2p}(x) - F_{2n}(x)}{x} = \frac{1}{3} - \frac{2}{3} \int_0^1 dx [\bar{d}(x) - \bar{u}(x)]$$



$$S_G(x, 1) = \int_x^1 dx' \frac{F_{2p}(x') - F_{2n}(x')}{x'}$$

$$S_G = 0.2281 \pm 0.0065$$

$$\begin{aligned} A(p) &= \int_0^1 dx [\bar{d}(x) - \bar{u}(x)] \\ &= 0.16 \pm 0.01 \end{aligned}$$

Excess:  $\bar{d} > \bar{u}$

# Proton Sea

	$\mathcal{A}(p)$
E866 2001	$0.118 \pm 0.012$
NMC 1994	$0.147 \pm 0.039$
NMC 1997	$0.1578 \pm 0.0097$
HERMES 1998	$0.16 \pm 0.03$
Unquenched QM	0.151

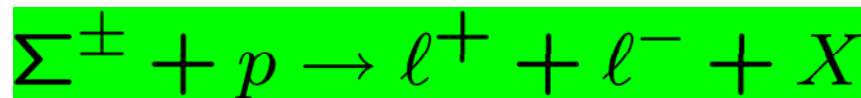
Flavor asymmetry: nonperturbative QCD  
Pauli blocking (Field & Feynman, 1977) **too small**  
Pion dressing of the nucleon ( $n-\pi^+$  channel)  
(Thomas et al., 1983, Henley & Miller, 1990)

# Other Models

- Baryon asymmetry

Model	$\mathcal{A}(\Sigma^+)/\mathcal{A}(p)$	$\mathcal{A}(\Xi^0)/\mathcal{A}(p)$
Unquenched QM	0.833	-0.005
Octet couplings	0.353	-0.647
Chiral QM	2	1
Balance Model	3.083	2.075

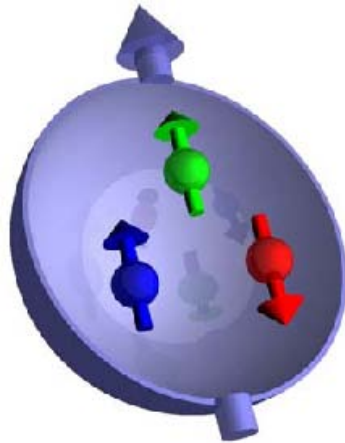
- Flavor asymmetry of  $\Sigma$  hyperons can be measured using the Drell-Yan process in hyperon-induced dilepton production with  $\Sigma$ -hyperon beams on protons



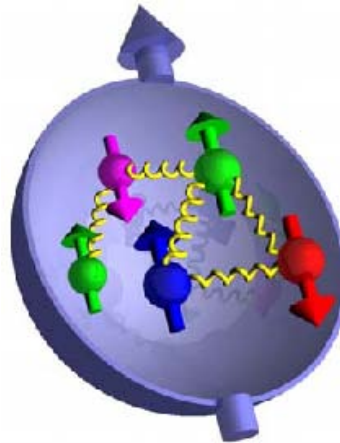
Alberg et al., PLB 389, 367 (1996)  
NPA 644, 93 (1998)

# 3. Proton Spin Crisis

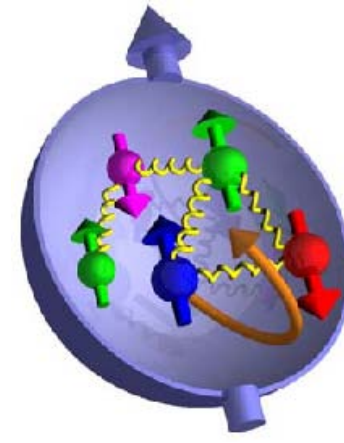
1980's



1990's



2000's



Naive parton model  
3 valence quarks

$$\frac{1}{2} = \frac{1}{2}(\Delta u + \Delta d)$$

QCD: contributions from  
sea quarks and gluons

$$\frac{1}{2} = \frac{1}{2}(\underbrace{\Delta u + \Delta d + \Delta s}_{\Delta \Sigma}) + \Delta G + \Delta L$$

.. and orbital angular  
momentum

$$\left. \begin{array}{l} \Delta u = 0.842 \\ \Delta d = -0.427 \\ \Delta s = -0.085 \end{array} \right\} \Delta \Sigma = 0.330 \pm 0.039$$

