

Nuclear Structure in the fpg Shell

N.H. Medina

Instituto de Física, Universidade de São Paulo, São Paulo, Brazil.

Andean School on “Nuclear Physics in the 21st Century”

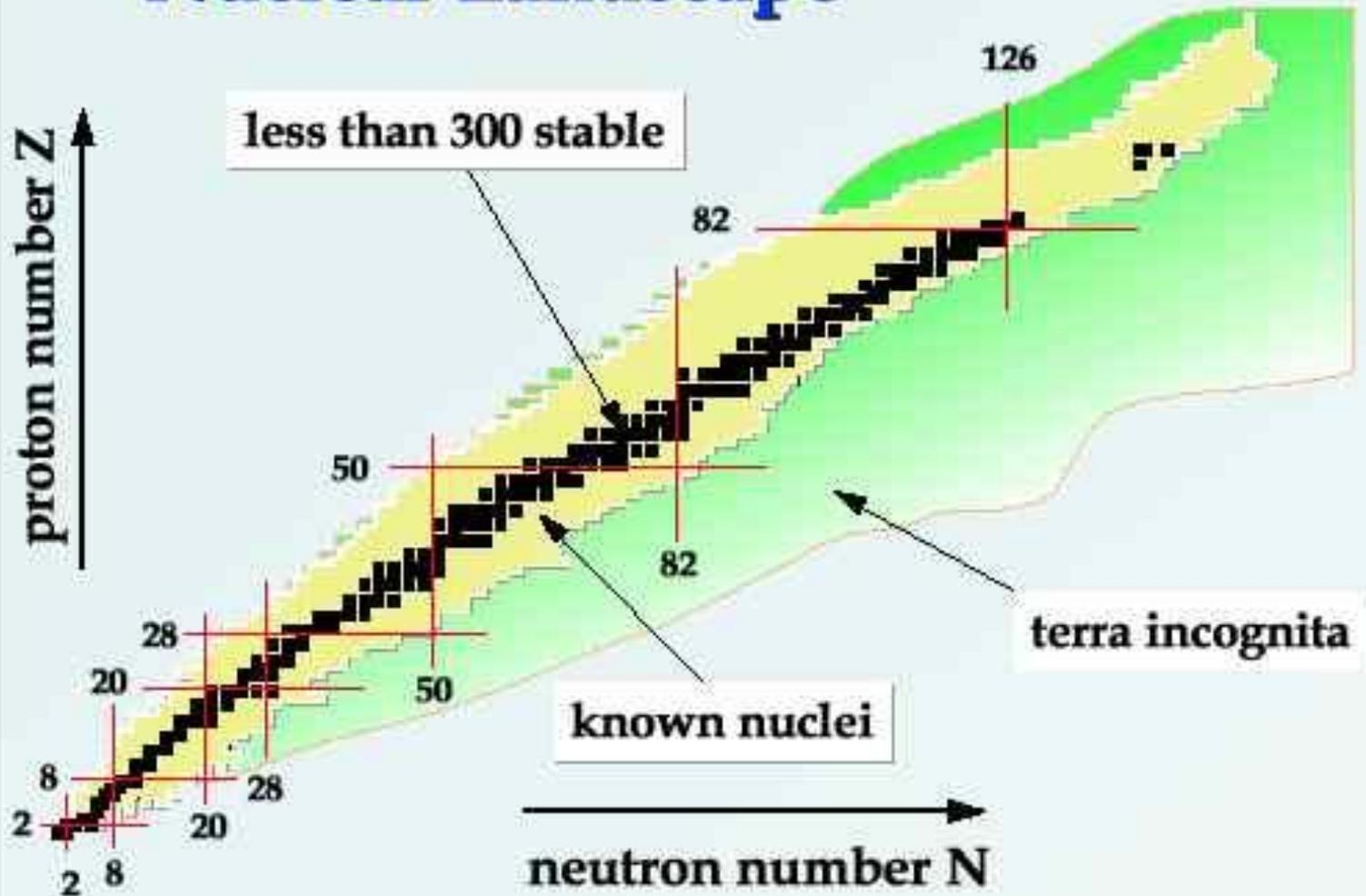


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November 26th 2012, Bogotá, Colombia

Nuclear Landscape



OUTLINE

In-beam γ -ray spectroscopy

High spin states

pf shell nuclei

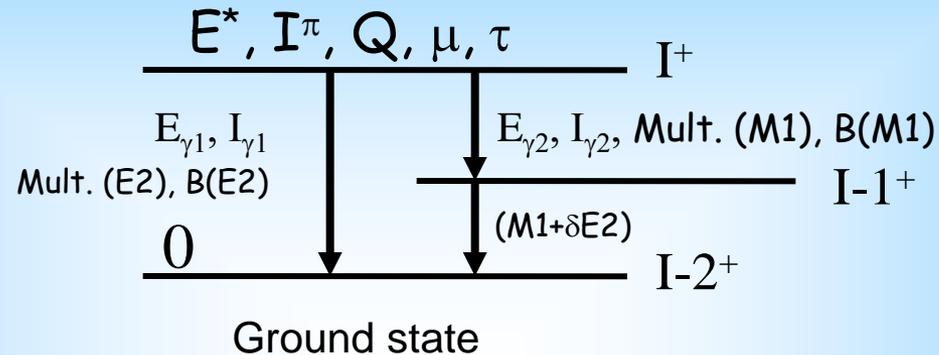


fpg shell nuclei



Conclusion

In-beam γ -ray spectroscopy



Excited state properties

$$E^*, I^\pi, Q, \mu, \tau$$

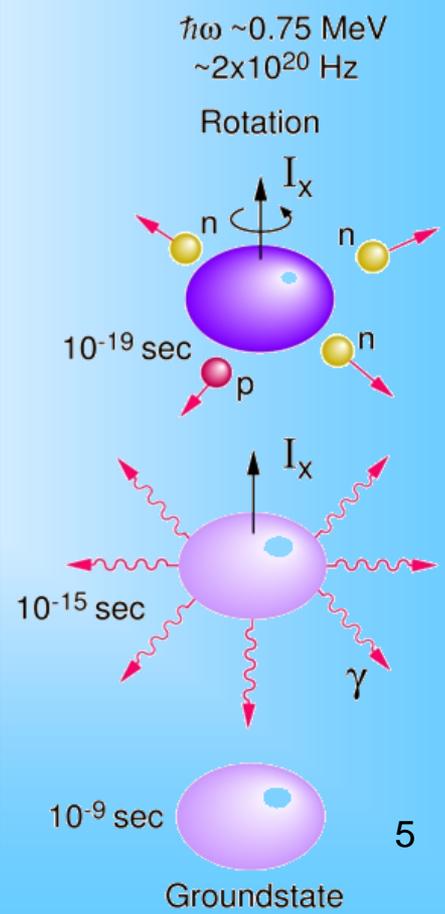
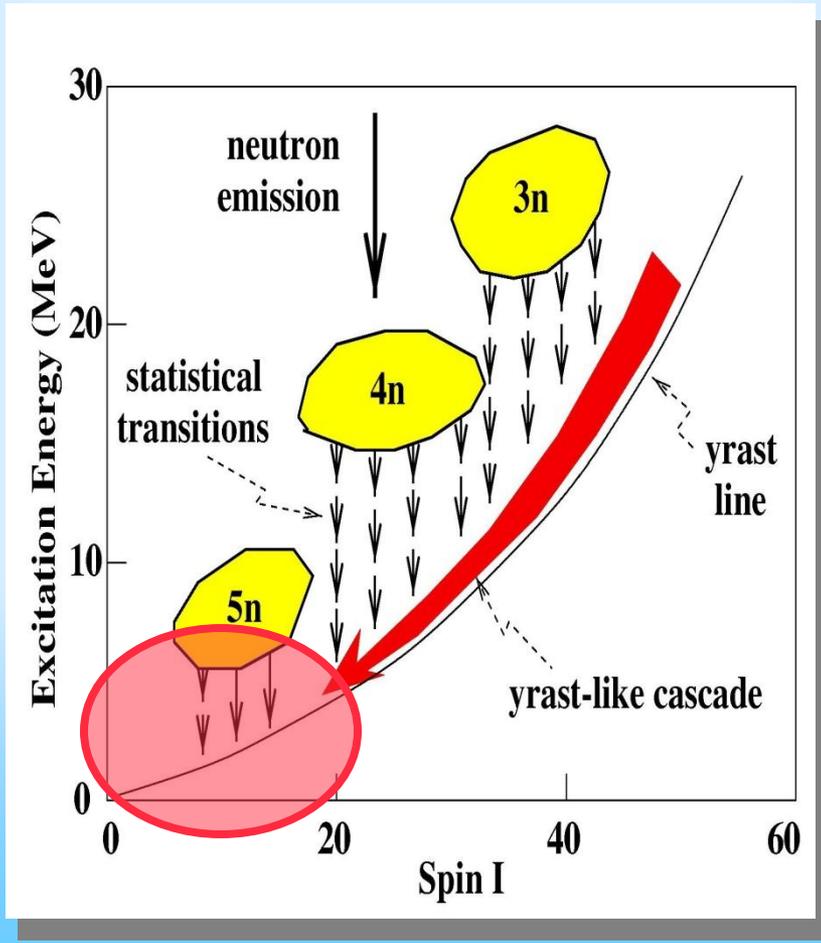
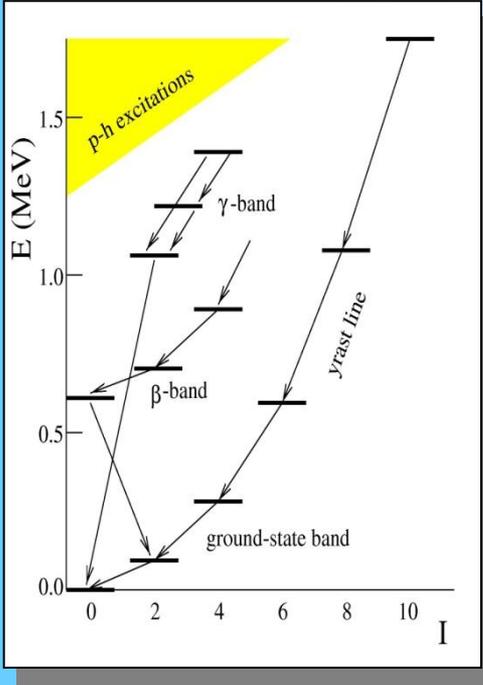
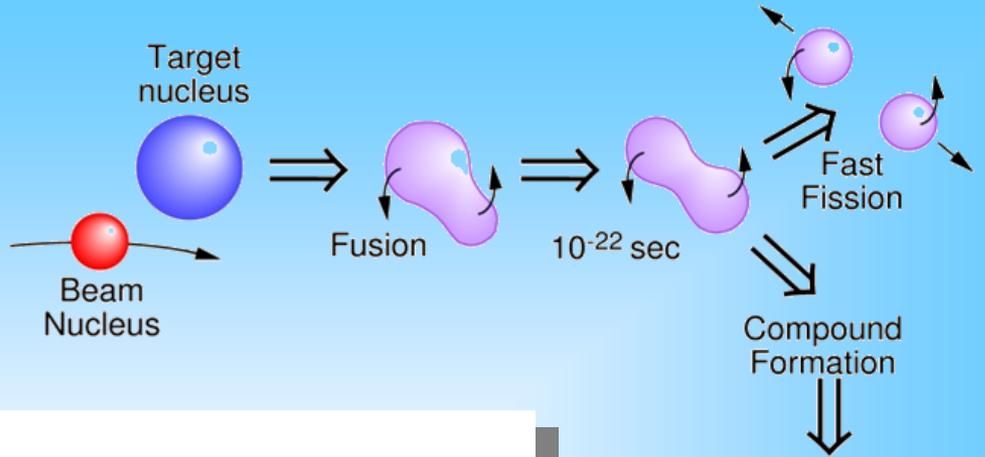
γ -ray transition properties

$$E_\gamma, I_\gamma, \text{multipolarity, mixing ratios } (\delta)$$

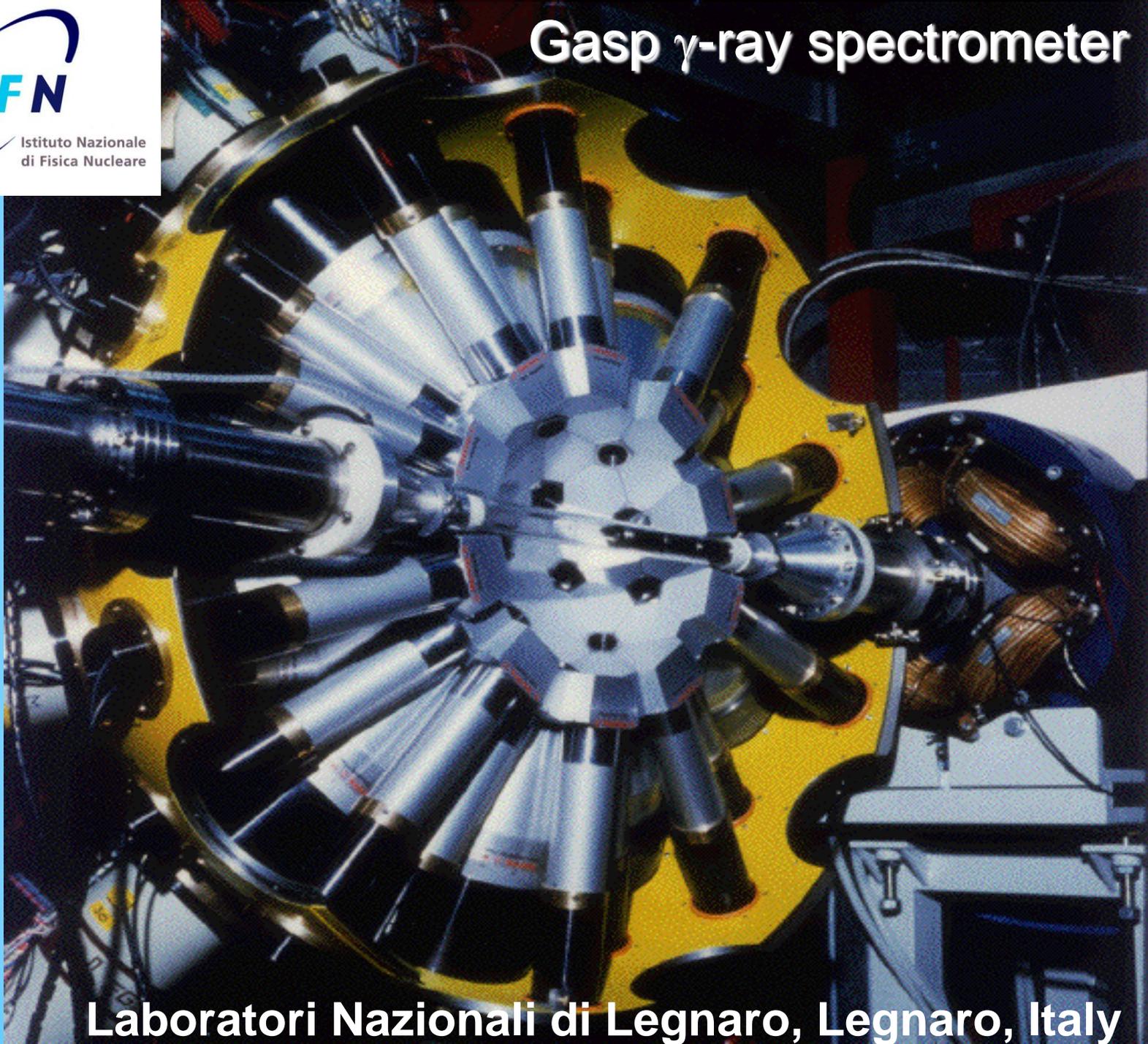
Construction of level schemes

Electromagnetic properties of the excited states

Fusion-evaporation reactions

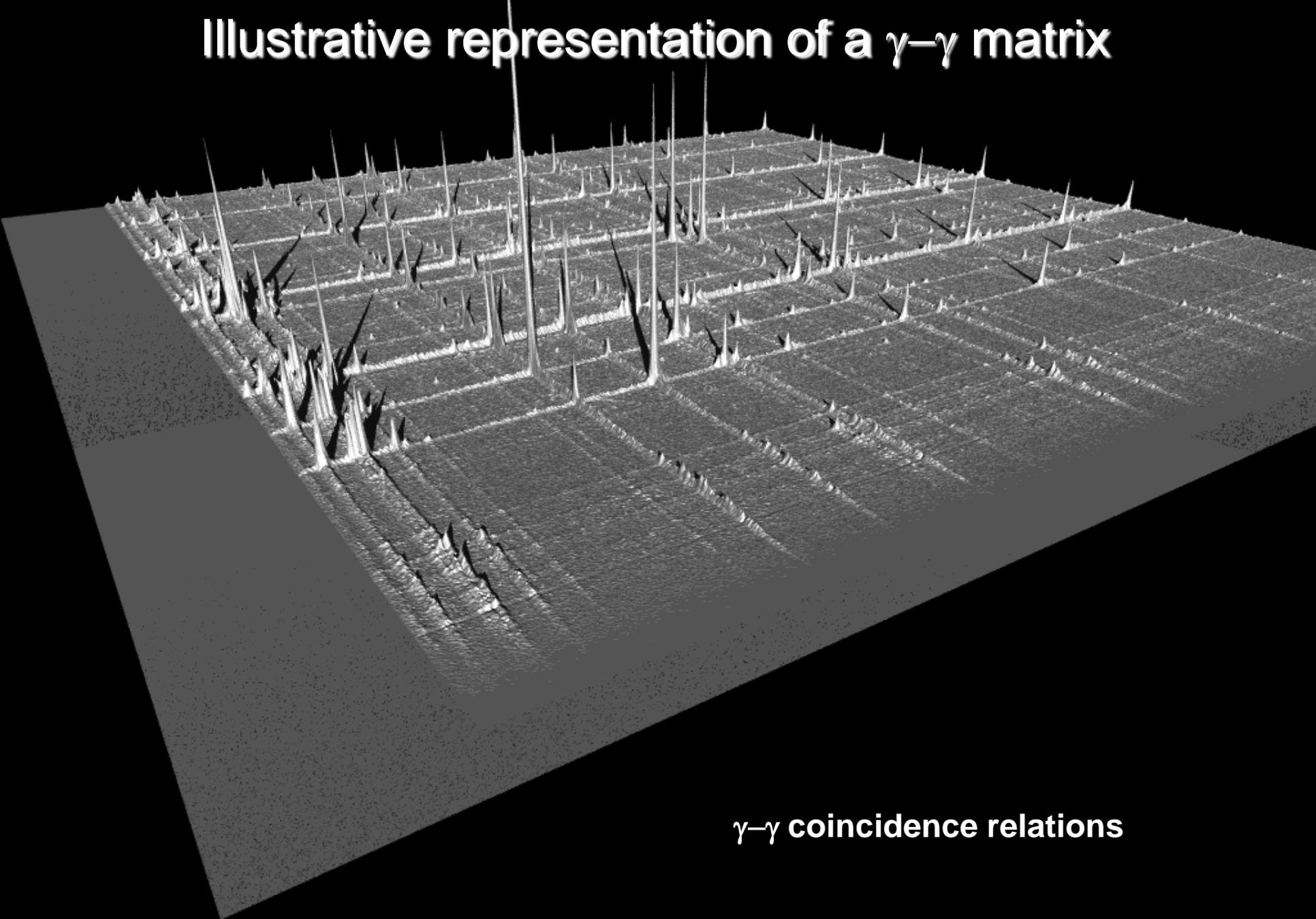


Gasp γ -ray spectrometer



Laboratori Nazionali di Legnaro, Legnaro, Italy

Illustrative representation of a γ - γ matrix

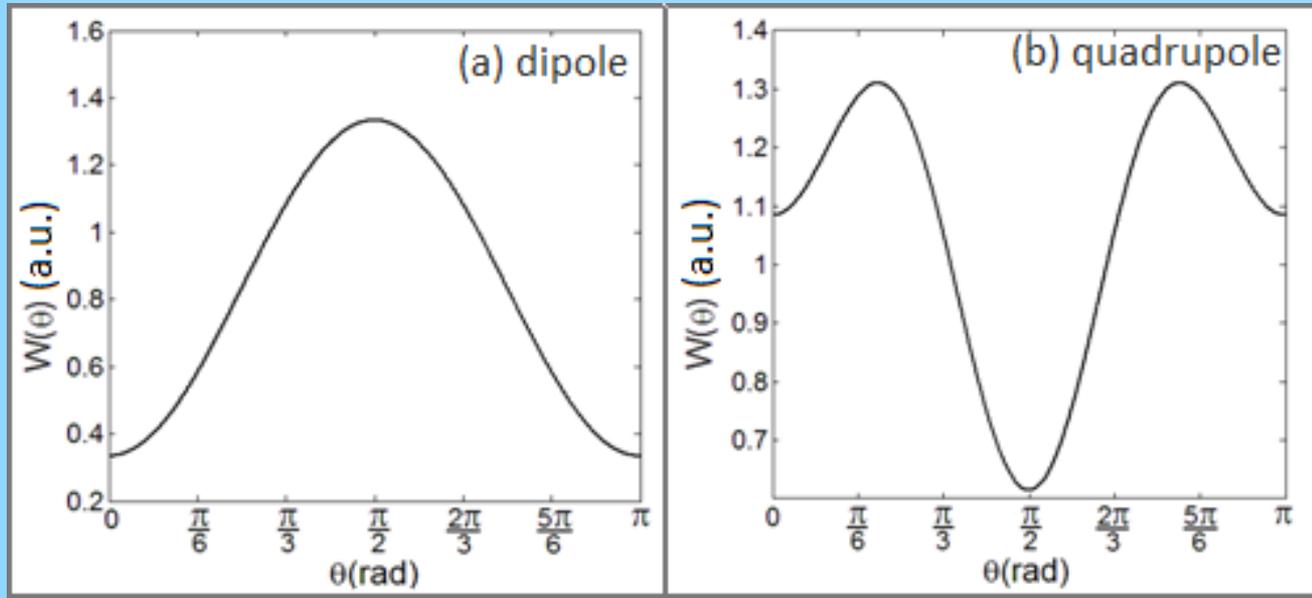


γ - γ coincidence relations

Symmetric γ - γ matrices or cubes allow level scheme construction

Excited State Angular Momentum

Assigned from γ -ray multiplicities



R_{ADO} : γ ray Angular Distribution from Oriented States

Excited states \rightarrow oriented in accordance with the beam direction

Transition between 2 levels

✚ Quadrupole $\rightarrow L=2$

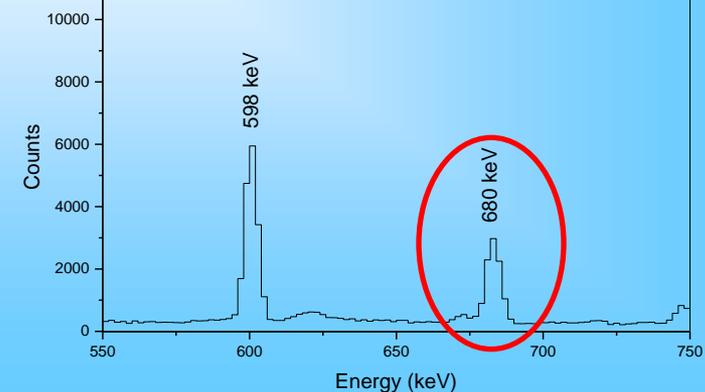
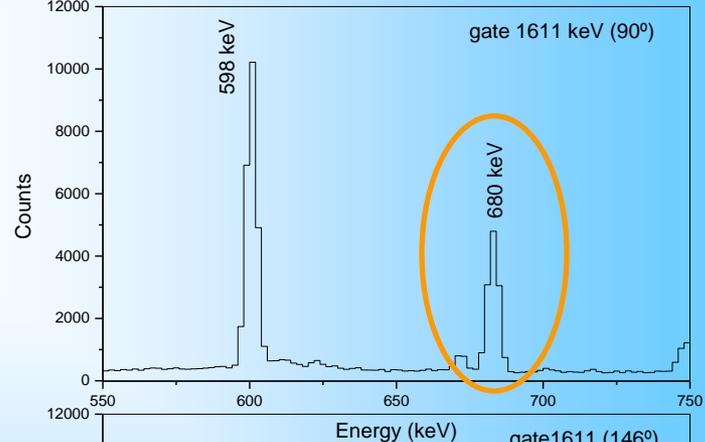
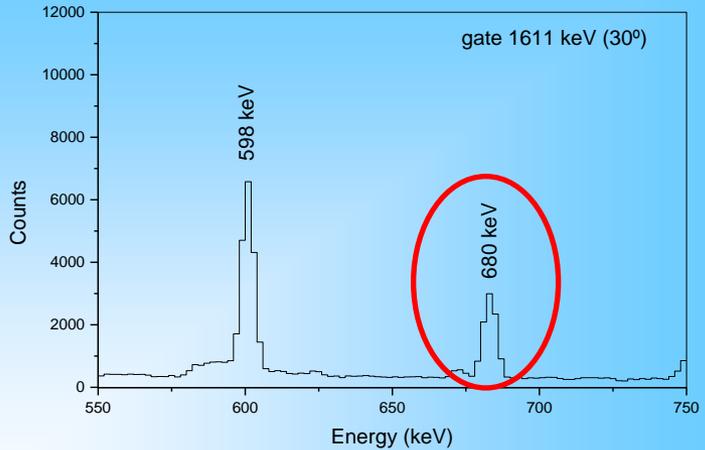
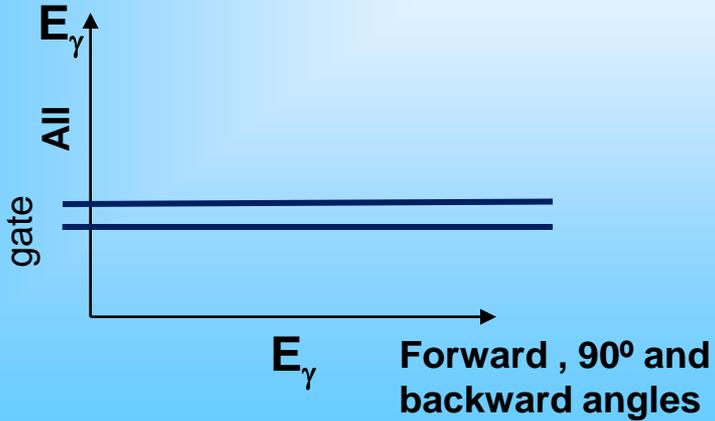
✚ Dipole $\rightarrow L=1$

✚ Mixed multiplicities: δ values.

R_{ADO} (angular distribution ratios), used to extract information about the γ transition multipolarities.

$$R_{ADO} = \frac{I_{\gamma}(34^{\circ}) \times I_{\gamma}(146^{\circ})}{2 \cdot I_{\gamma}(90^{\circ})}$$

Three asymmetric matrices having on the first axis the detectors in 34° , 90° and 146° and the second axis all the other detectors.



Doppler Shift Attenuation Method

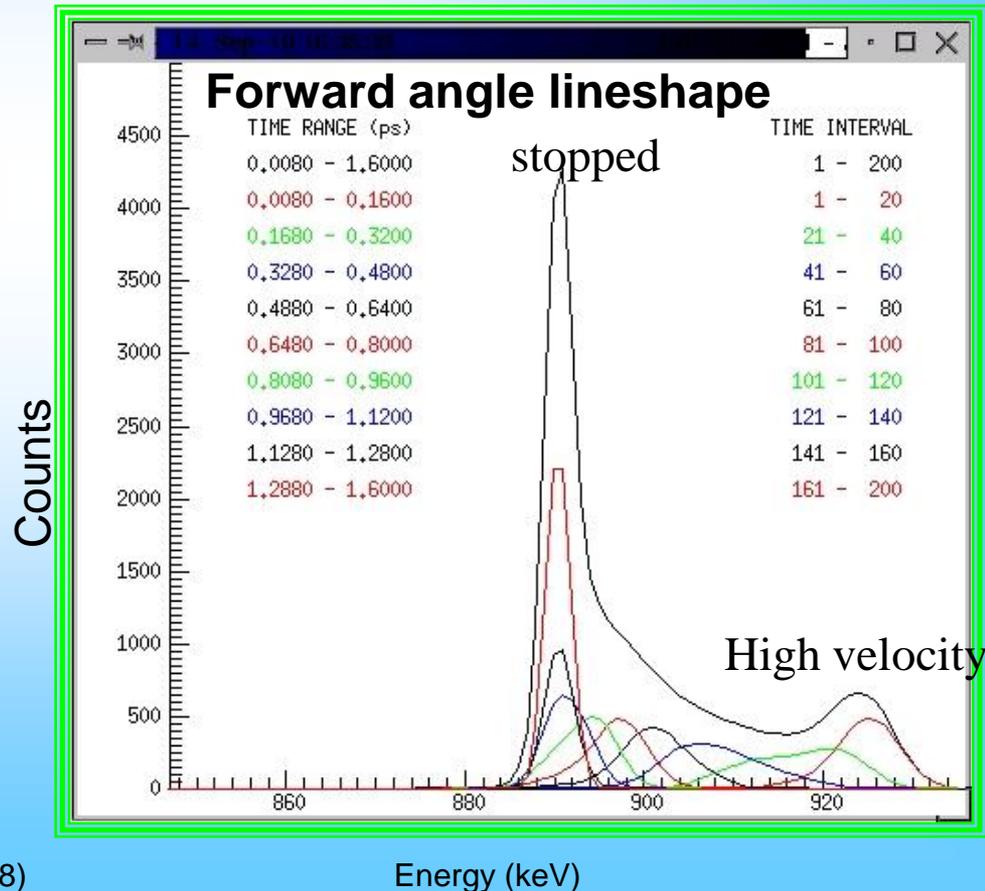
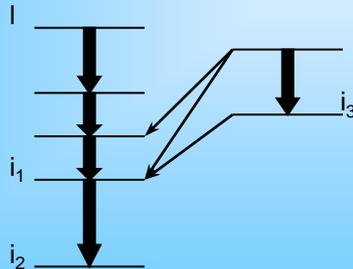
Lifetimes extracted from the lineshape fit of the gamma-rays emitted by nuclei stopping in a backing material (Au or Pb)

$$E_{\gamma} \approx E_0 (1 + (v/c) \cos\theta)$$

This method uses Monte Carlo Simulation of the trajectories of the recoiling nuclei in a target using Northcliffe & Schilling stopping power parameterization

L.C. Northcliffe & R.F. Schilling, Nucl. Data Tables A 7, 233 (1970).

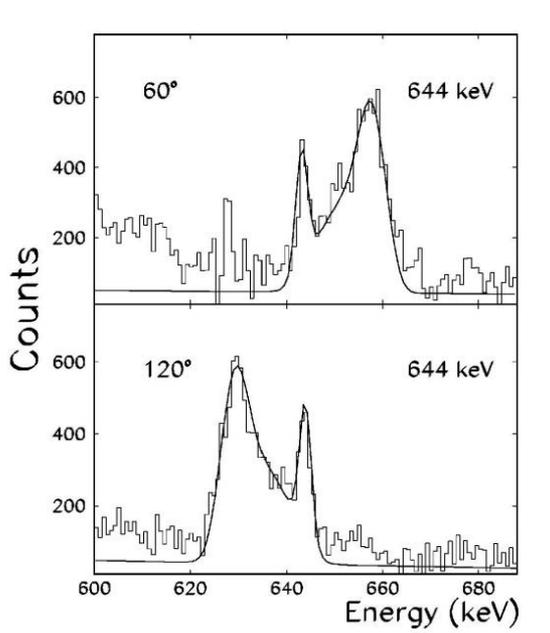
- Velocity components in the direction of the γ -ray detectors
- Free parameters: τ and sidefeeding time



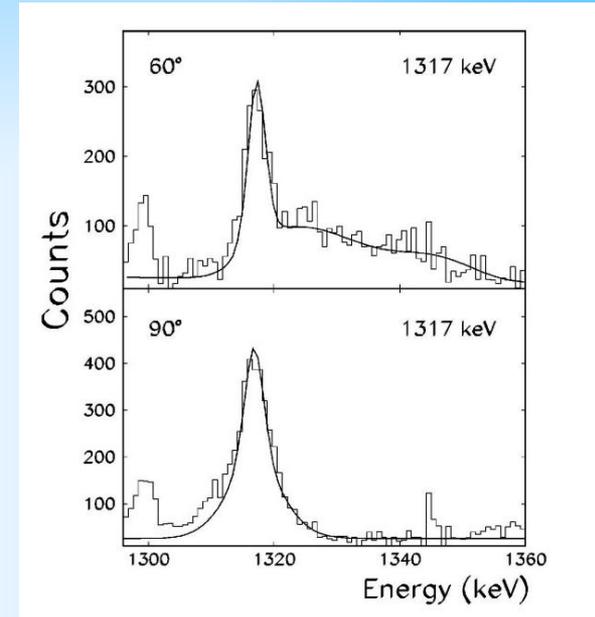
J.C. Wells & N.R. Johnson, Rep. ORNL 6689, 44 (1991)

F. Brandolini and R.V. Ribas, Nucl. Inst. Meth. A 417, 150 (1998)

Examples of γ -ray lineshape observed at 90 degrees, forward and backward angles.



Current and charge distribution are sensitive to the nuclear state wave function.



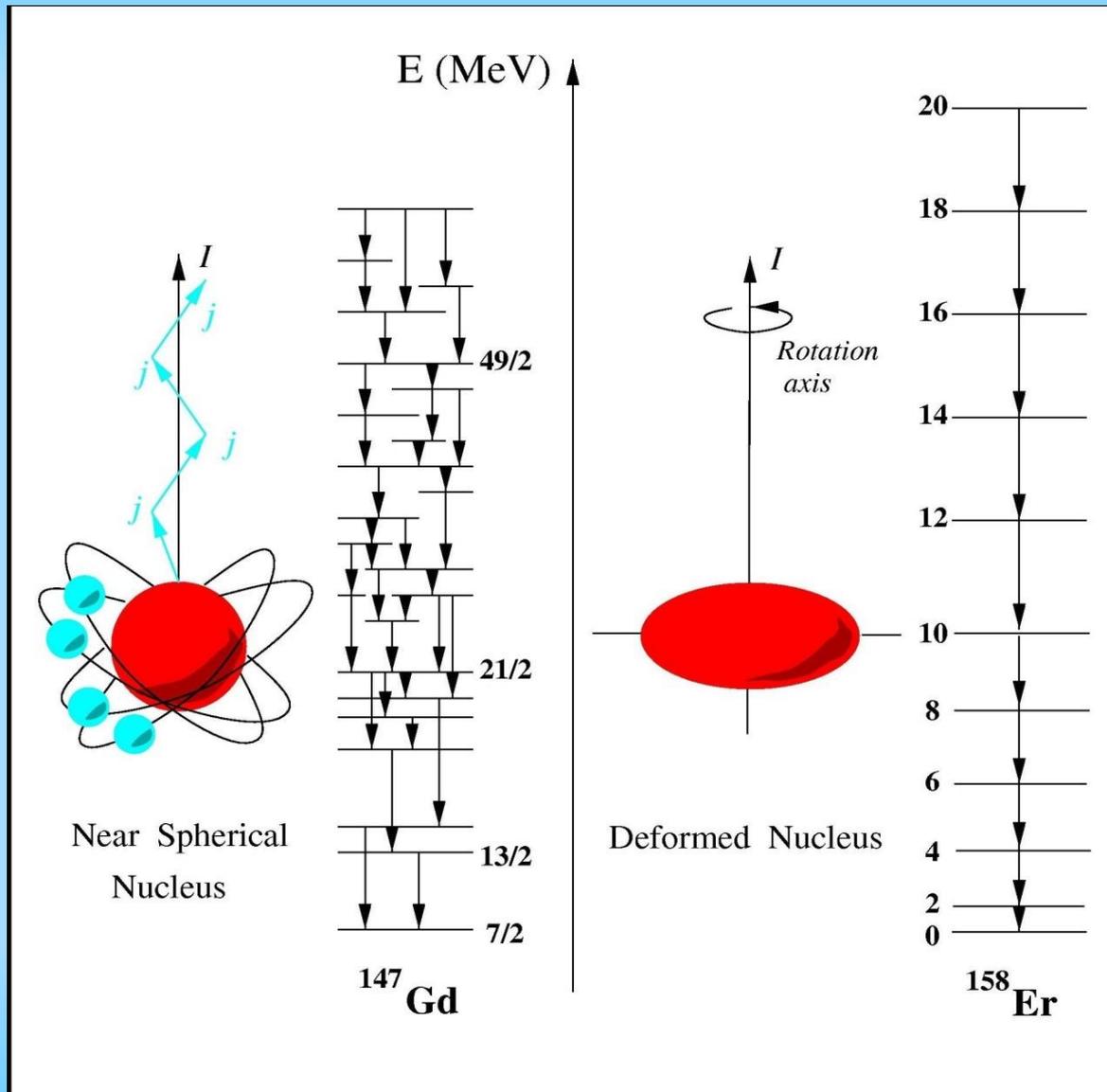
$$T_{fi}(\lambda L) = \frac{8\pi(L+1)}{\hbar L((2L+1)!!)^2} \left(\frac{E_\gamma}{\hbar c} \right)^{2L+1} B(\lambda L: I_i \rightarrow I_f)$$

$$B(E2) = \frac{815.6}{E_\gamma^5 \tau(1+\alpha)} B \quad e^2 fm^4 \quad ; \quad B(M1) = \frac{0.05697}{E_\gamma^3 \tau(1+\alpha)} B \quad \mu_N^2$$

$$B(E2) = \frac{5}{16\pi} Q_0^2 \langle I_i K 2 0 | I_f K \rangle^2$$

$$g = g_R + (g_K - g_R) \frac{K^2}{I(I+1)}$$

High spin states



The Rigid Rotor

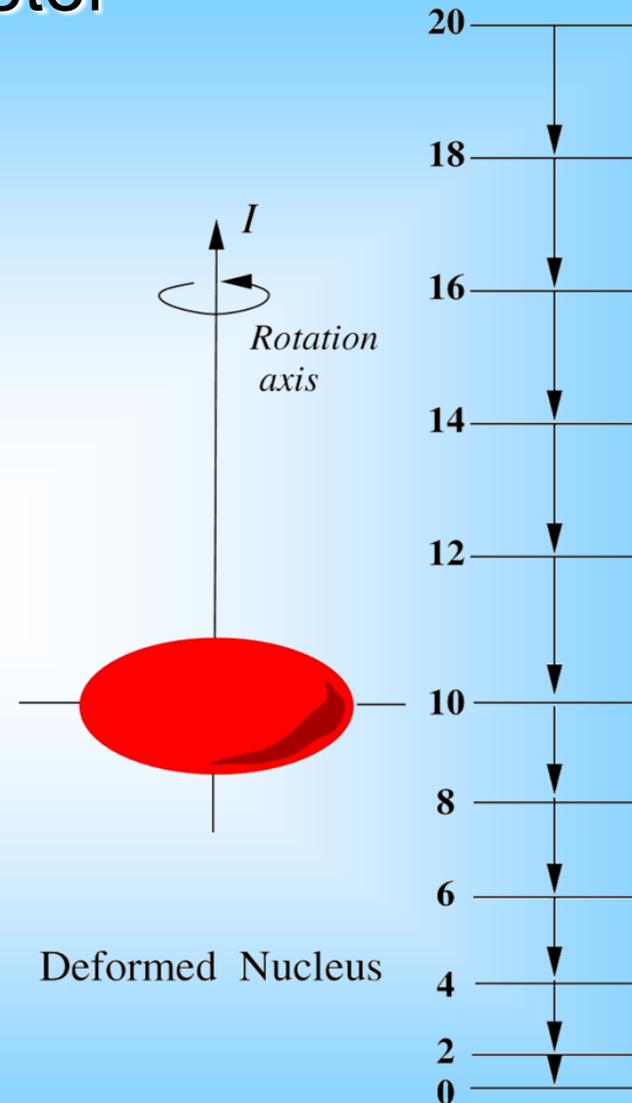
$$E = \frac{1}{2} \mathfrak{I} \omega^2 \quad ; \quad I = \mathfrak{I} \omega$$