HERMES, PRD 75, 012007 (2007)  
COMPASS, PLB 647, 8 (2007)

# Proton Spin

- COMPASS@CERN:  $\Delta G$  is small
- Unquenched quark model

Ageev et al., PLB 633, 25 (2006)  
Platchkov, NPA 790, 58 (2007)

		CQM	Unquenched QM		
			Valence	Sea	Total
$p$	$\Delta\Sigma$	1	0.38	0.30	0.68
	$2\Delta L$	0	0.00	0.32	0.32
	$2\Delta J$	1	0.38	0.62	1.00

- More than half of the proton spin from the sea!
- Orbital angular momentum related to flavor asymmetry

$$|\psi_N\rangle = \frac{1}{\sqrt{1+a^2+b^2}} [ |N\rangle + a|N\pi\rangle + b|\Delta\pi\rangle ]$$

$$\Delta L = \mathcal{A}(p) = \frac{2a^2 - b^2}{3(1+a^2+b^2)}$$

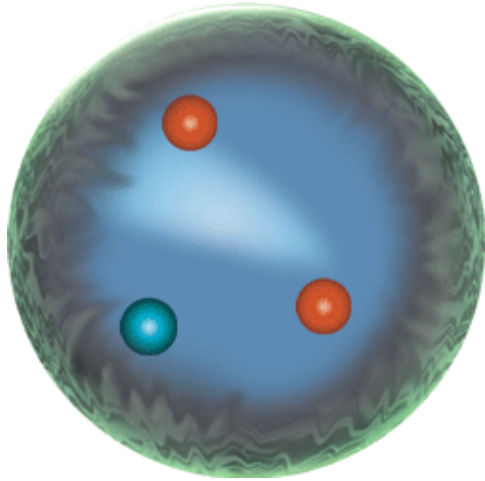
Garvey, PRC 81, 055212 (2010)