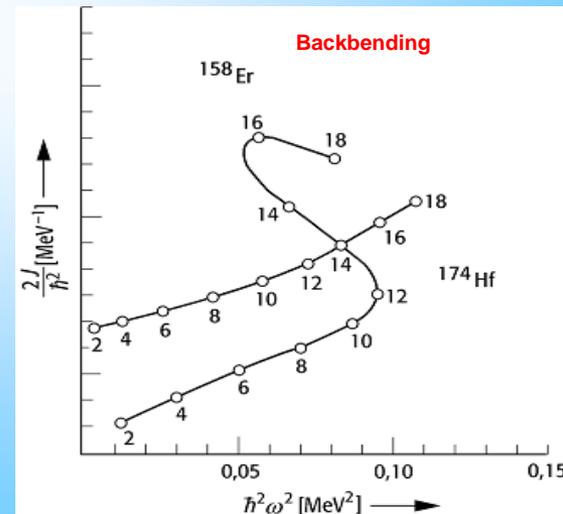
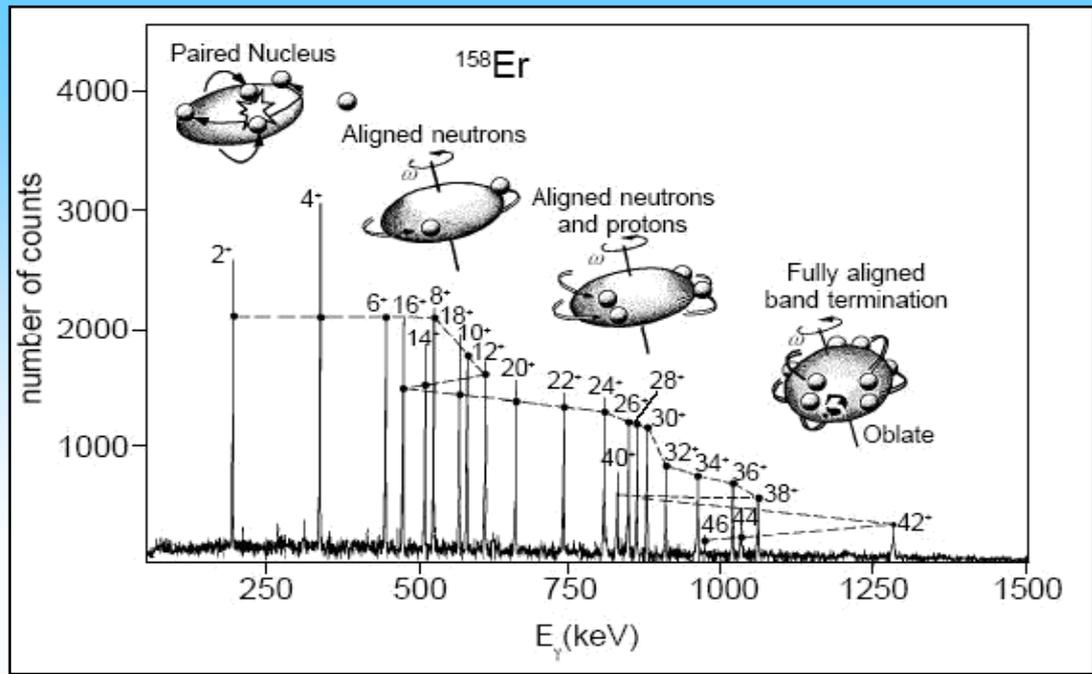
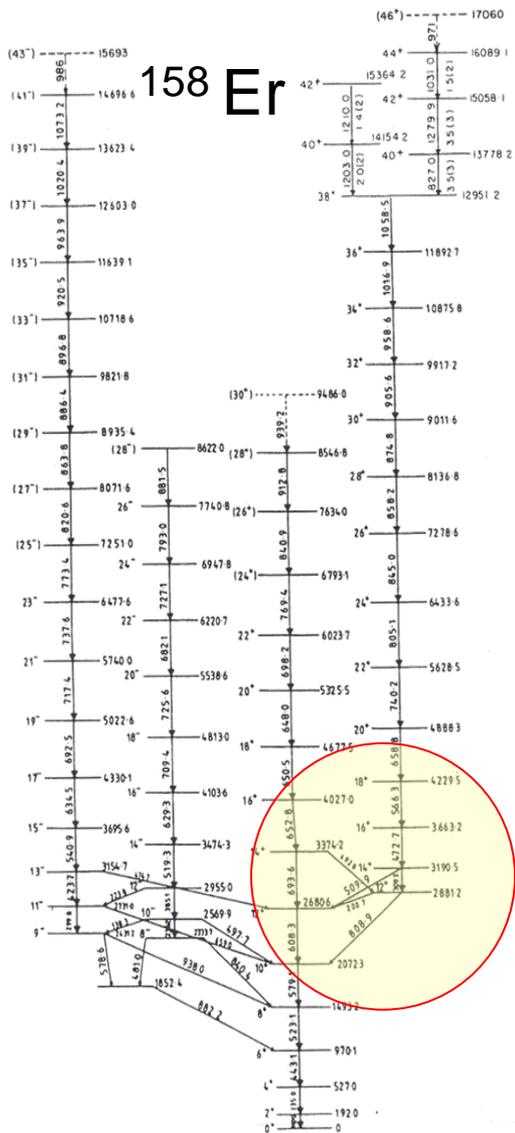
$$E = \frac{\hbar^2}{2\mathfrak{I}} I(I+1)$$

$$Q_s = Q_0 \frac{3K^2 - I(I+1)}{(I+1)(2I+3)}$$

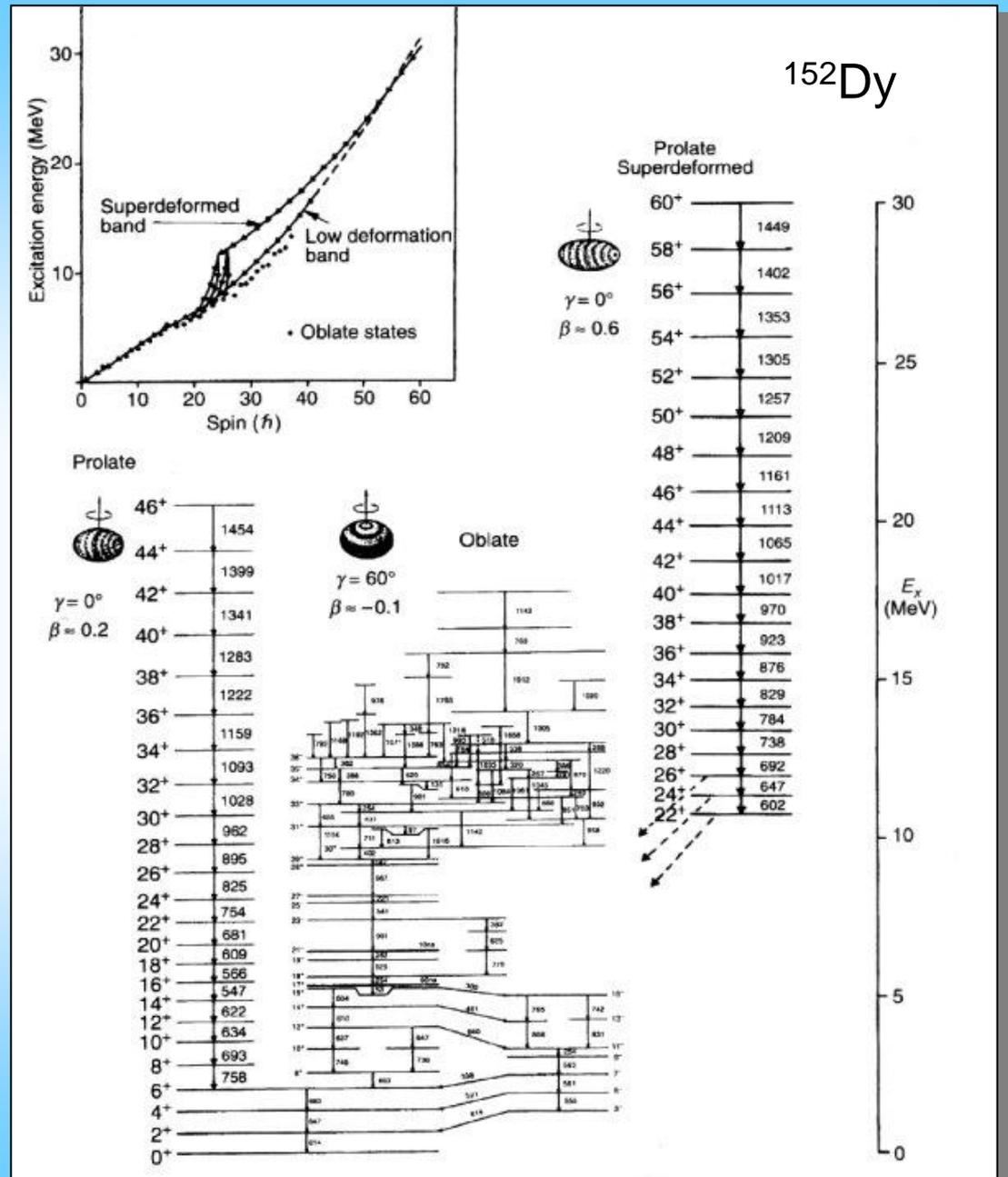
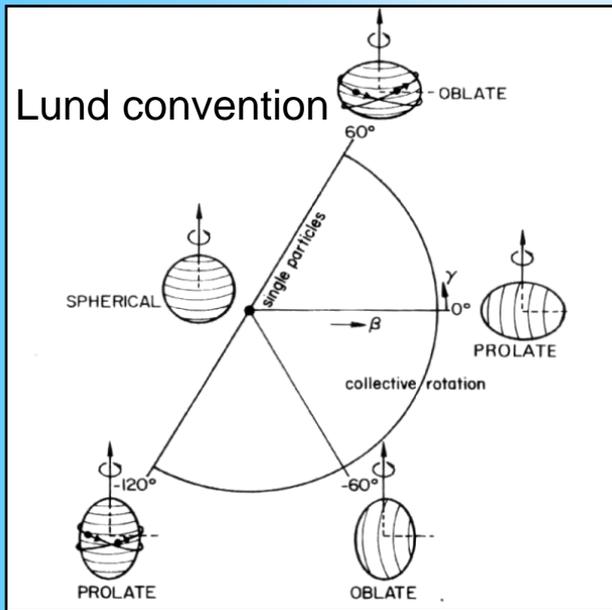
$$B(E2) = \frac{5}{16\pi} Q_0^2 \langle I_i K 20 | I_f K \rangle^2$$

$$g = g_R + (g_K - g_R) \frac{K^2}{I(I+1)}$$

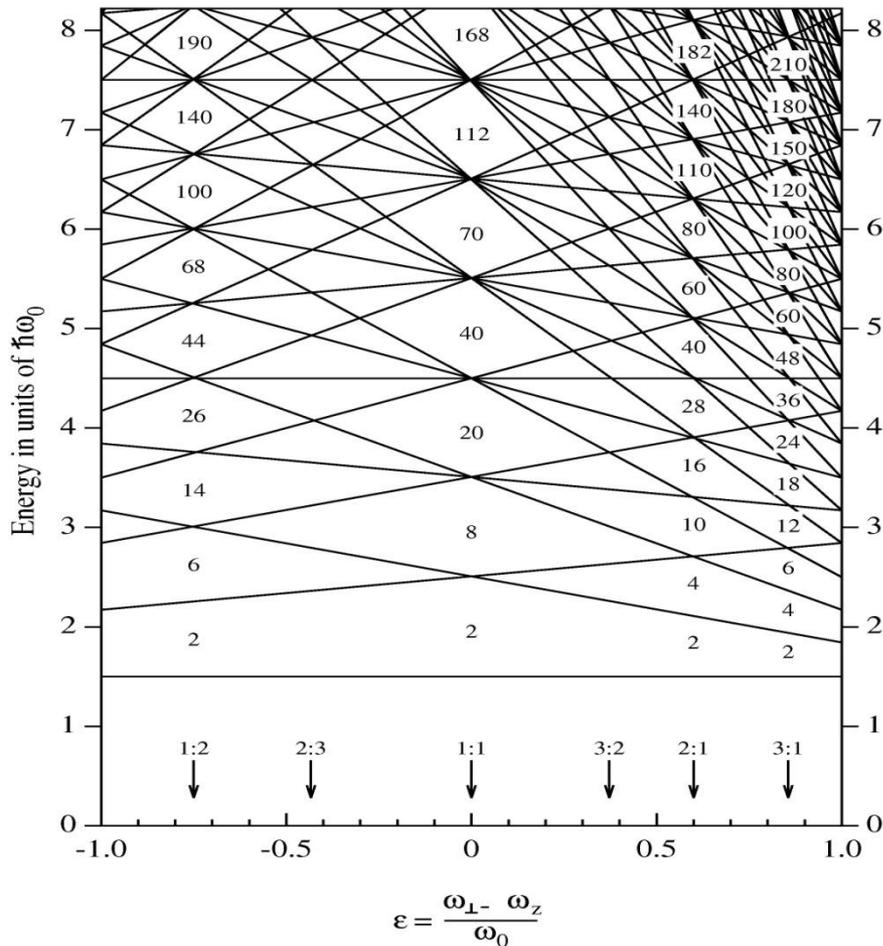




Shape Coexistence



Deformed Shell Gaps



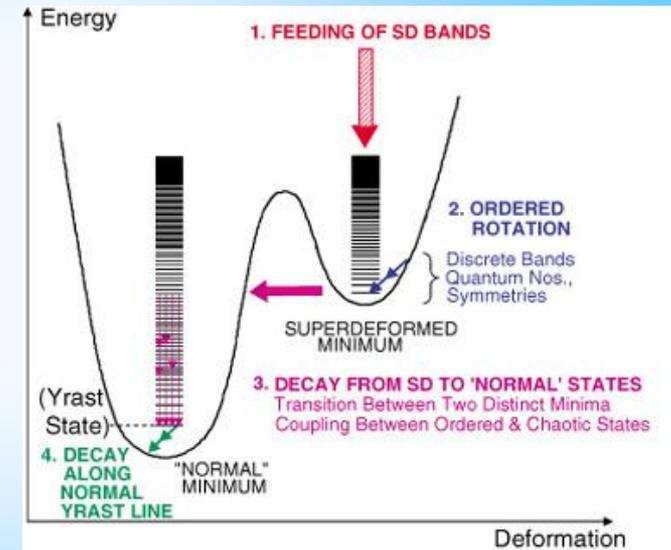
Single-particle level energies calculated for an axially symmetric harmonic oscillator

Second minima $\beta_2 \sim 0.75$

V.M. Strutinski, Nucl. Phys. A 95, 420 (1967)

Observed in the ^{152}Dy nucleus

P.J. Twin et al., Phys. Rev. Lett. 57, 811 (1986)



Third minima $\beta_2 \sim 0.9$

Predicted but not observed

Superdeformation

320 superdeformed bands

$A = 40, 80, 130, 150, 160$ and 190

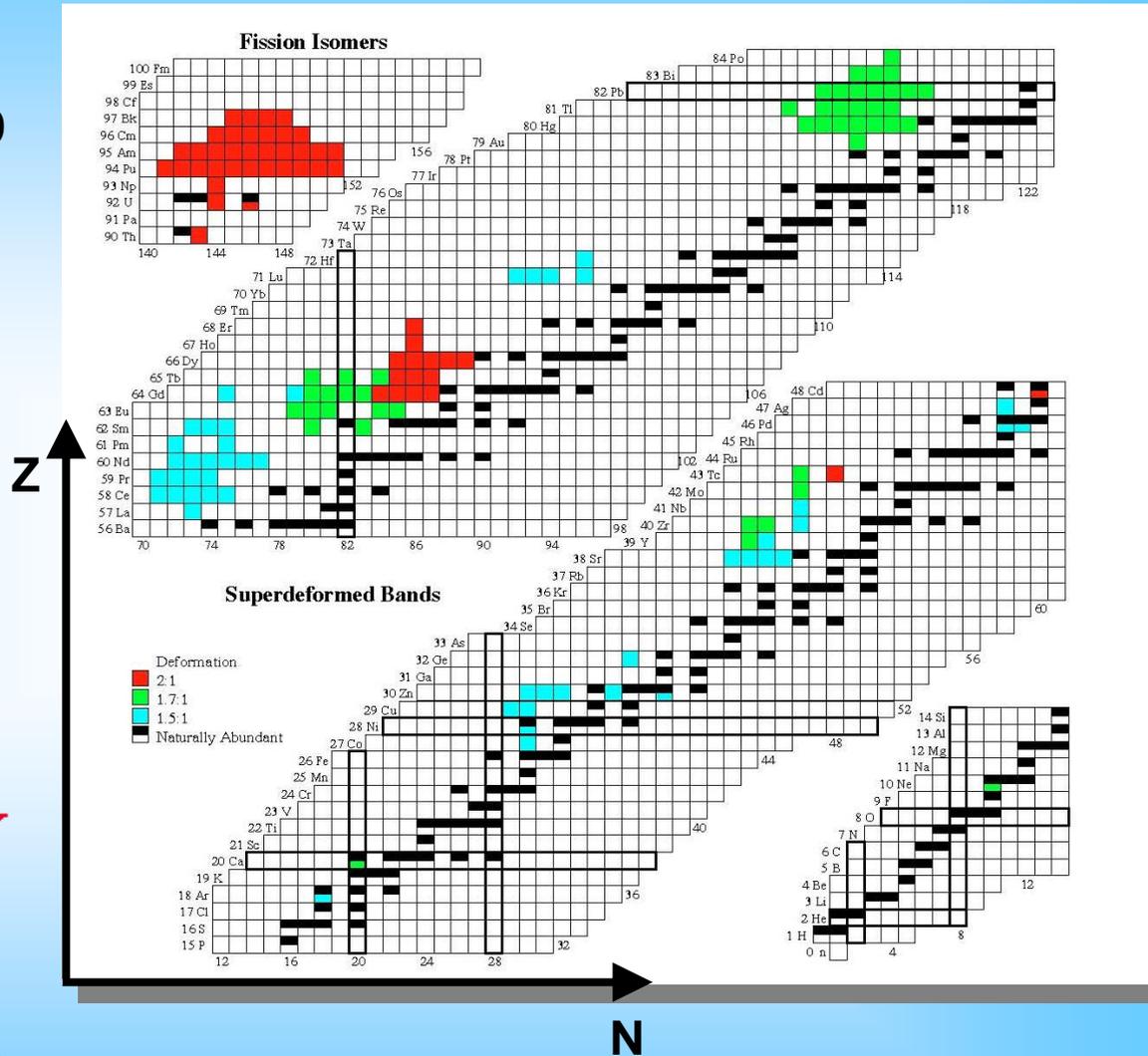
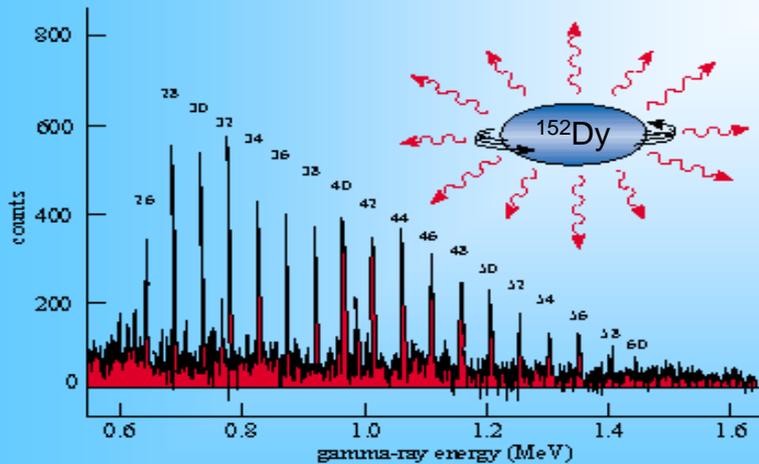
Feeding and Decay modes

Linking transitions:

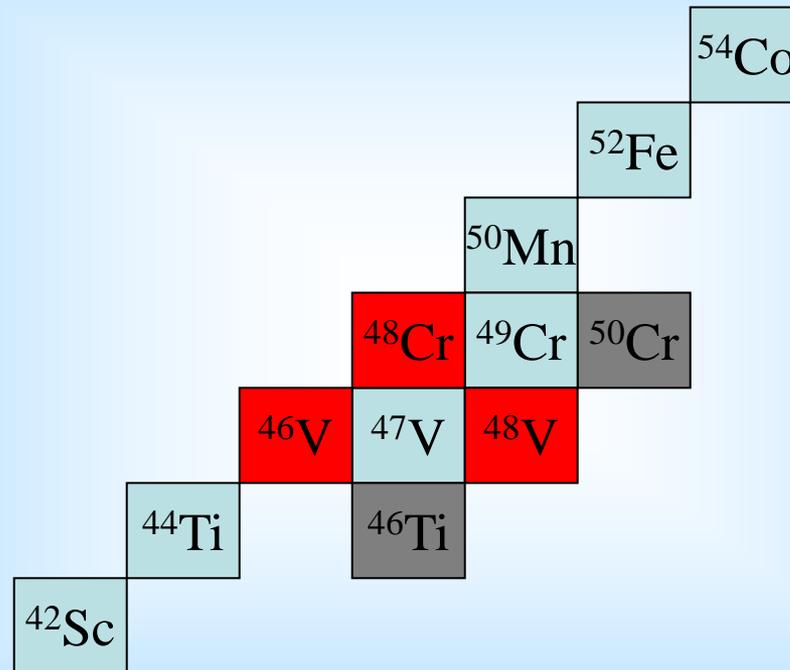
$^{133,135,137}\text{Nd}$, ^{194}Hg , ^{194}Pb

^{152}Dy : 6 SD bands

$$\Delta E_\gamma \approx \text{const.}$$

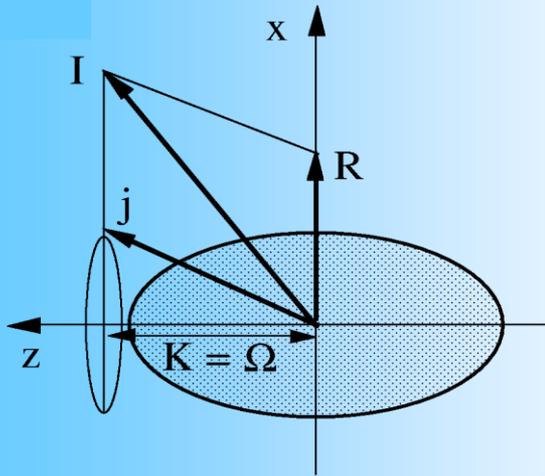


pf shell nuclei ($A=50$)

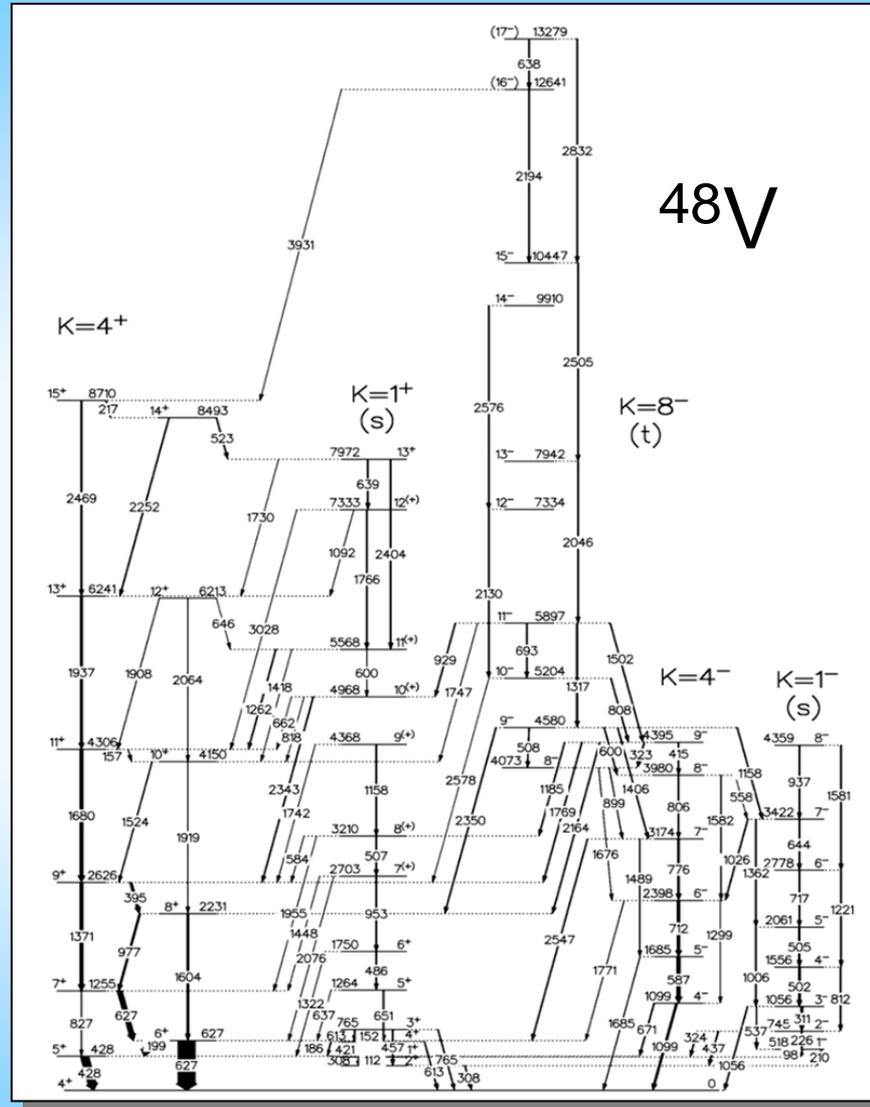


Nuclei with valence nucleons occupying the fp orbitals

The odd-odd ^{48}V nucleus



K is the angular momentum projection in the symmetry axis



Level scheme of the ^{48}V nucleus.

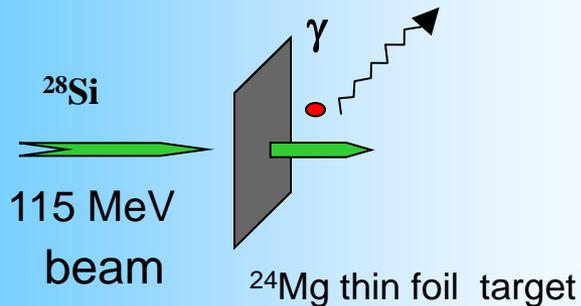
Experimental Details

Fusion-evaporation reactions:



Thin target experiment

Level scheme investigation.
self-supporting target.



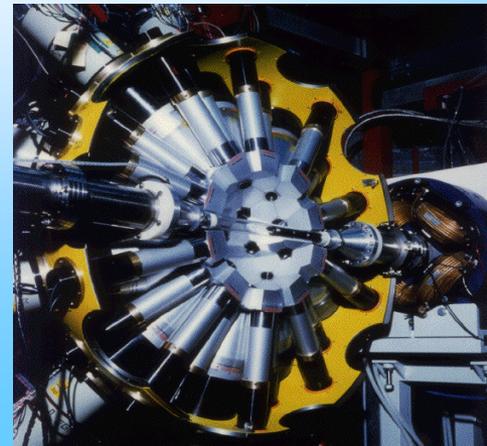
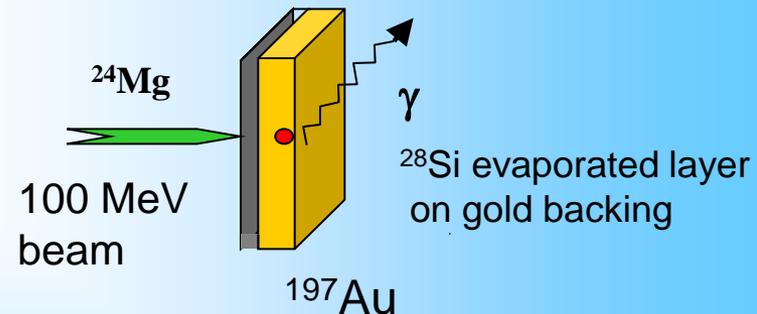
XTU Tandem accelerator
Legnaro National Laboratories, Italy (LNL)

GASP γ -ray spectrometer

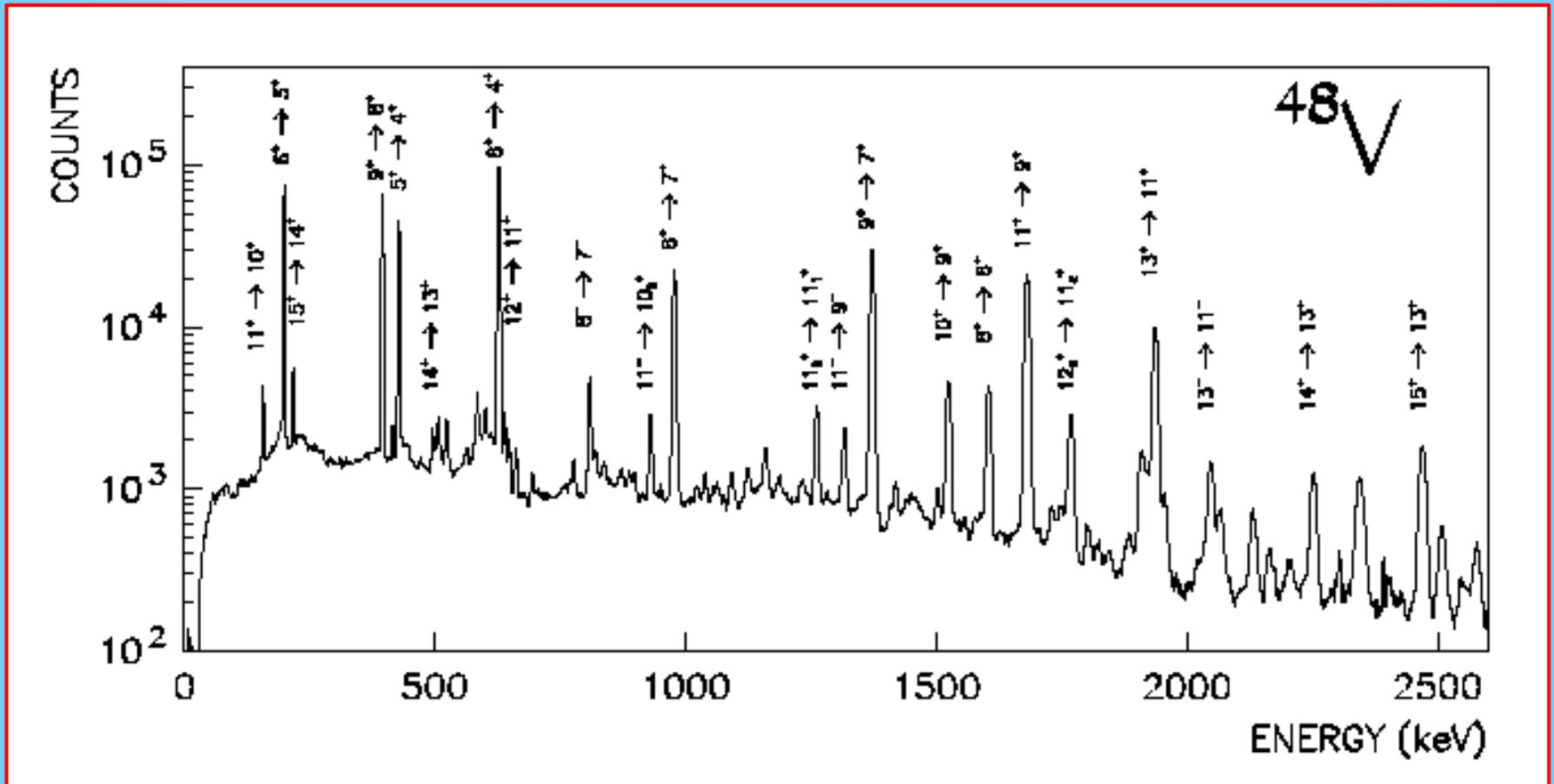


Thick target experiment

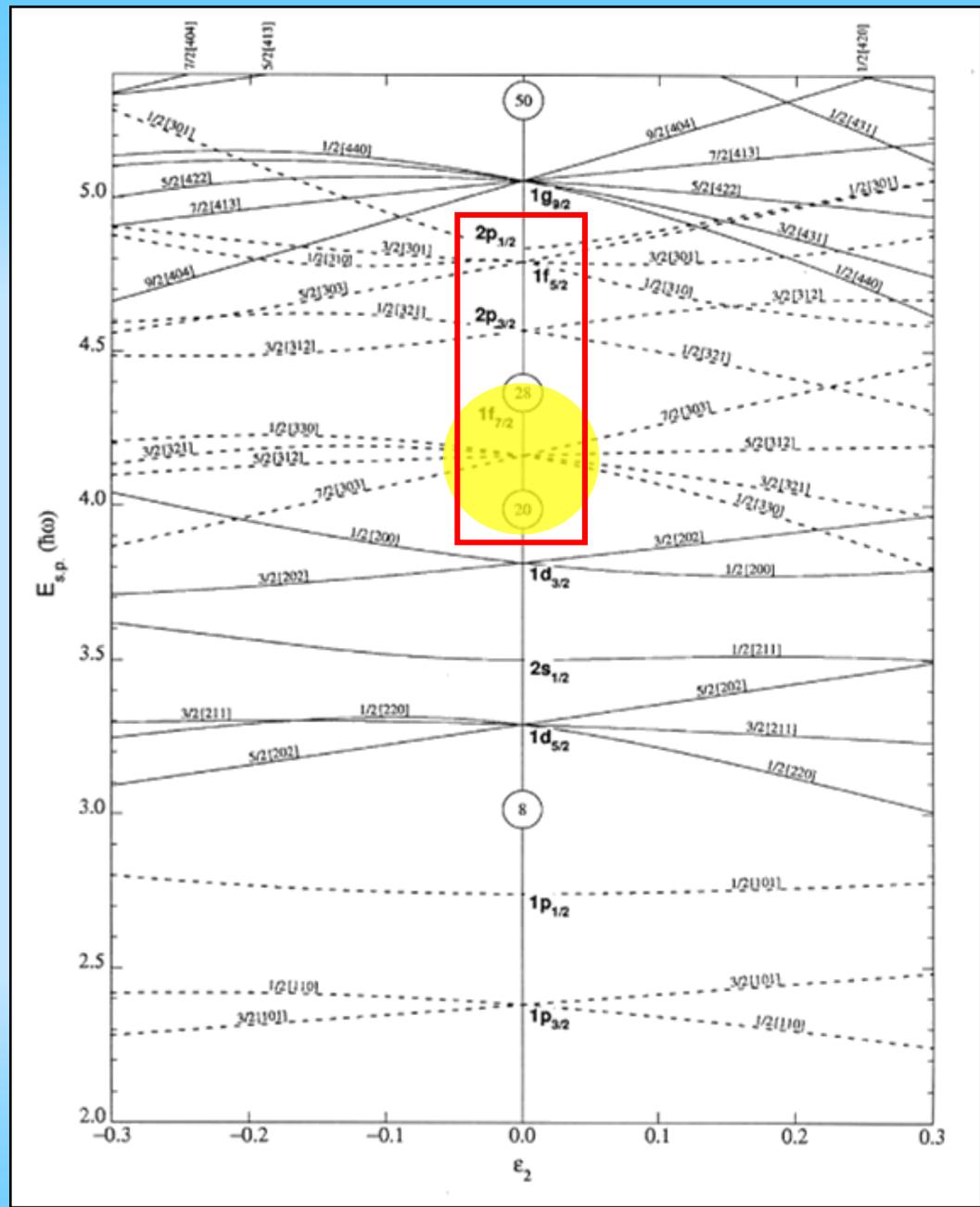
Lifetime measurements.
backed targets



γ -ray spectrum

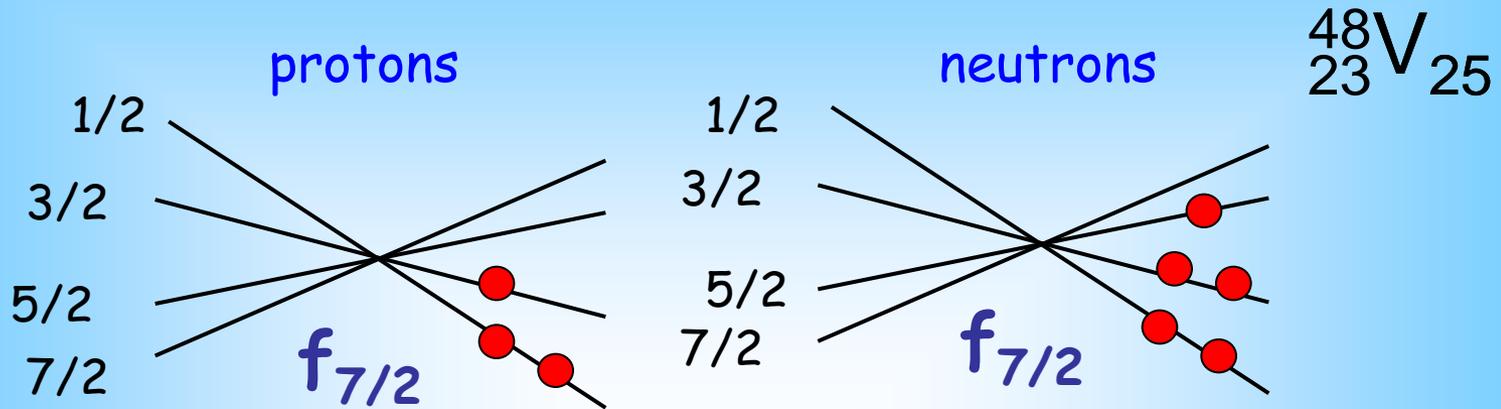


Gamma-ray spectrum from the ^{24}Mg on ^{28}Si fusion reaction ($E = 100$ MeV) gated on some low-lying transition of the ^{48}V gs band, and on 3 protons detected by the ISIS array

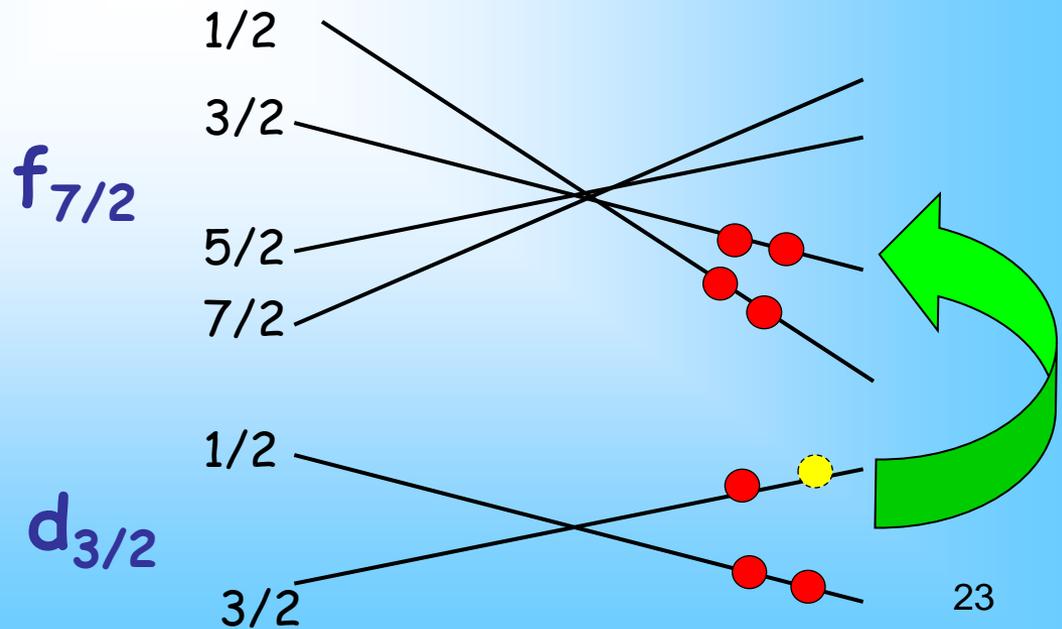


Nilsson diagram for protons and neutrons, Z or $N \leq 50$

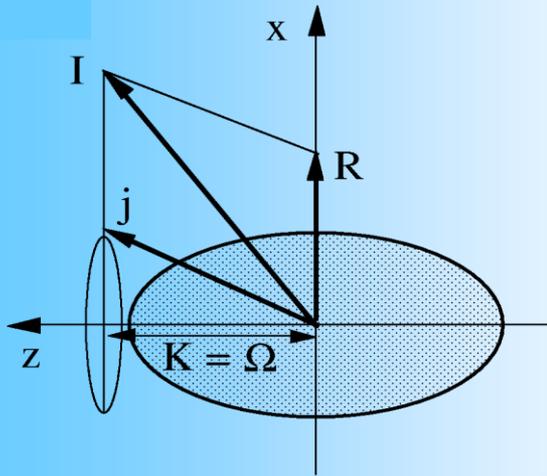
Natural parity states (positive)



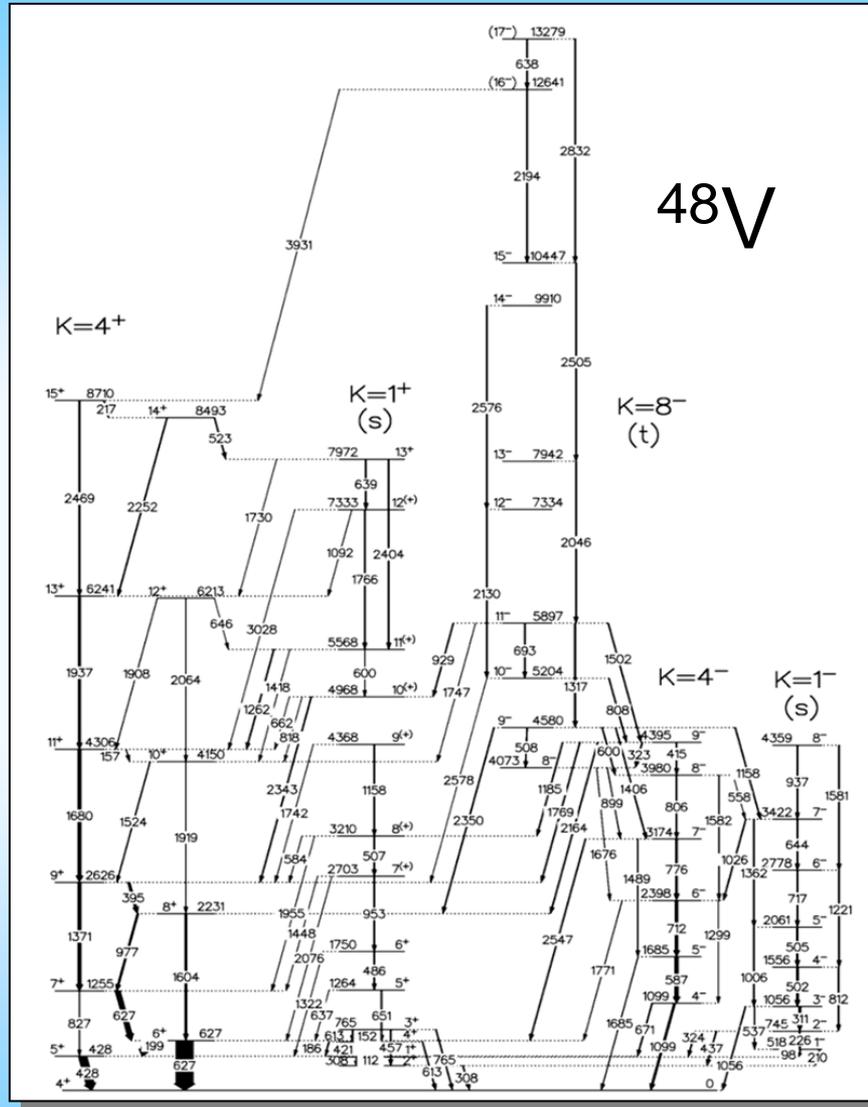
Non-natural parity states (negative)



Odd-odd ^{48}V nucleus



K is the angular momentum projection in the symmetry axis



Level scheme of the ^{48}V nucleus.