- Importance of orbital angular momentum

Myhrer & Thomas, 2008

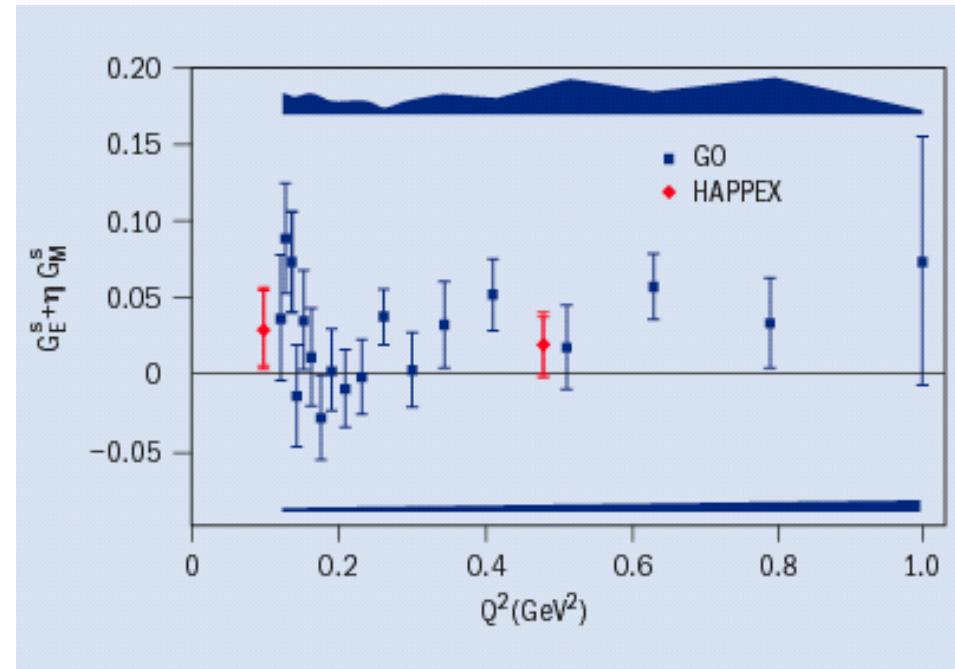


# 4. Strangeness in the Proton

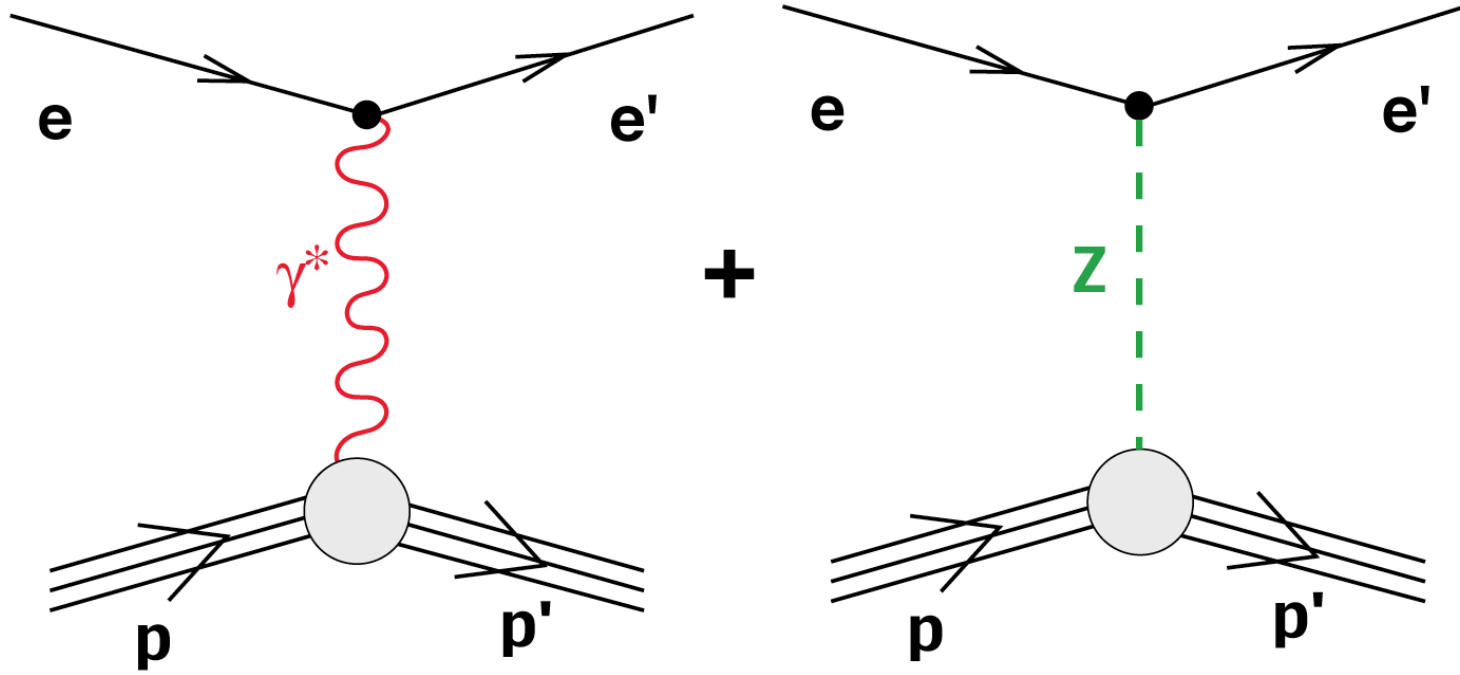


The strange (anti)quarks come uniquely from the sea: there is no contamination from up or down valence quarks

New data from parity violating electron scattering



"There is no excellent beauty that hath not some strangeness in the proportion"  
(Francis Bacon, 1561-1626)