Shell Model

$$\hat{H} = -\sum_{i=1}^A \frac{\hbar^2}{2m} \nabla^2 + \frac{1}{2} \sum_{i \neq j} V(x_i, x_j) \quad \Psi = \Psi(x_1, x_2, x_3, \dots, x_A)$$

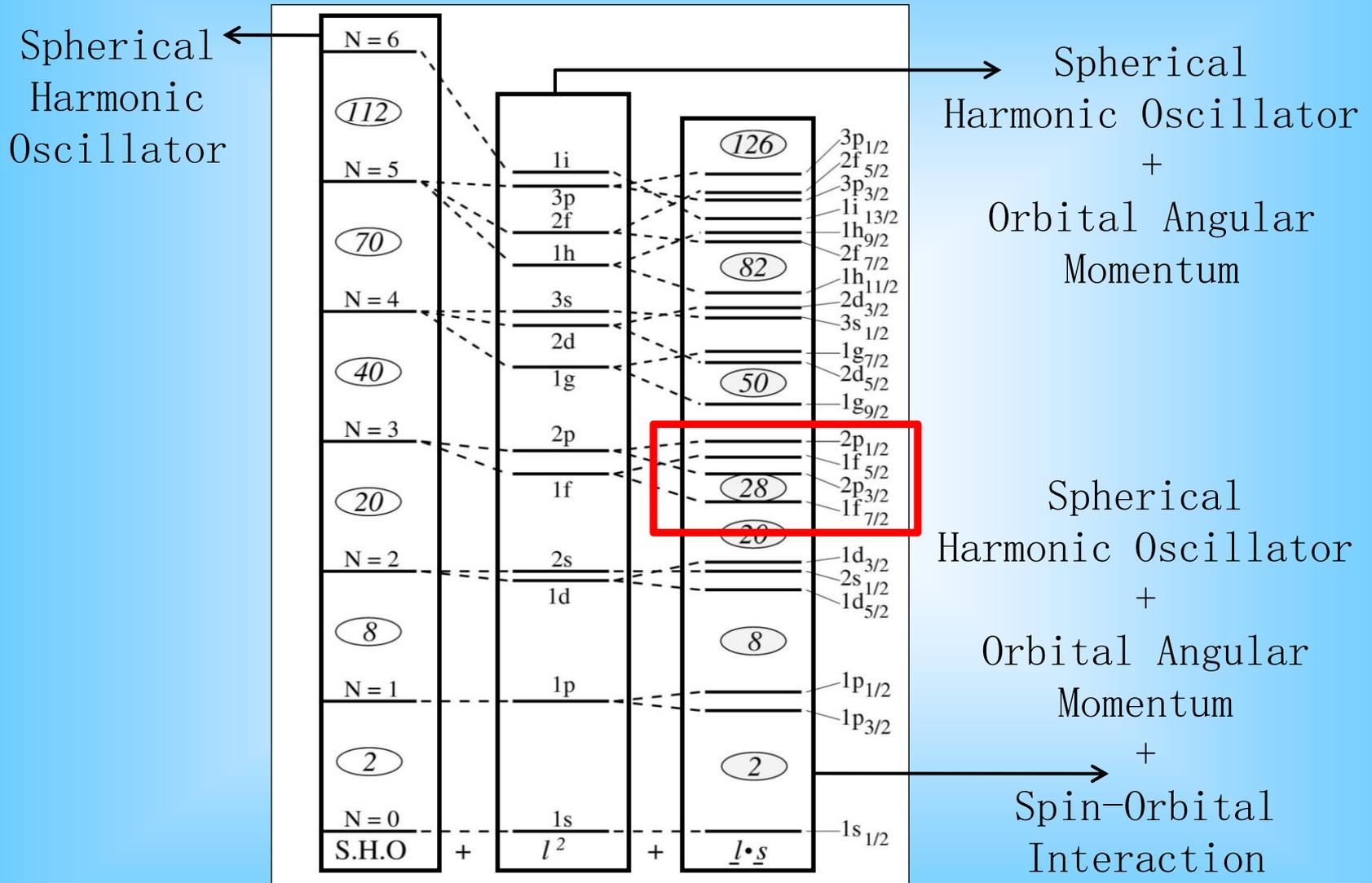
Independent Particles Approximation (mean field)

$$\Psi(x_1, x_2, \dots, x_A) = \phi_1(x_1)\phi_2(x_2)\dots\phi_A(x_A) \quad (\text{Slater determinant})$$

$$\left[-\frac{\hbar^2}{2m} \nabla^2 + V_{\text{eff}}(x_a) \right] \phi_a = E_a \phi_a$$

$$V_{\text{eff}} = \frac{1}{2} m \omega^2 r^2 + D l^2 - \mathbf{C} \mathbf{l} \cdot \mathbf{s}$$

Large Scale Shell Model



Configuration Mixing

Many valence particles

Most of the excited states are formed by mixing particle-hole configurations

$$\Psi = c_0 \Psi_{0p0h} + c_1 \Psi_{1p1h} + c_2 \Psi_{2p2h} + \dots$$

Particle-hole configurations are mixed by the two-body **residual interaction**:

$$H = T + V = T + U_{\text{eff}} + \underbrace{V - U_{\text{eff}}}$$

Mean Field Potential

Residual interaction

Basic idea of the **interacting shell model**:
Diagonalize the Hamiltonian H in the base of independent particle configurations.

Residual Interactions

70's	sd shell ^{16}O nucleus	(KB)
80's	<i>Universal sd (A~30)</i>	(USD)
80's - 2000	<i>A~50 (fp shell)</i>	(KB3, KB3G)

Collective states described by a coherent superposition of (many) single-particle states.

2004	<i>Nuclei around ^{56}Ni</i>	(GXPF1)
2009	f_5p_9 region ($1p_{3/2}$, $0f_{5/2}$, $1p_{1/2}$ and $0g_{9/2}$).	(JUN45)
2010	fpg region ($0f_{7/2}$, $1p_{3/2}$, $0f_{5/2}$, $1p_{1/2}$ and $0g_{9/2}$).	(fpg)
2010	Inclusion of the $2d_{5/2}$ orbital	(LNPS)

KB	T.T.S. Kuo and G.E. Brown, Nucl. Phys. A 114 , 241 (1968)
USD	B.H. Wildenthal, Prog. Part. Nucl. 11 , 5 (1984)
KB3	A. Poves and A. P. Zuker, Phys. Rep. 71 , 141 (1981)
KB3G	A. Poves et al., Nucl. Phys. A 694 , 157 (2001)
GXPF1	M. Honma et al., Phys. Rev. C 69 , 034335 (2004)
JUN45	M. Honma et al., Phys. Rev. C 80 064323 (2009).
fpg	K. Sieja and F. Nowacki, Phys. Rev. C 81 061303 (2010)
LNPS	S.Lenzi, K. Sieja and F. Nowacki, Phys. Rev. C 82 054301 (2010)

Large Scale Shell Model

Large configuration spaces

To have a good description of the nuclear structure with the Shell Model depends on the choice of :

- An adequate configuration space , i.e. defining the inert core and the active orbitals (number of nucleons to be excited).
- An appropriate *residual interaction*. This is the most important ingredient to have a good description of the nuclear structure.
- A code capable to solve the problem .
 To build and diagonalize the Hamiltonian matrix.

Large Scale Shell Model

Antoine code

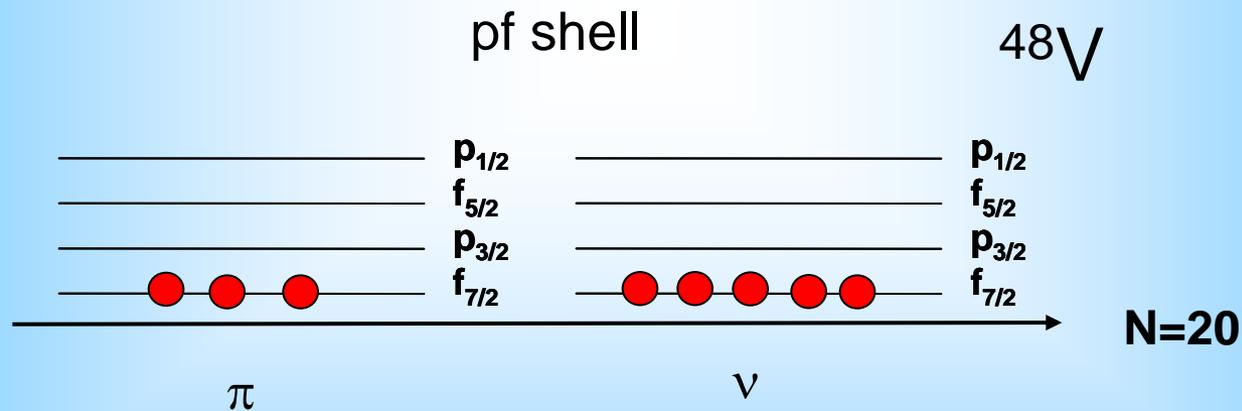
m-scheme and Lanczos method

KB3G residual interaction

Configuration space: 10^7 elements

^{40}Ca inert core

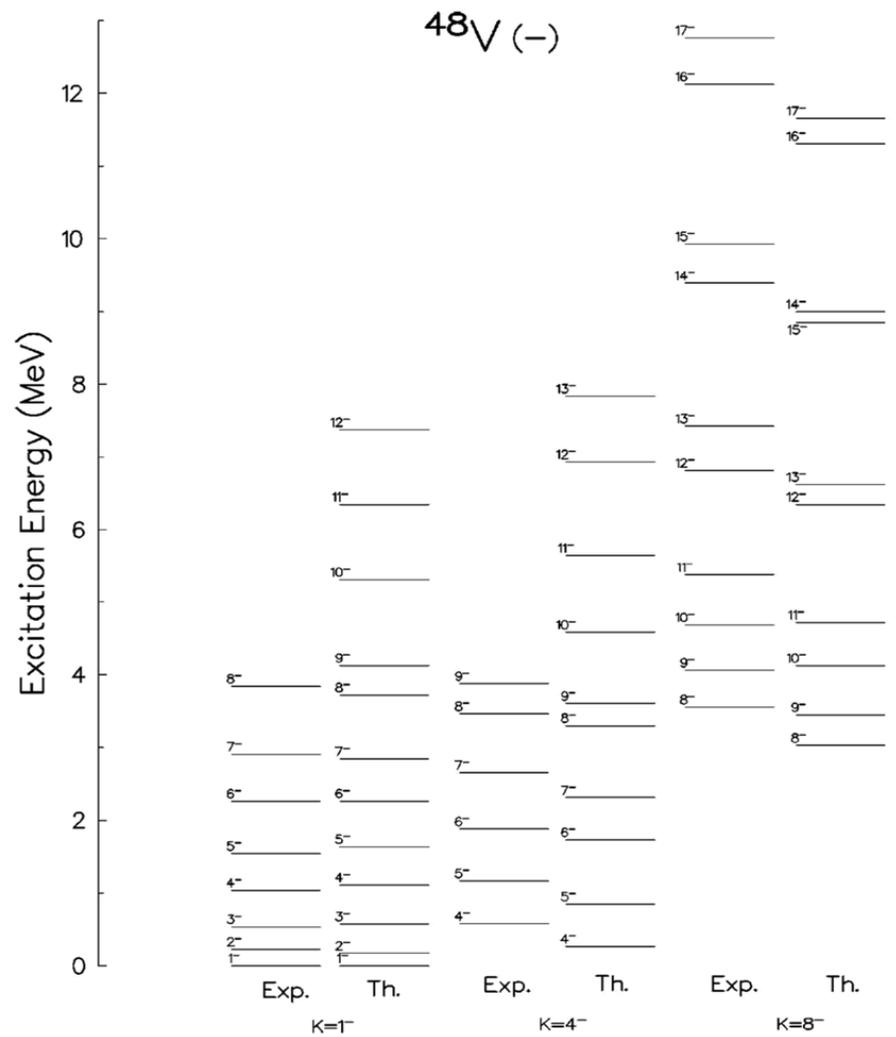
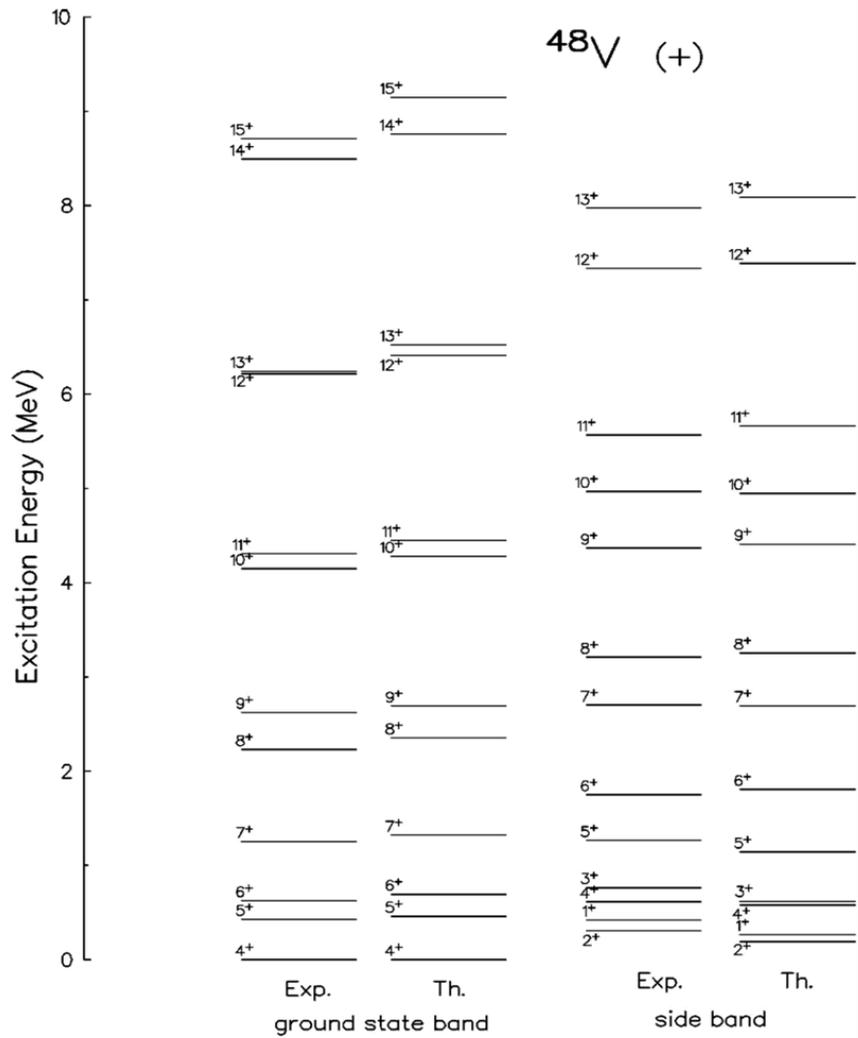
full pf shell



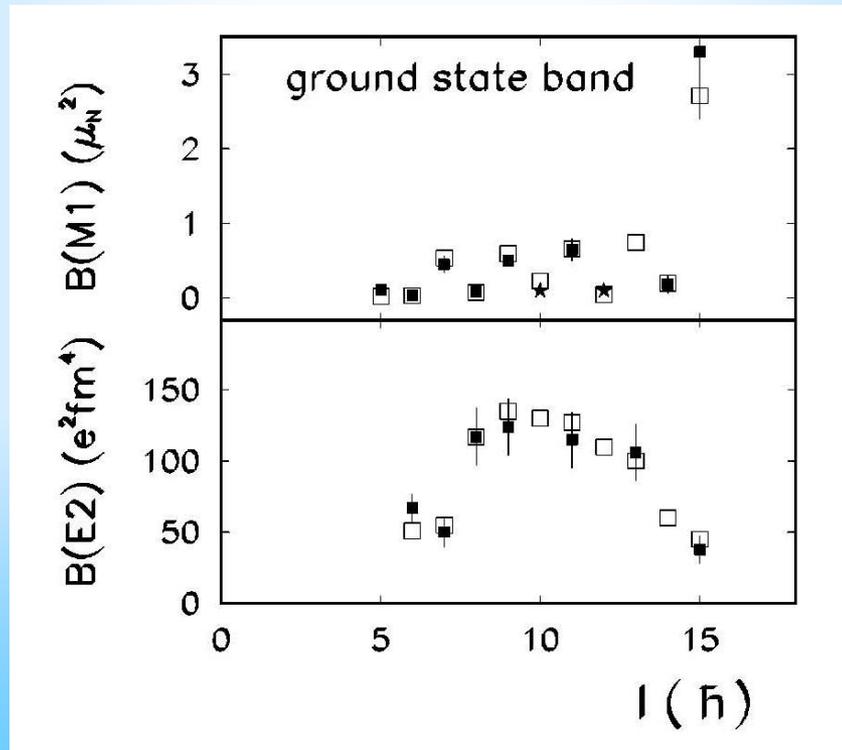
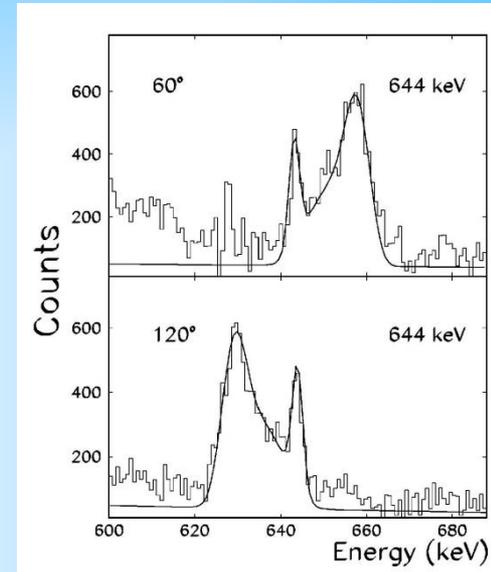
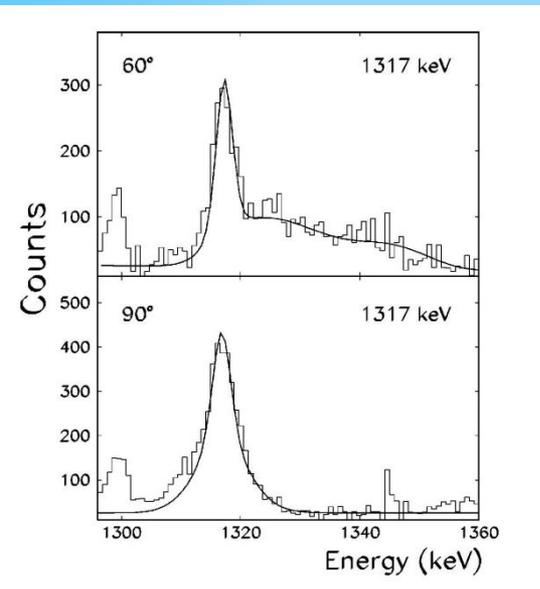
$$q_{ef}^{\pi} = 1,5e \quad \text{and} \quad q_{ef}^{\nu} = 0,5e$$

$$g_l = \begin{cases} 1 & \text{protons} \\ 0 & \text{neutrons} \end{cases}$$

$$g_s = \begin{cases} 5,586 & \text{protons} \\ -3,826 & \text{neutrons} \end{cases}$$