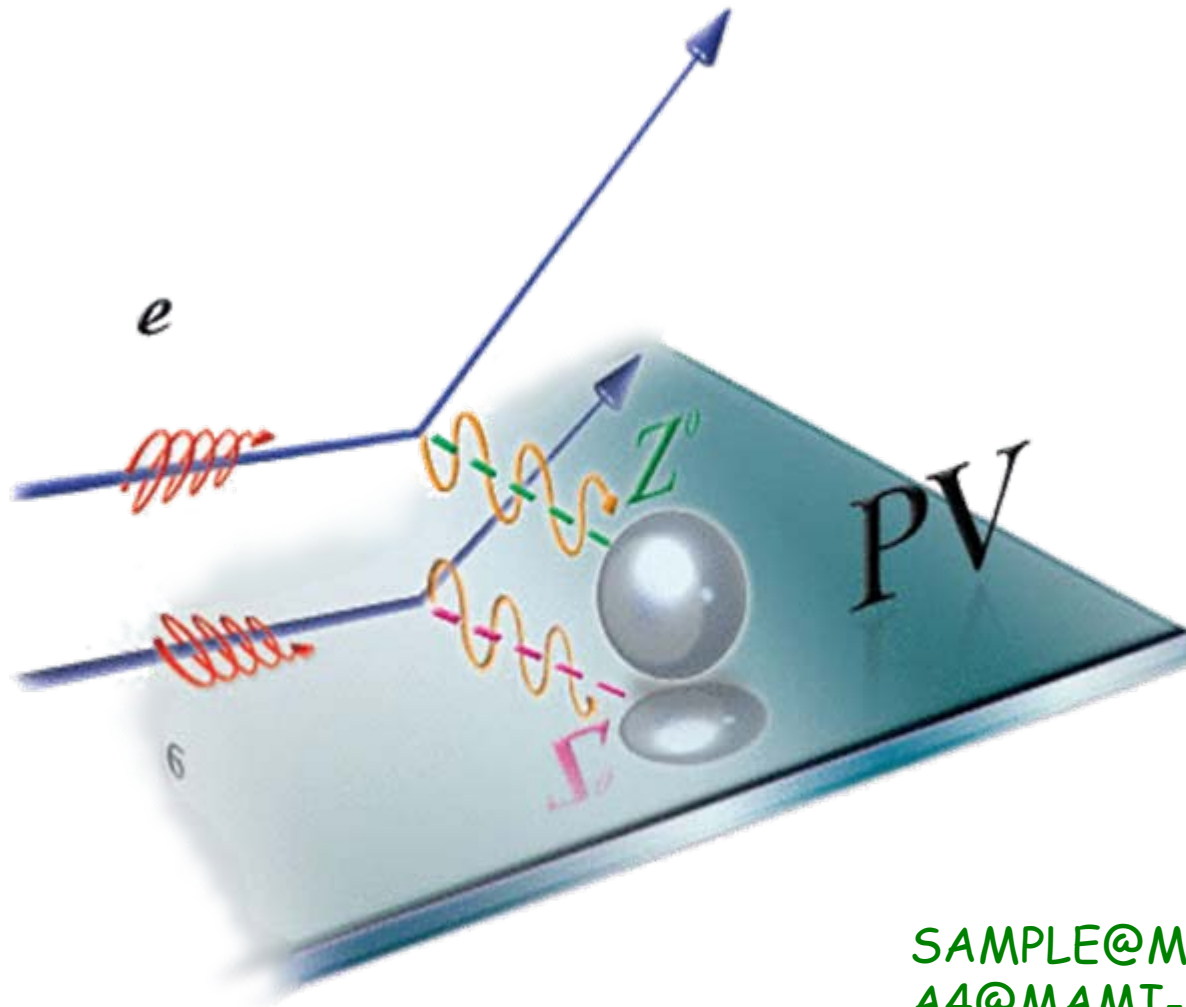


Parity conserving

$$G^\gamma(Q^2)$$

Parity violating

$$G^Z(Q^2)$$



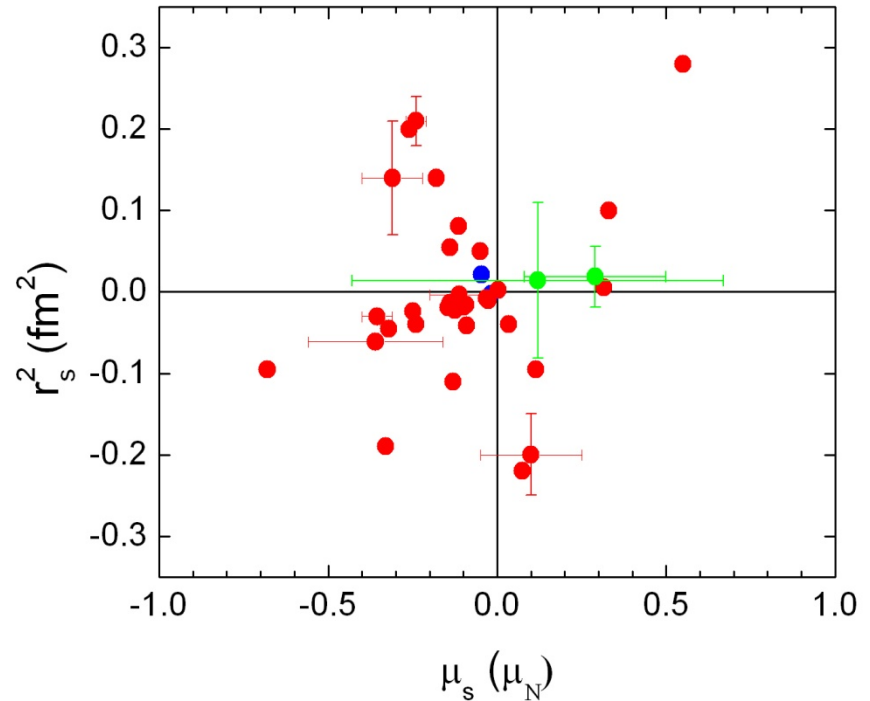
SAMPLE@MIT-BATES  
A4@MAMI-Mainz  
HAPPEX@JLab  
GO@JLab

# Strange Proton

- Strange radius and magnetic moment of the proton
- Theory
- Lattice QCD
- Global analysis PVES
- Unquenched QM

$$\mu_s = 0.0018 (\mu_N)$$
$$\langle r^2 \rangle_s = 0.012 (\text{fm}^2)$$

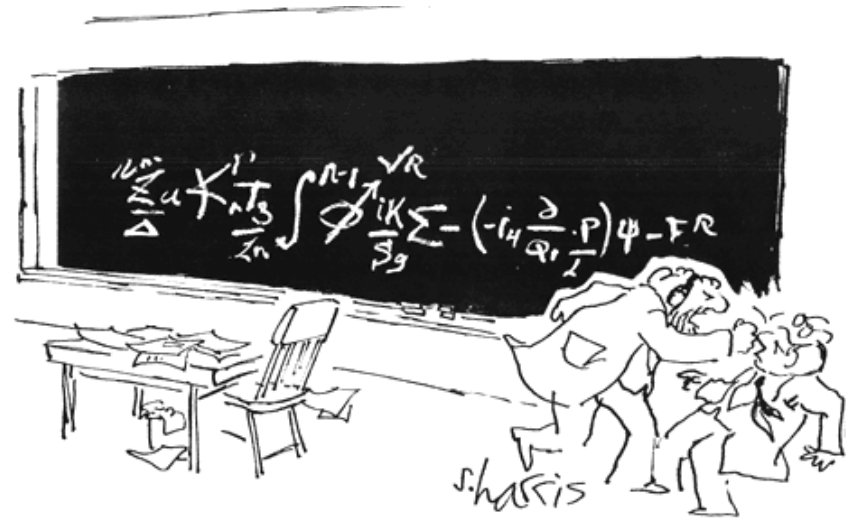
Ferretti, Ph.D. Thesis, 2011  
Bijker, Ferretti & Santopinto,  
PRC 85, 035204 (2012)



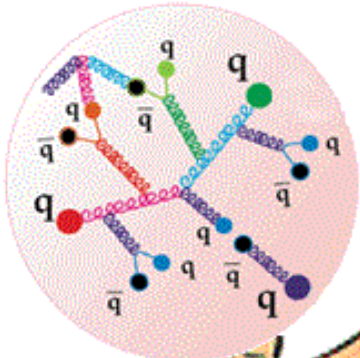


# Theory

- Lattice QCD
- Chiral perturbation theory
- Dispersion relations
- Chiral quark-soliton model
- Kaon loops
- Quark models
- Chiral bag models
- Skyrme model
- Vector Meson Dominance
- Unquenched quark model
- ...