DSAM Lifetime measurements

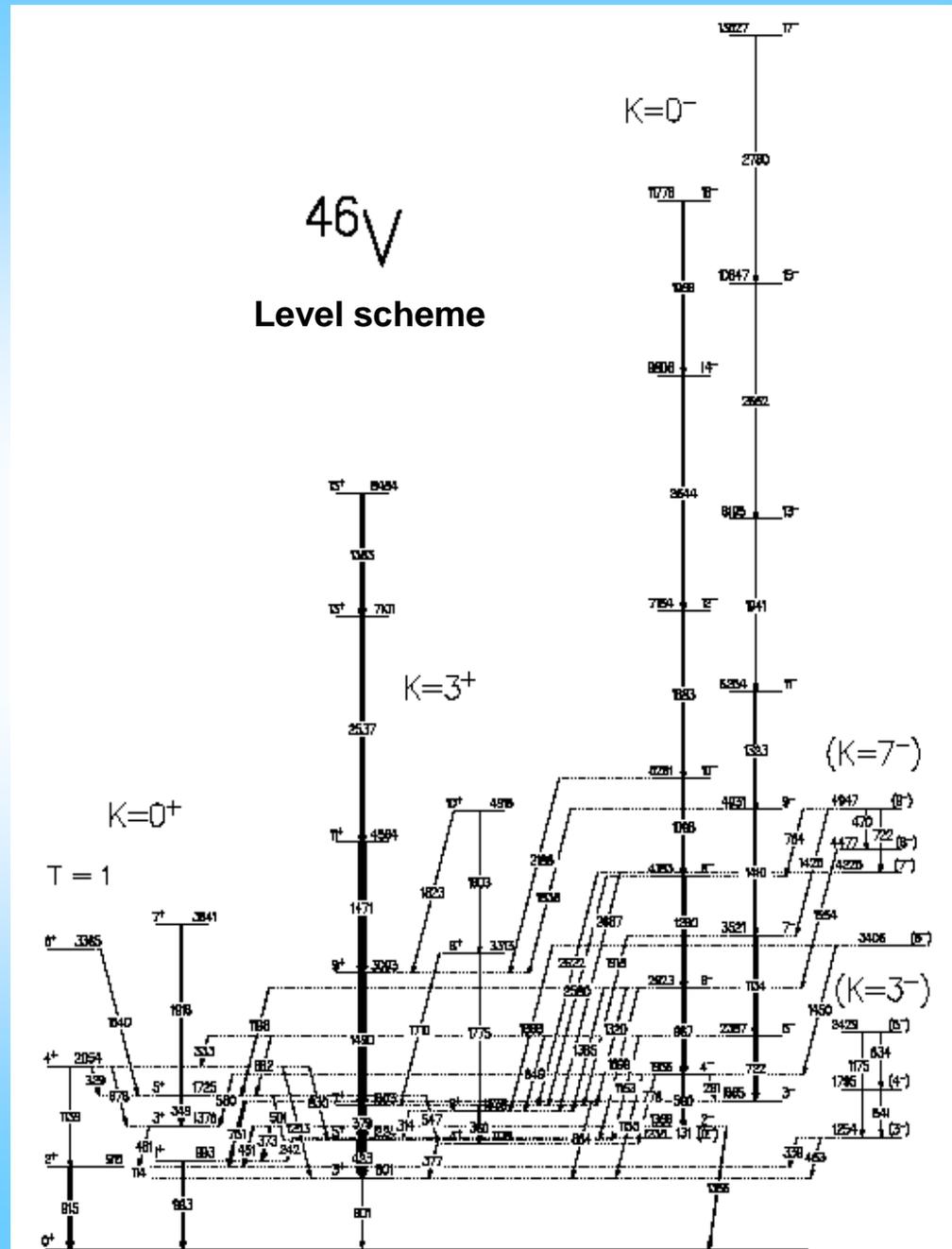


The odd-odd ^{46}V nucleus

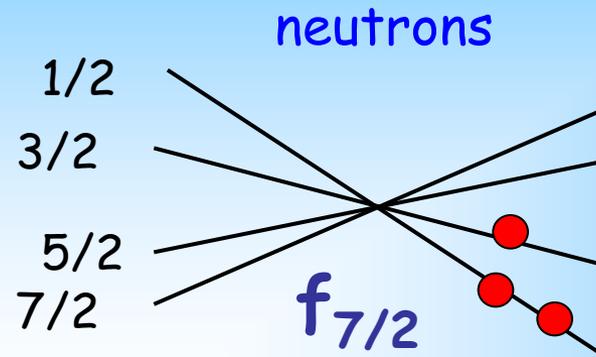
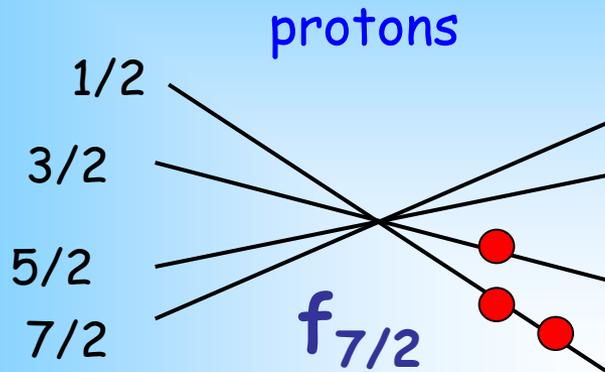
XTU Tandem accelerator (LNL)
GASP spectrometer

$^{24}\text{Mg} + ^{28}\text{Si}$ $E = 100$ MeV
(lifetime measurements)

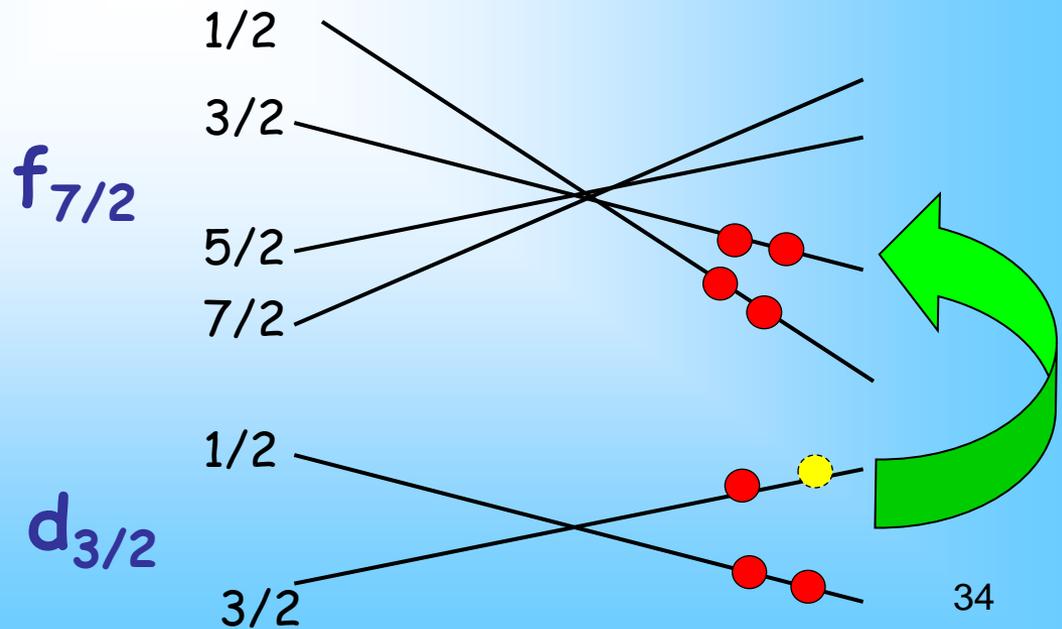
$^{28}\text{Si} + ^{24}\text{Mg}$ $E = 115$ MeV
(level scheme)



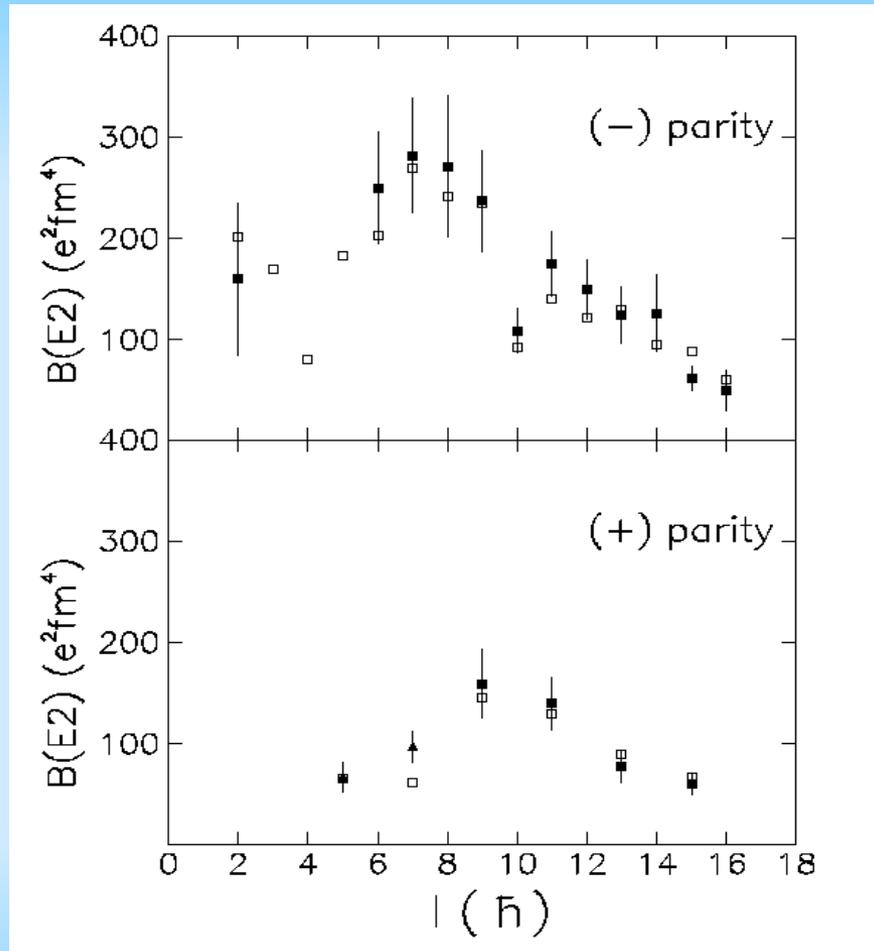
Natural parity states



Non-natural parity states



Lifetime analysis for ^{46}V .



Experimental B(E2) transition rates for positive and negative parity bands in ^{46}V . The drop for the negative parity state at $l=10^-$ is correctly predicted. This is explained by the band crossing of the $K=0^-$ with the $K=7^-$ band.

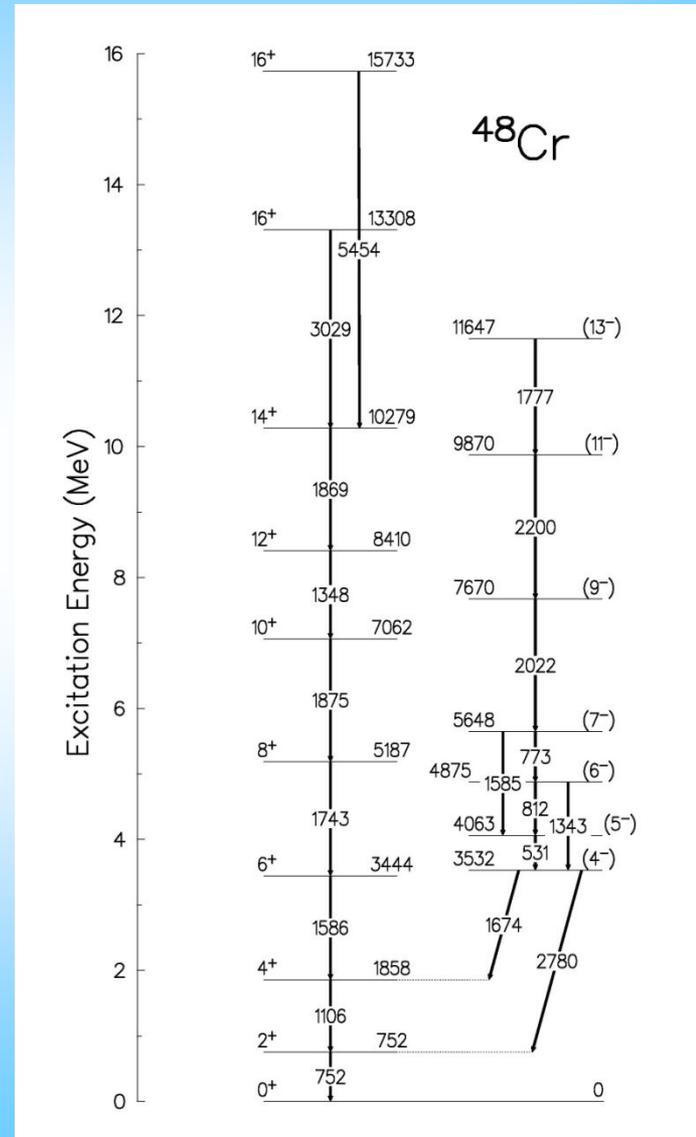
The even-even ^{48}Cr nuclei

XTU Tandem accelerator
 Laboratori Nazionali di Legnaro (LNL), Italy
 GASP γ -ray spectrometer

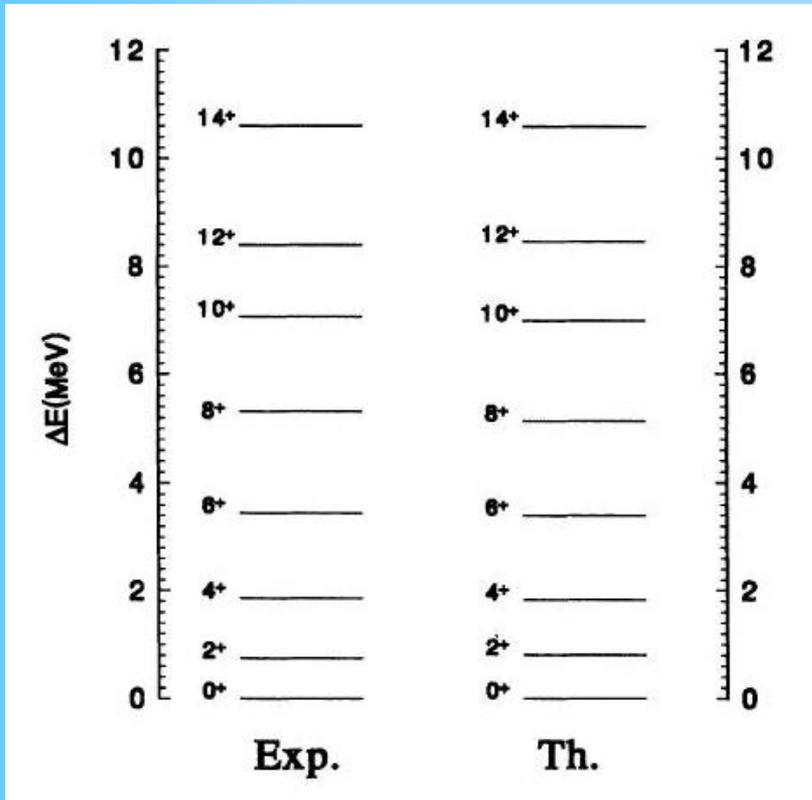
Fusion-evaporation reactions:

$^{32}\text{S} + ^{24}\text{Mg}$ $E = 130$ MeV
 (level scheme construction)

$^{28}\text{Si} + ^{28}\text{Si}$ $E = 115$ MeV
 (lifetime measurements)

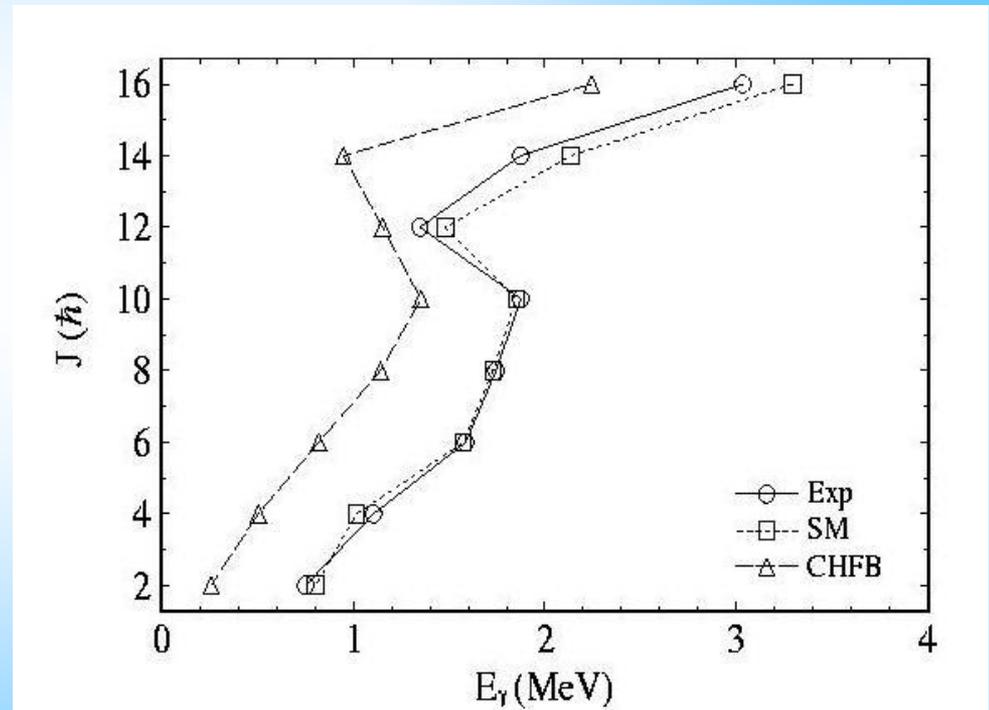


Large Scale Shell Model



Experimental levels compared to those calculated using the LSSM

Antoine code
full pf shell
KB3 residual interaction

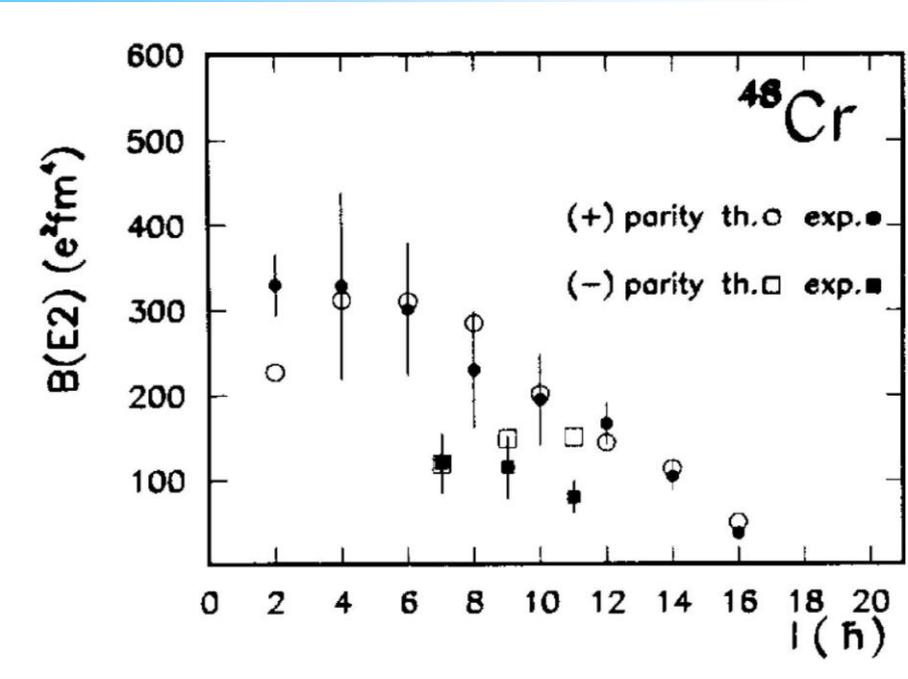
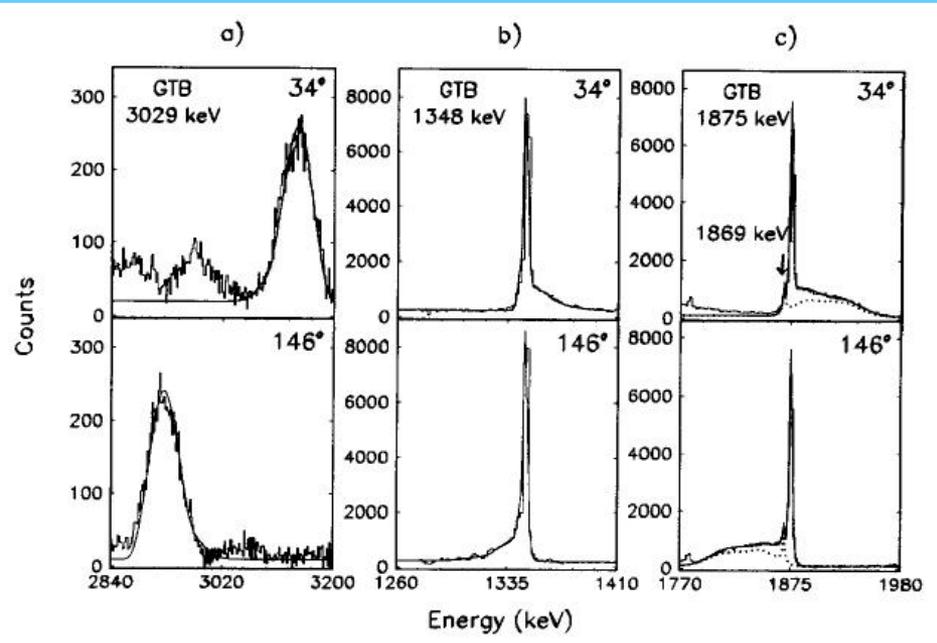