*"You want proof? I'll give you proof!"*



# Summary and Conclusions

- First explicit calculations of flavor content of physical observables in an unquenched quark model
- Preserves the successes of the CQM
- **Magnetic moments of octet baryons**
- **Flavor asymmetry of sea quarks**
- **Quark spins and orbital angular momenta**
- **Strange loops of the proton**
- **Correspondence with MCM and Chiral QM**
- First results are very promising, and indicate that the unquenched quark model may provide an important improvement of the CQM and enhance its range of applicability



# Outlook

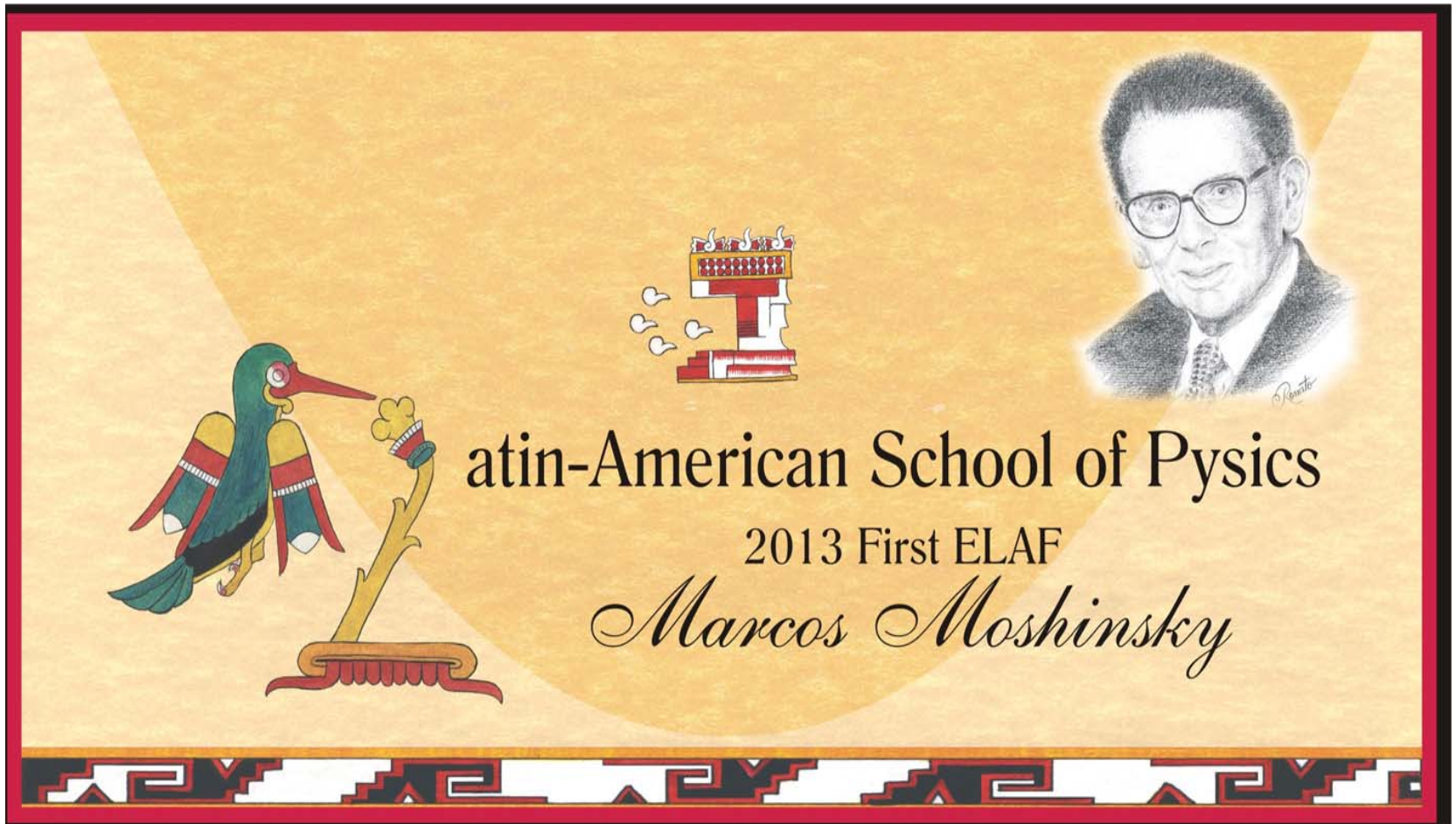
- Colaboración con la Dra. Elena Santopinto de la Universidad de Genova (Italia)
- Electromagnetic couplings (Hugo García Tecocoatzi)
- Relation with Chiral QM and MCM (Miguel Ángel López Ruiz, Silvia Díaz Gómez, Gustavo Hazel Guerrero Navarro, Emmanuel Ortiz Pacheco)
- Self energies (Giuseppe Galata, Jacopo Ferretti)
- Tetraquarks (Giuseppe Galata)
- Axial couplings
- Strong couplings
- ...



# Lecture Notes

- **Nuclear Supersymmetry**  
"VI Escuela Mexicana de Física Nuclear"  
AIP Conf Proc 1271, 90-131 (2010)
- **Quark Models of the Nucleon**  
"VII Escuela Mexicana de Física Nuclear"  
unpublished
- VIII Escuela Mexicana de Física Nuclear  
Verano de 2013, UNAM, México DF



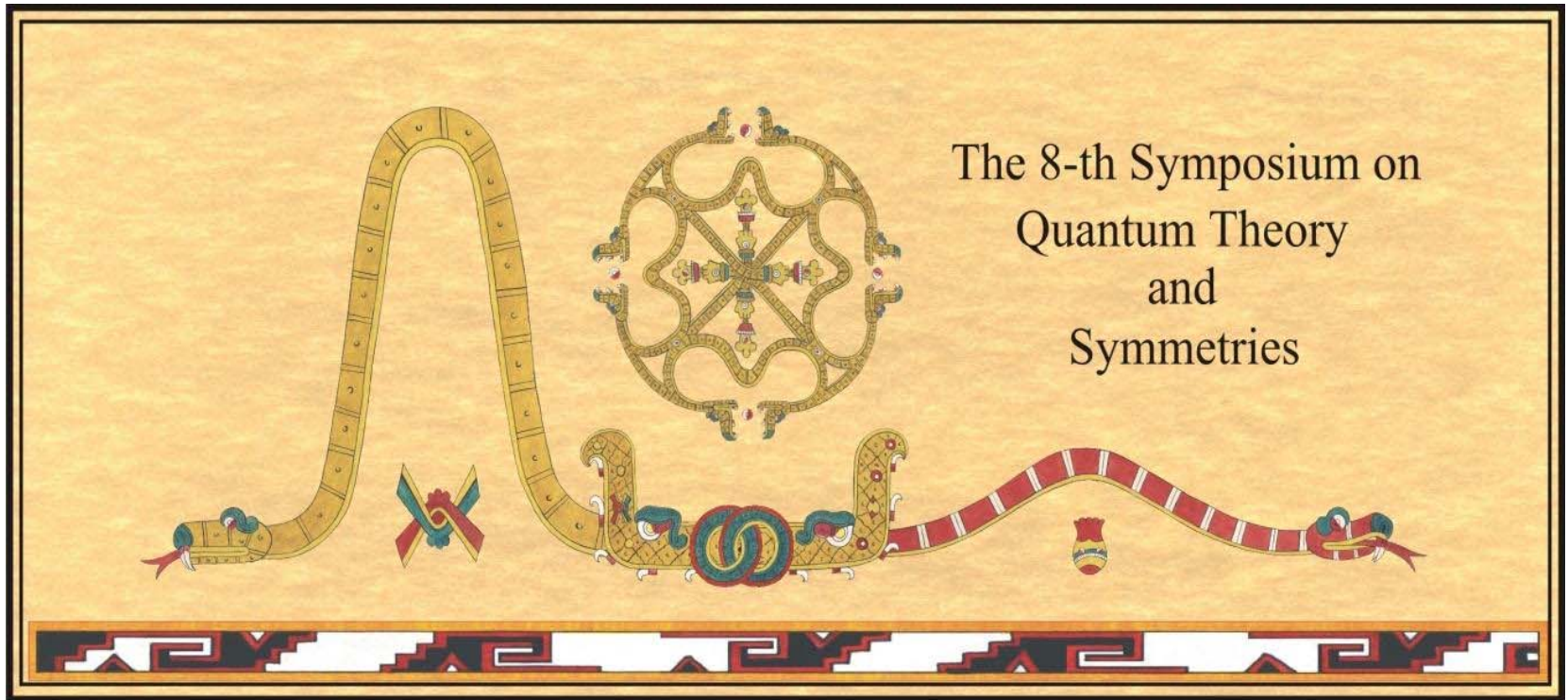


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2013 First ELAF

*Marcos Moshinsky*

México DF, 22 de julio - 2 de agosto de 2013  
<http://www.nucleares.unam.mx/~bijker/elaf2013.html>



México DF, 5 - 9 de agosto de 2013  
<http://www.fis.unam.mx/symposiaqts>