Experimental levels compared to those calculated using the LSSM and CHFB

Lineshape examples

^{48}Cr nucleus

$\beta \sim 0.28$ near the ground state
 $\beta \sim 0.1$ at $I^\pi = 16^+$



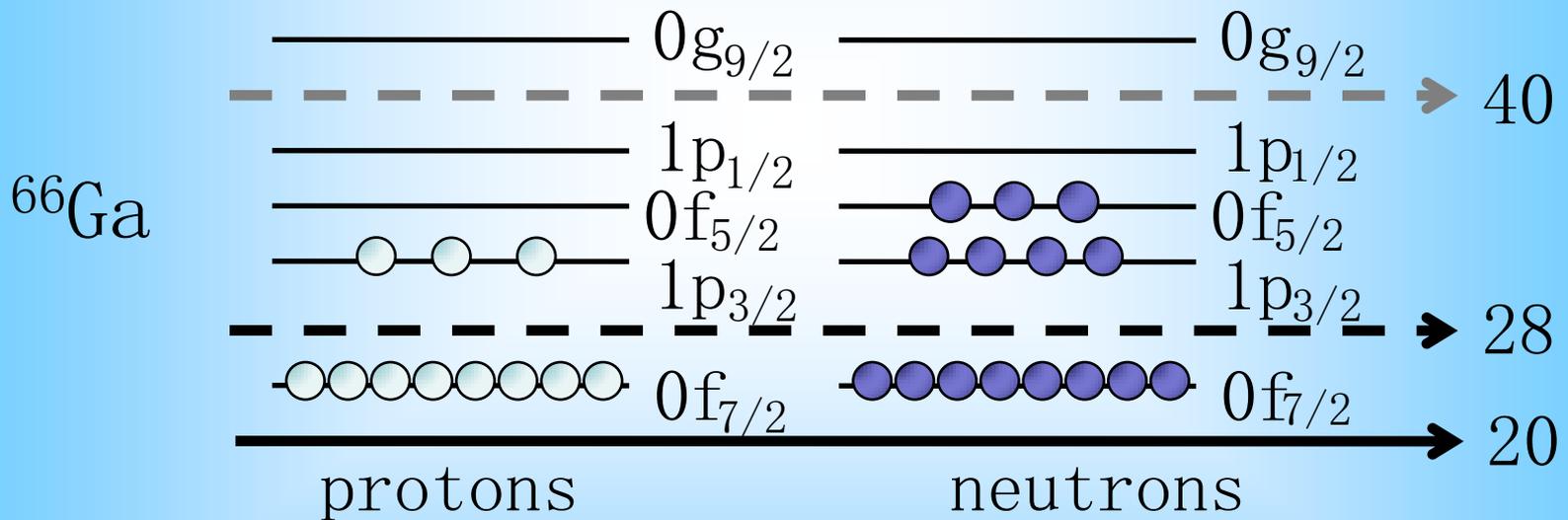
Experimental and calculated B(E2) transition rates of the positive and negative parity states.

A Systematic Study of the odd-odd $^{64,66,68,70}\text{Ga}$ nuclei

		^{65}Ge	^{66}Ge	^{67}Ge	^{68}Ge	^{69}Ge	^{70}Ge	^{71}Ge	^{72}Ge	^{73}Ge
	^{63}Ga	^{64}Ga	^{65}Ga	^{66}Ga	^{67}Ga	^{68}Ga	^{69}Ga	^{70}Ga	^{71}Ga	
^{61}Zn	^{62}Zn	^{63}Zn	^{64}Zn	^{65}Zn	^{66}Zn	^{67}Zn	^{68}Zn	^{69}Zn		

The goal of this study is to determine the role of the $0g_{9/2}$ orbital in the high spin excited states of the odd-odd $^{64,66,68,70}\text{Ga}$ nuclei.

All these Ga nuclei ($Z=31$) have valence nucleons in the upper part of the pf shell.

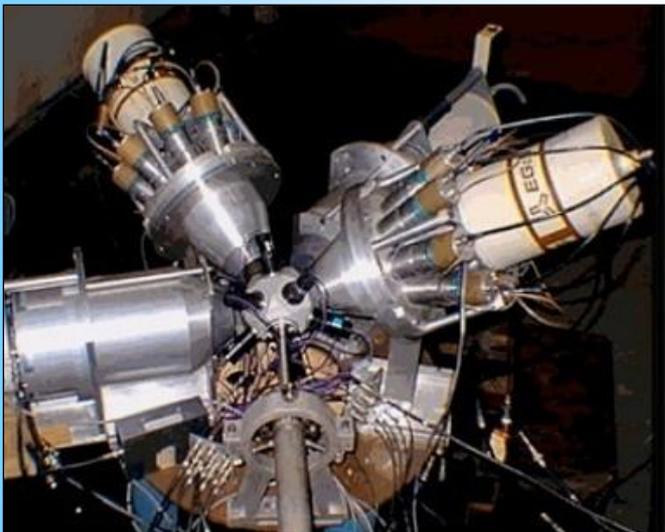


$$\pi = \prod_i^A (-1)^{l_i} = (-1)^{\sum_{i=1}^A l_i}$$

p orbital: $l=1$
 f orbital: $l=3$
 g orbital: $l=4$

Experiments performed to study the $^{64,66,70}\text{Ga}$ nuclei

- 8 MV tandem Pelletron accelerator
University of São Paulo, Brazil:
 - $^{58}\text{Ni}(^{11}\text{B},2\text{pn})^{66}\text{Ga}$, $E_{\text{beam}} = 44$ MeV.
 - $^{51}\text{V}(^{19}\text{F},\text{p}3\text{n})^{66}\text{Ga}$, $E_{\text{beam}} = 54$ MeV.
- SACI-PERERE spectrometer:

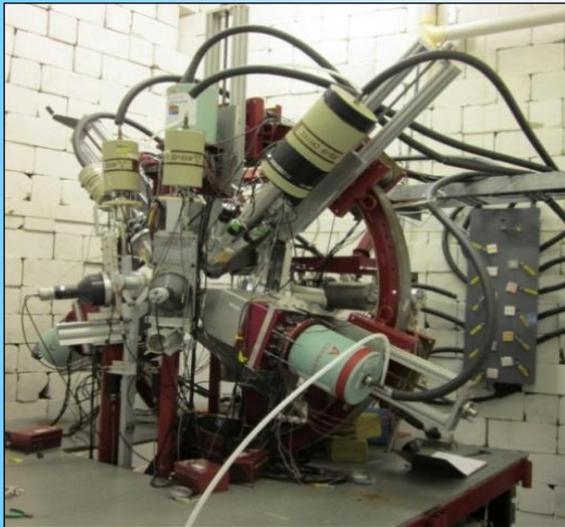


4 Compton suppressed HPGe detectors.

11 ΔE -E plastic scintillator detectors.

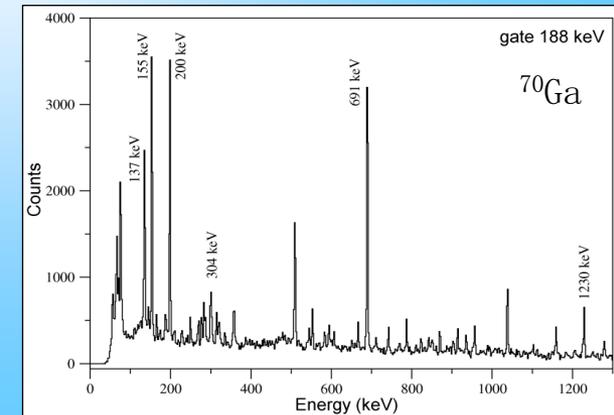
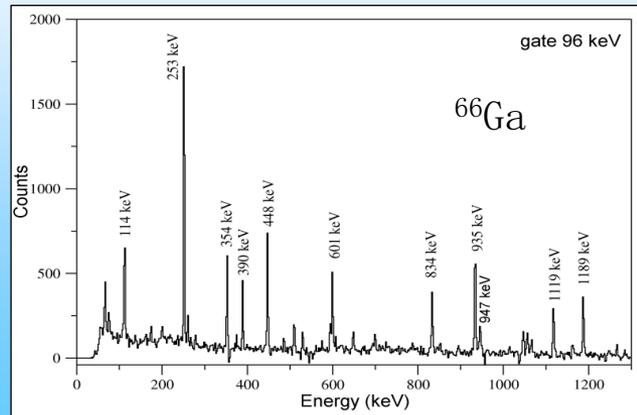
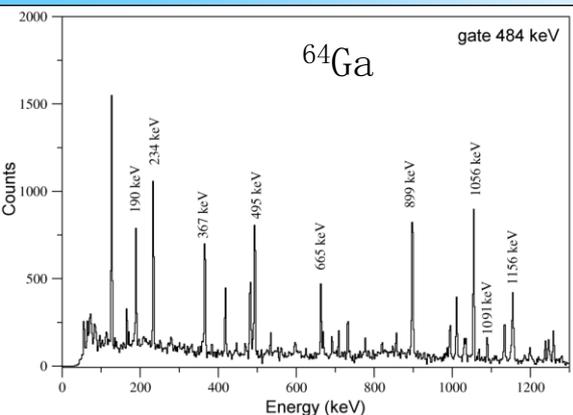
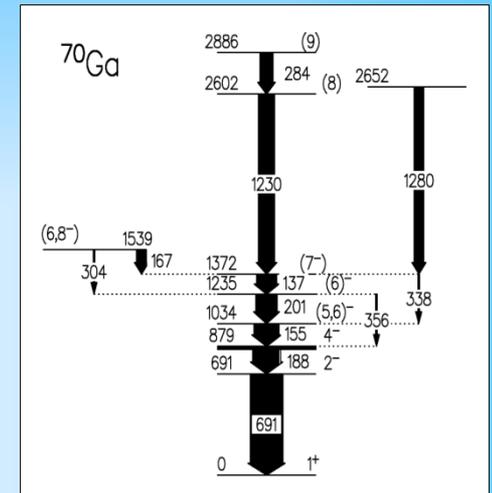
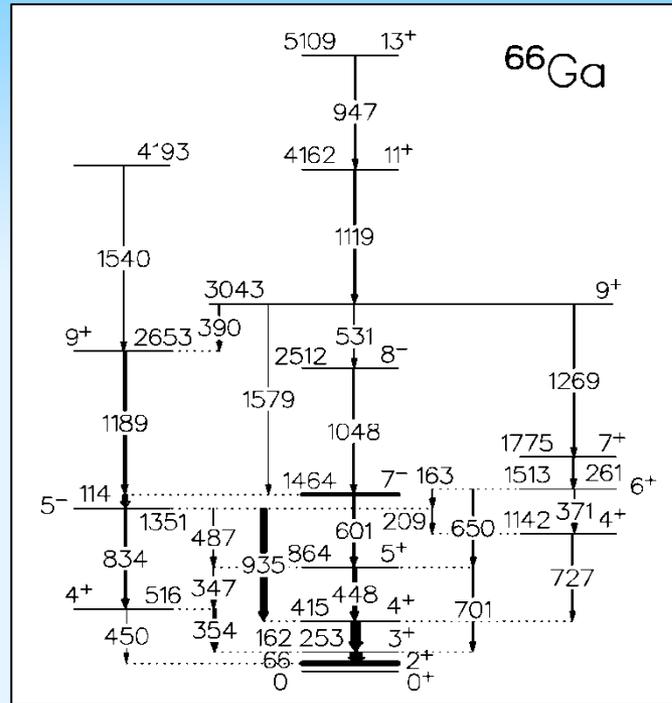
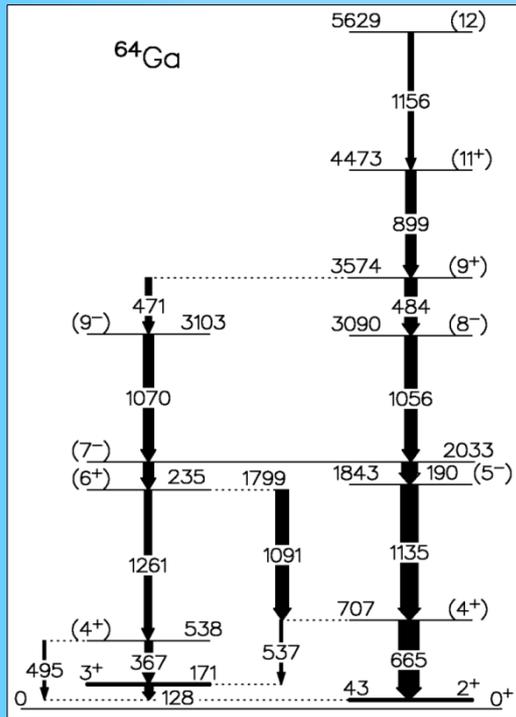
Experiments performed to study the $^{64,66,70}\text{Ga}$ nuclei

- Super-FN tandem Van de Graaff electrostatic accelerator (9 MV)
Florida State University (FSU), USA:
 - $^{58}\text{Ni}(^{12}\text{C},\alpha\text{pn})^{64}\text{Ga}$, $E_{\text{beam}} = 54$ MeV.
 - $^{55}\text{Mn}(^{18}\text{O},\alpha 3\text{n})^{66}\text{Ga}$, $E_{\text{beam}} = 67$ MeV.
 - $^{55}\text{Mn}(^{18}\text{O},2\text{pn})^{70}\text{Ga}$, $E_{\text{beam}} = 50$ MeV.
- FSU Clover Array:



7 Compton suppressed HPGe detectors.
+
3 Compton suppressed Clover
detectors (4 detectors each).

Odd-odd gallium isotope level schemes



Large Scale Shell Model

- Antoine code.

CAURIER, E and NOWACKI, F. Acta Physica Polonica B 30, (1999).

- two different effective interactions:

- JUN45 -> Developed specially for the $f_5p g_9$ region ($1p_{3/2}$, $0f_{5/2}$, $1p_{1/2}$ and $0g_{9/2}$).

HONMA, H. et al., Physical Review C 80, 064323 (2009).

- fpg -> Developed for the fpg region (**$0f_{7/2}$** , $1p_{3/2}$, $0f_{5/2}$, $1p_{1/2}$ and $0g_{9/2}$).

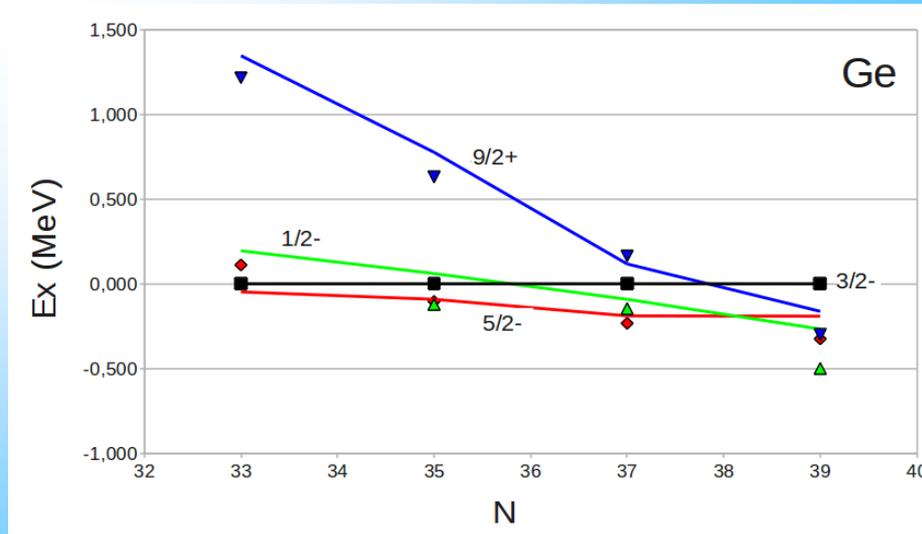
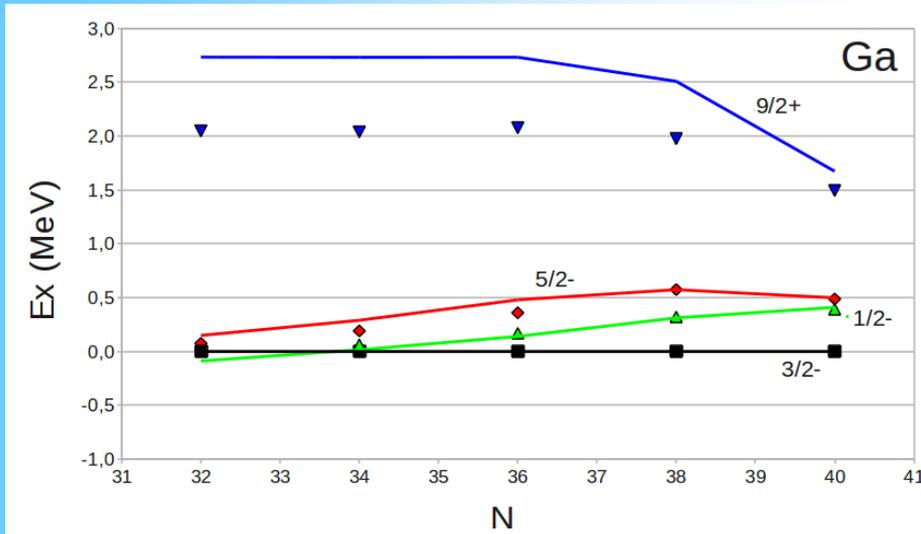
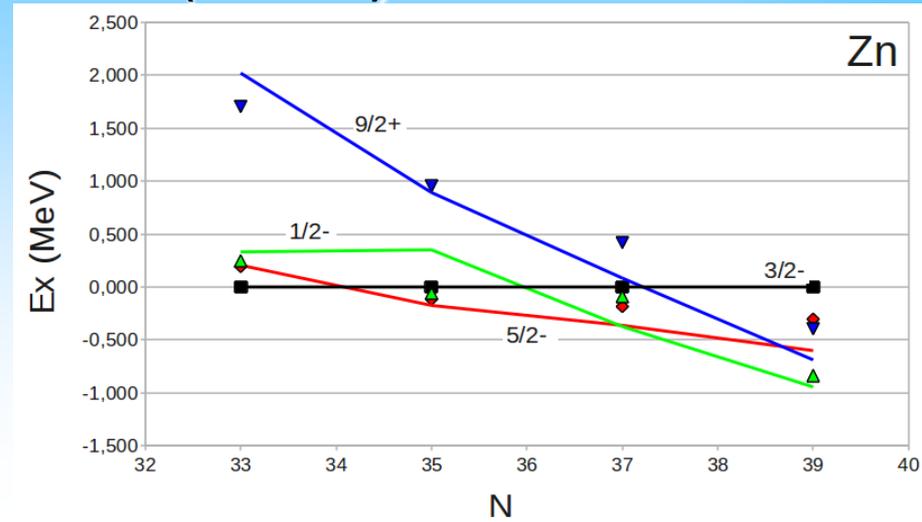
SIEJA, K. and NOWACKI, F. Physical Review C 81, 061303(R) (2010).

fpg neighbor odd nuclei: Zn (Z=30), Ga (Z=31) and Ge (Z=32)

Antoine code

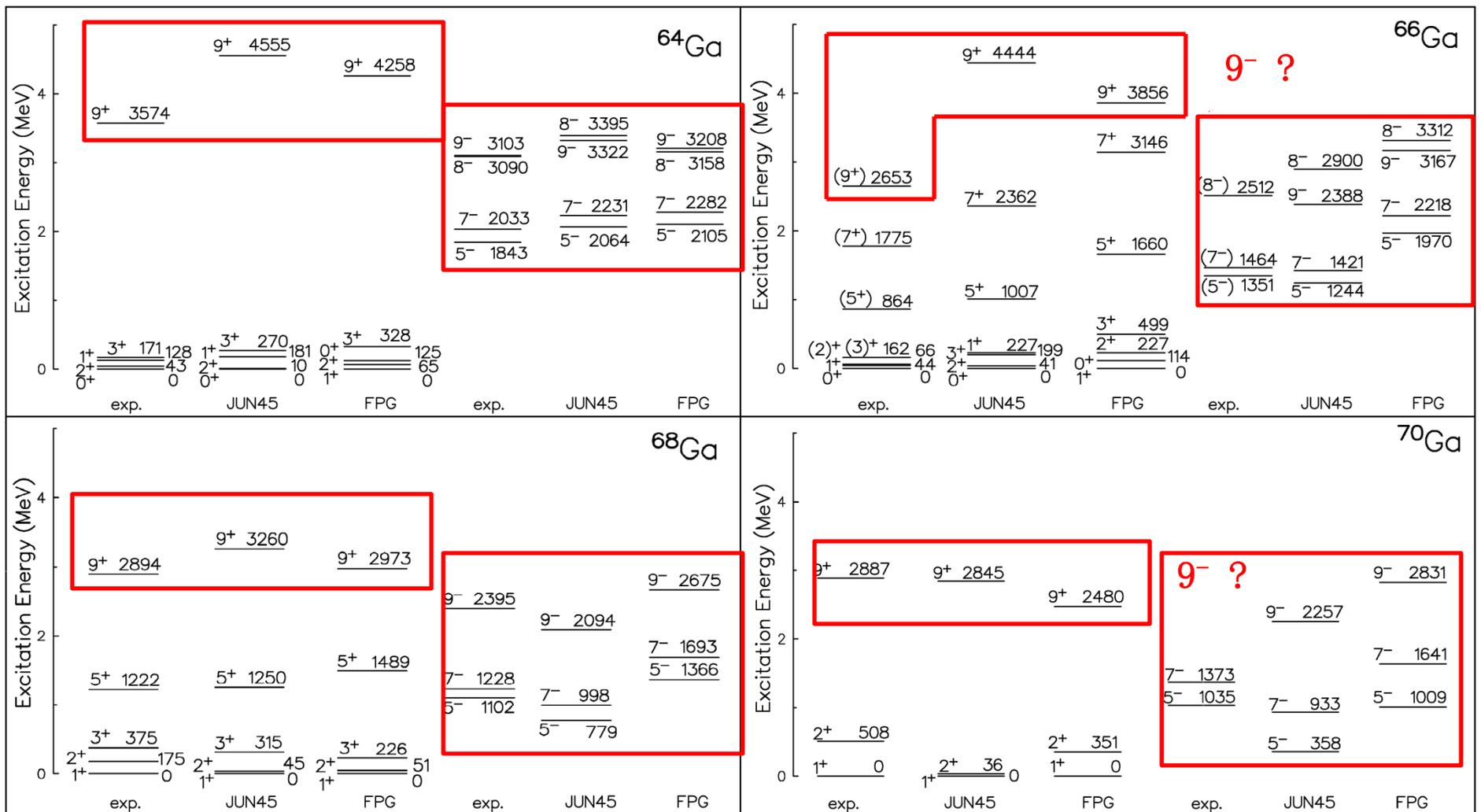
JUN45 residual interaction

$1/2^-$, $3/2^-$, $5/2^-$ and $9/2^+$ excited states



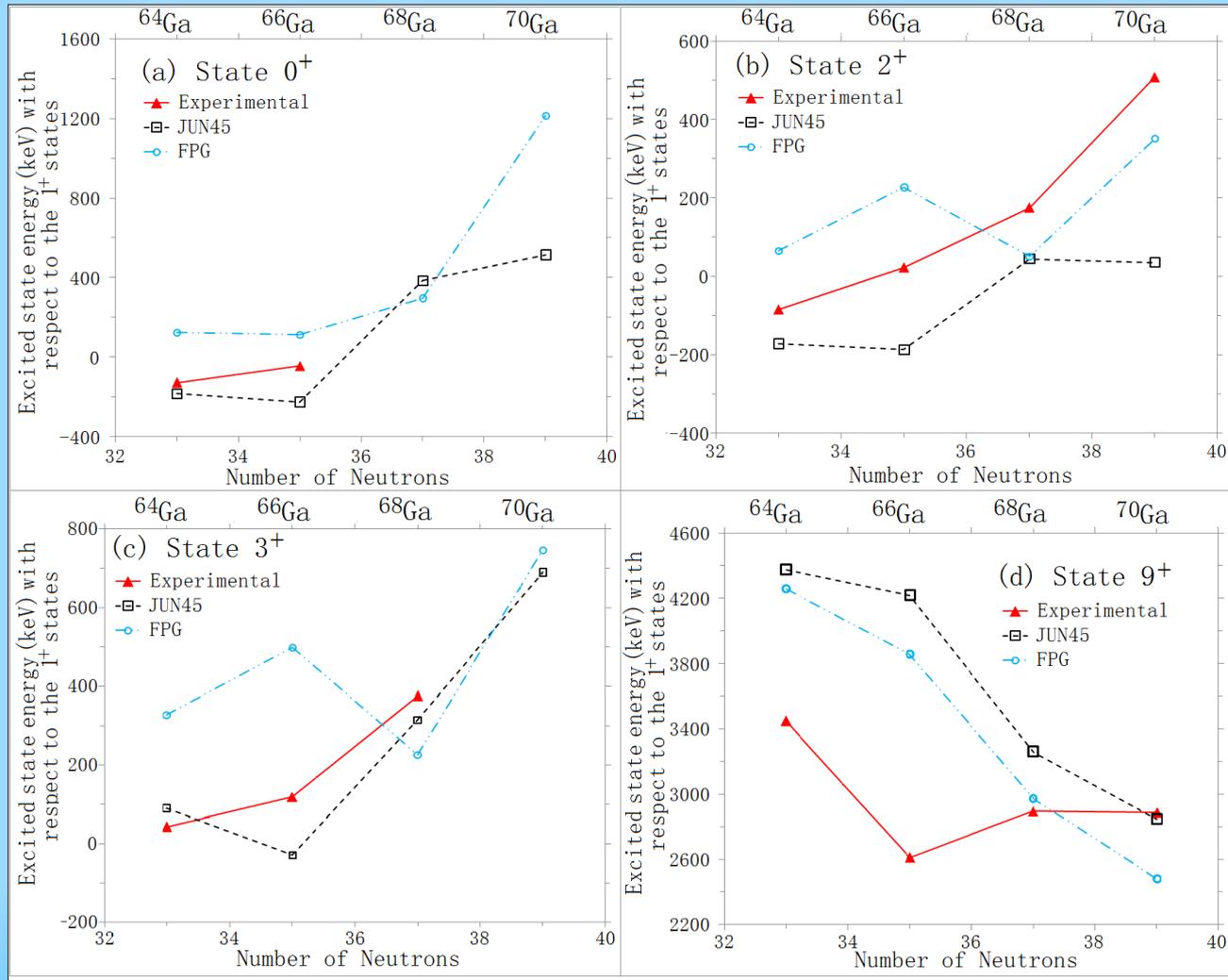
$9/2^+$ excited states are due to nucleon excitation to the $g_{9/2}$ orbital

Antoine Results for $^{64,66,68,70}\text{Ga}$

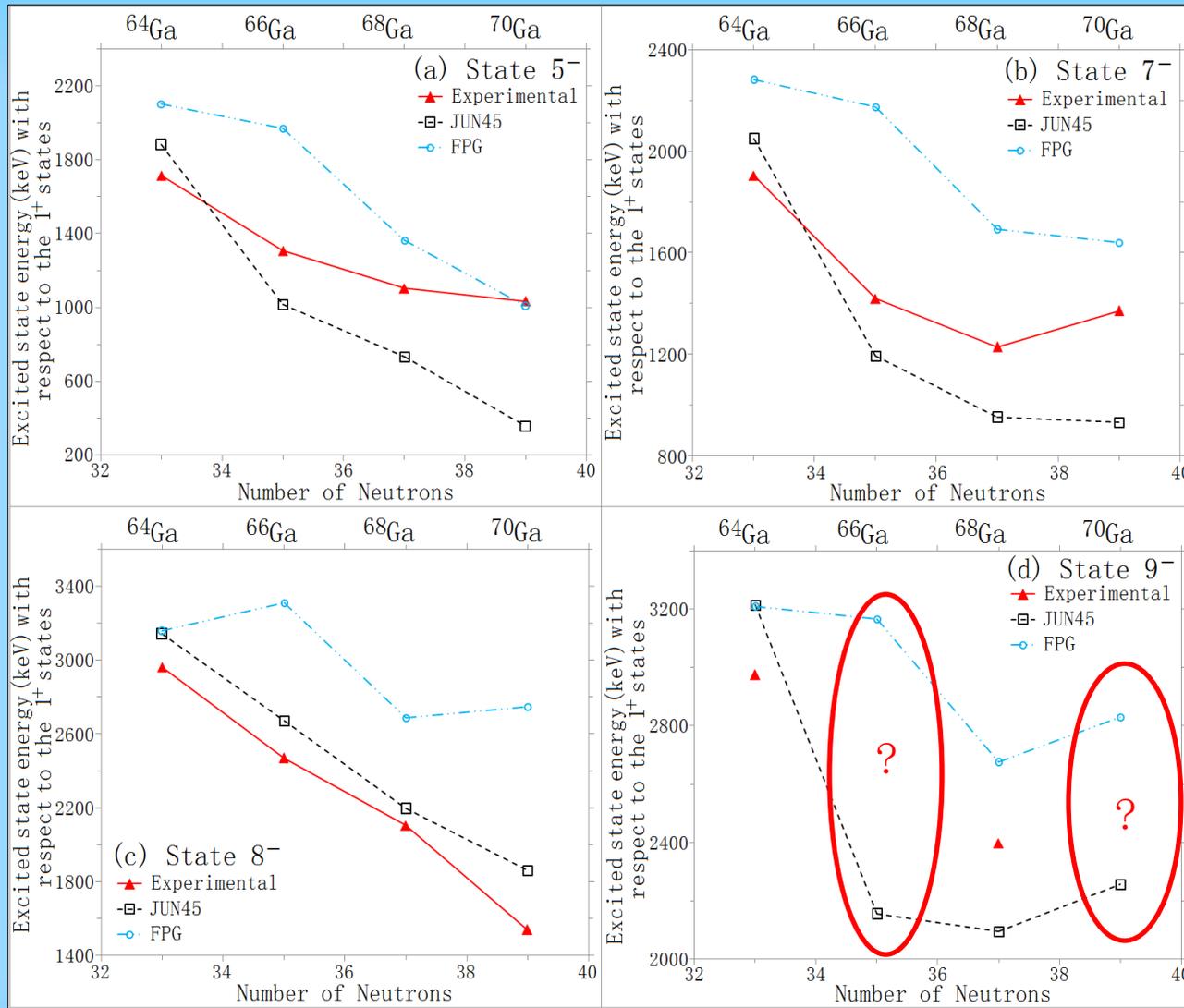


9^+ state: 1 proton and 1 neutron in the $0g_{9/2}$ orbital
 All negative parity states: one neutron in the $0g_{9/2}$ orbital

Systematic Study of $^{64,66,68,70}\text{Ga}$ nuclei

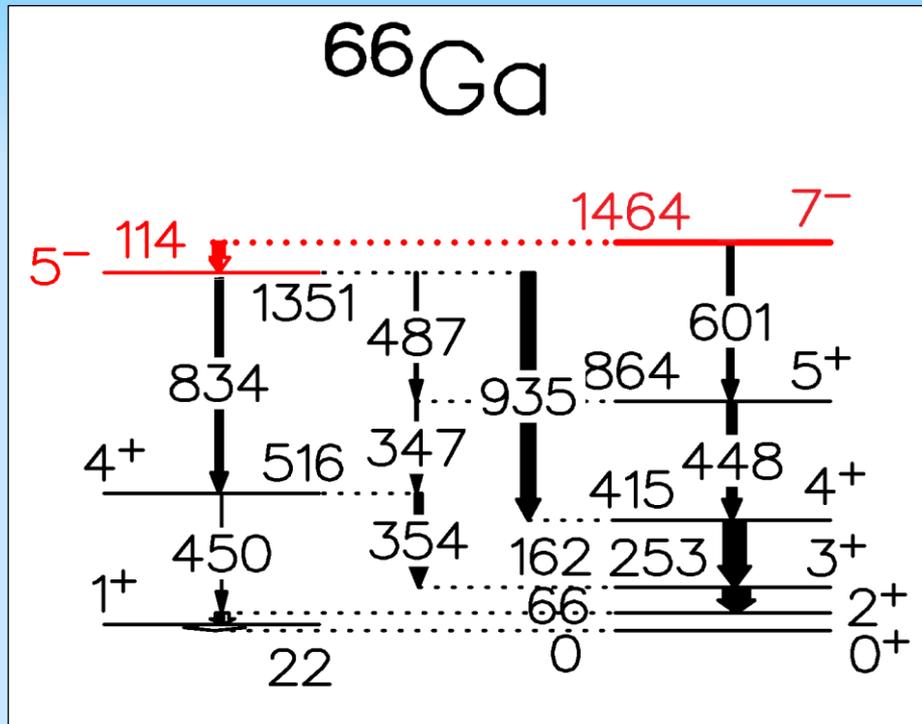


Systematic Study of $^{64,66,68,70}\text{Ga}$ nuclei



The excited states are described by particle-hole excitations and they are characterized by wave functions with large mixture of configurations.

Test of the calculated wave functions: ⁶⁶Ga 7⁻ Isomeric State E2 transition



$$B_{\text{EXP}}(E2) = \frac{\ln(2) \times I_{\gamma}}{1.23 \times 10^9 \times T_{1/2} \times I_{\text{total}} \times E_{\gamma}^5}$$

$$B(E2, J_i M_i \zeta \rightarrow J_f M_f \xi) = \frac{1}{2J_i + 1} |\langle J_f \xi || \mathbf{O}_{E2} || J_i \zeta \rangle|$$

Calculated B(E2) for the ^{66}Ga $7^- \rightarrow 5^-$ Transition

$$B(E2, J_i M_i \zeta \rightarrow J_f M_f \xi) = \frac{1}{2J_i + 1} |\langle J_f \xi || \mathbf{O}_{E2} || J_i \zeta \rangle|$$

interaction	J^π	Mix (%)	Configuration								J^π	Mix (%)	Configuration								
			protons				neutrons						protons				neutrons				
			$1p_{3/2}$	$0f_{5/2}$	$1p_{1/2}$	$0g_{9/2}$	$1p_{3/2}$	$0f_{5/2}$	$1p_{1/2}$	$0g_{9/2}$			$1p_{3/2}$	$0f_{5/2}$	$1p_{1/2}$	$0g_{9/2}$	$1p_{3/2}$	$0f_{5/2}$	$1p_{1/2}$	$0g_{9/2}$	
JUN45	7^-	10.1	2	1	0	0	4	2	0	1	5^-	5.2	2	1	0	0	4	2	0	1	
		4.7	2	1	0	0	3	3	0	1		4.0	2	1	0	0	3	3	0	1	
		10.3	2	1	0	0	2	4	0	1		7.3	2	1	0	0	2	4	0	1	
		4.6	2	1	0	0	2	2	2	1		2.5	2	1	0	0	2	2	2	1	
		4.2	1	1	1	0	2	4	0	1		4.9	1	1	1	0	2	4	0	1	
FPG	7^-	9.5	2	1	0	0	4	2	0	1	5^-	3.7	2	1	0	0	4	2	0	1	
		7.0	2	1	0	0	3	2	1	1		3.4	2	1	0	0	3	2	1	1	
		9.1	2	1	0	0	2	4	0	1		4.6	2	1	0	0	2	4	0	1	
		8.3	2	1	0	0	2	2	2	1		2.5	2	1	0	0	2	2	2	1	
													6.2	2	0	1	0	4	2	0	1
													5.0	2	0	1	0	3	2	1	1
													5.1	2	0	1	0	2	2	2	1

$$B_{\text{JUN45}}(E2) = 301 \text{ e}^2\text{fm}^4$$

$$B_{\text{fpg}}(E2) = 259 \text{ e}^2\text{fm}^4$$

Experimental B(E2) for the $^{66}\text{Ga } 7^- \rightarrow 5^-$ Transition

Two known values for the $^{66}\text{Ga } 7^-$ isomeric state:

$$T_{1/2} = 57.3 (14) \text{ ns} \quad \text{or} \quad T_{1/2} = 39 (2) \text{ ns}$$

A. Filevich et al., Nucl. Phys. A, 295, 513, 1978.

T. Kouda et al., Ann. Rep. 1996, Radio-isotope Center, Tohoku University, Japan, p. 19, 1997.

SISMEI spectrometer

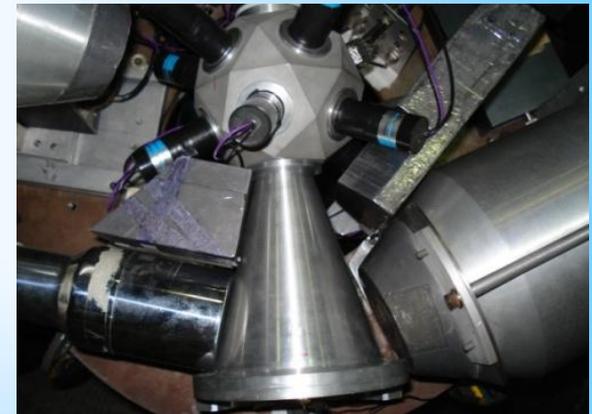
$^{58}\text{Ni}(^{11}\text{B}, 2pn)^{66}\text{Ga}$, $E_{\text{beam}} = 45 \text{ MeV}$

$$T_{1/2} = 58.1 (12) \text{ ns}$$

$$B_{\text{EXP}}(\text{E2}) = 242 (6) \text{ e}^2\text{fm}^4$$

$$B_{\text{JUN45}}(\text{E2}) = 301 \text{ e}^2\text{fm}^4$$

$$B_{\text{fpg}}(\text{E2}) = 259 \text{ e}^2\text{fm}^4$$



D.L. Toufen, Master Thesis, Universidade de São Paulo (2008).

Conclusion

In-beam γ -ray spectroscopy

High spin states

Nuclear Shapes

Shape coexistence

Superdeformed shapes

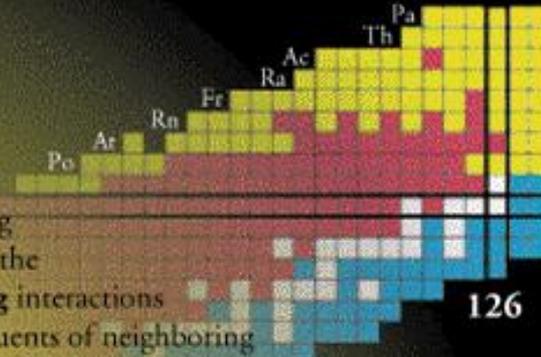
Large Scale Shell Model

fp shell

$^{46,48}\text{V}$ and ^{48}Cr

fpg shell

$^{64,66,68,70}\text{Ga}$



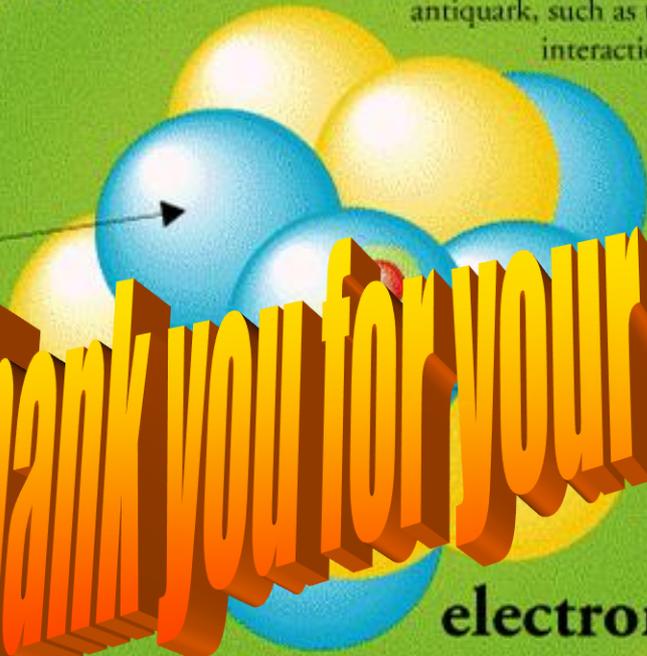
The Nucleus

$(1-10) \times 10^{-15} \text{ m}$

At the center of the atom is a nucleus formed from **nucleons**—protons and neutrons. Each nucleon is made from three **quarks** held together by their strong interactions, which are mediated by gluons. In turn, the nucleus is held together by the **strong** interactions between the gluon and quark constituents of neighboring nucleons. Nuclear physicists often use the exchange of mesons—particles which consist of a quark and an antiquark, such as the **pion**—to describe interactions among the nucleons.

neutron
 10^{-15} m
proton

Thank you for your attention



quark
 $< 10^{-19} \text{ m}$

electromagnetic field

In an atom, **electrons** range around the nucleus at distances typically up to 10,000 times the nuclear diameter. If the electron cloud were shown to scale, this chart would cover a small town.

